



Physiologically structured population models: Formulation, analysis and **ecological insights**

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in collaboration with

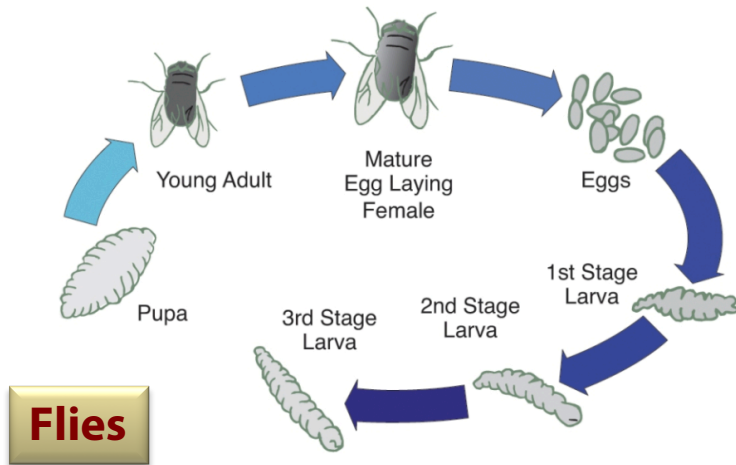
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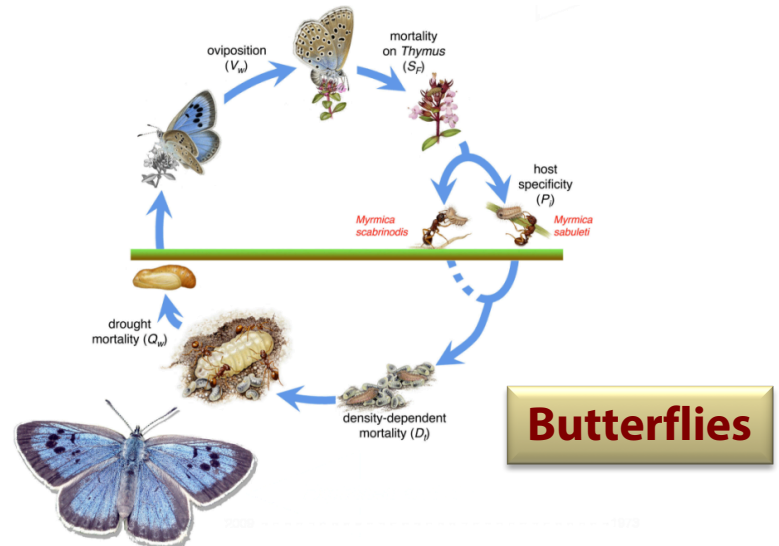




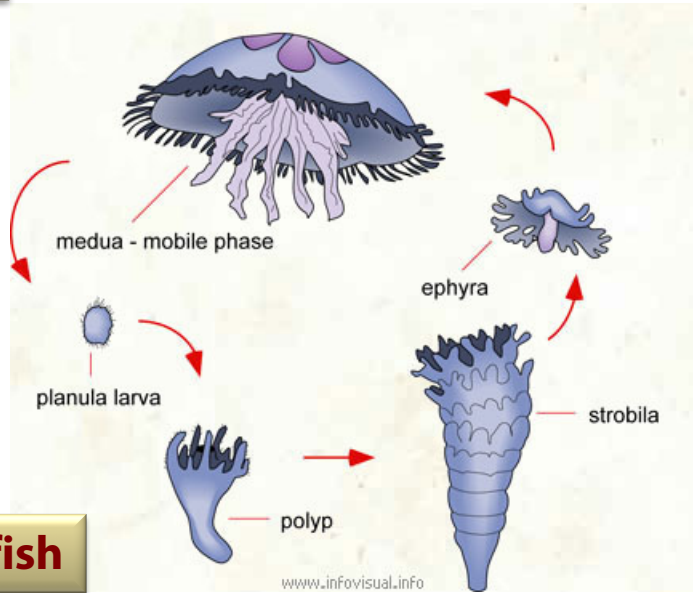
Development predominates



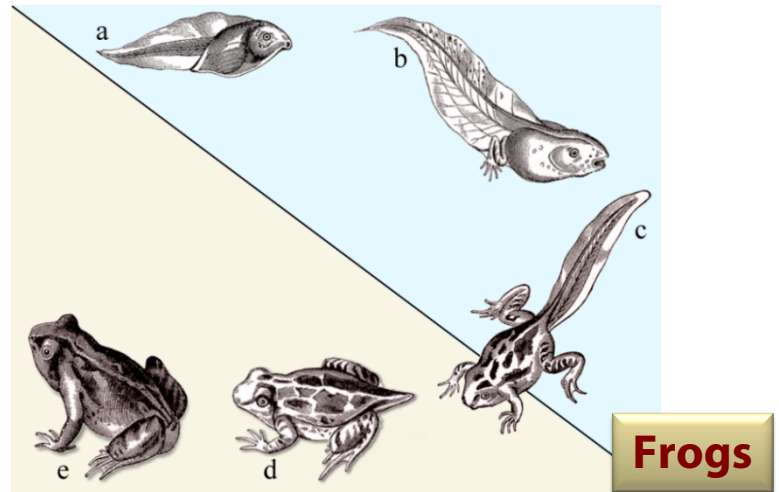
Flies



Butterflies



Jellyfish

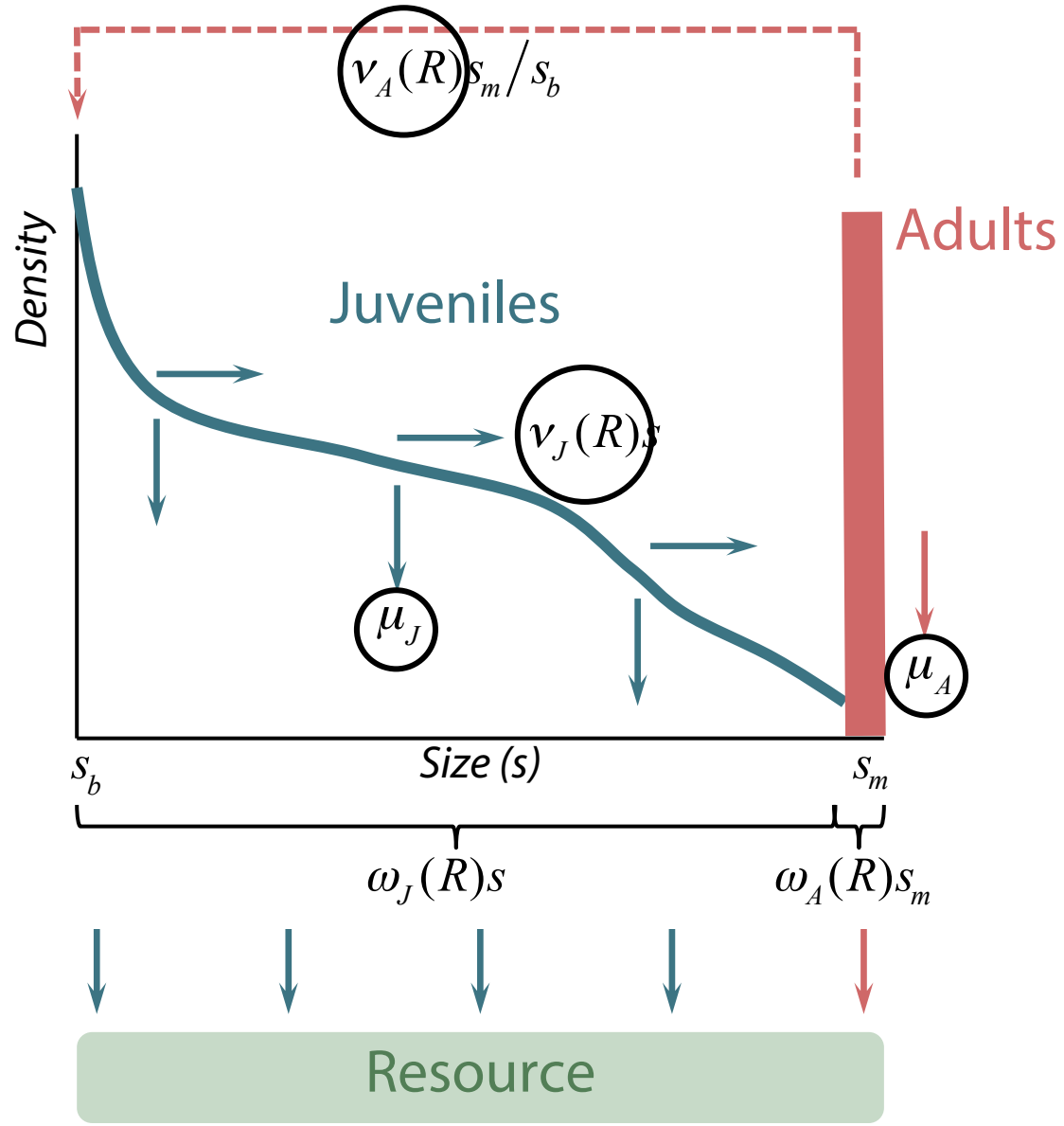


Frogs

Individual ecology changes over life!



The size-structured population model





The size-structured population model

$$\frac{\partial c(t, s)}{\partial t} + \nu_J(R) \frac{\partial (sc(t, s))}{\partial s} = -\mu_J c(t, s) \quad \text{for } s_b \leq s < s_m$$

$$\nu_J(R) s_b c(t, s_b) = \frac{\nu_A(R) s_m}{s_b} C_A(t)$$

$$\frac{dC_A}{dt} = \nu_J(R) s_m c(t, s_m) - \mu_A C_A(t)$$

$$\frac{dR}{dt} = \rho(R_{max} - R) - \omega_J(R) \int_{s_b}^{s_m} sc(t, s) ds - \omega_A(R) s_m C_A(t)$$

Mass conservation:

Juvenile **growth** and adult **reproduction** proportional to body size:

$$g(s, R) = \nu_J(R) s = (\sigma \omega_J(R) - T) s$$

$$b(s_m, R) = \frac{\nu_A(R) s_m}{s_b} = \frac{(\sigma \omega_A(R) - T) s_m}{s_b}$$



A bit of modelling philosophy

Does your model fit my system?

Most likely, not at all!

Does it provide insight about my system?

Probably yes!

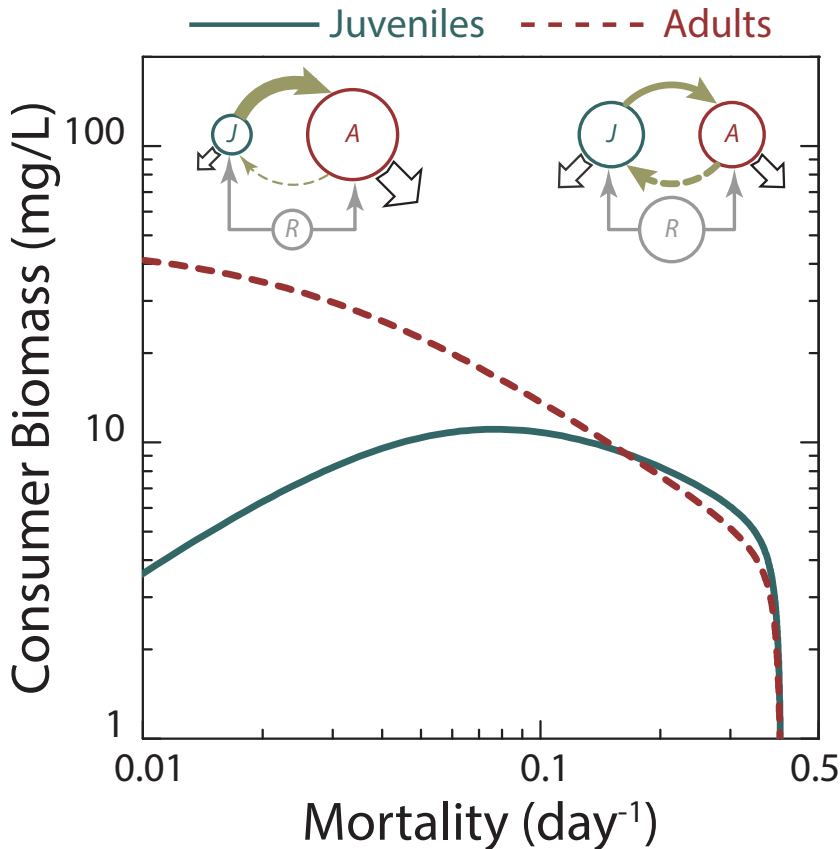
Model (equations) are just a vehicle to gain insight about an ecological system. It is these insights and their implications that matter



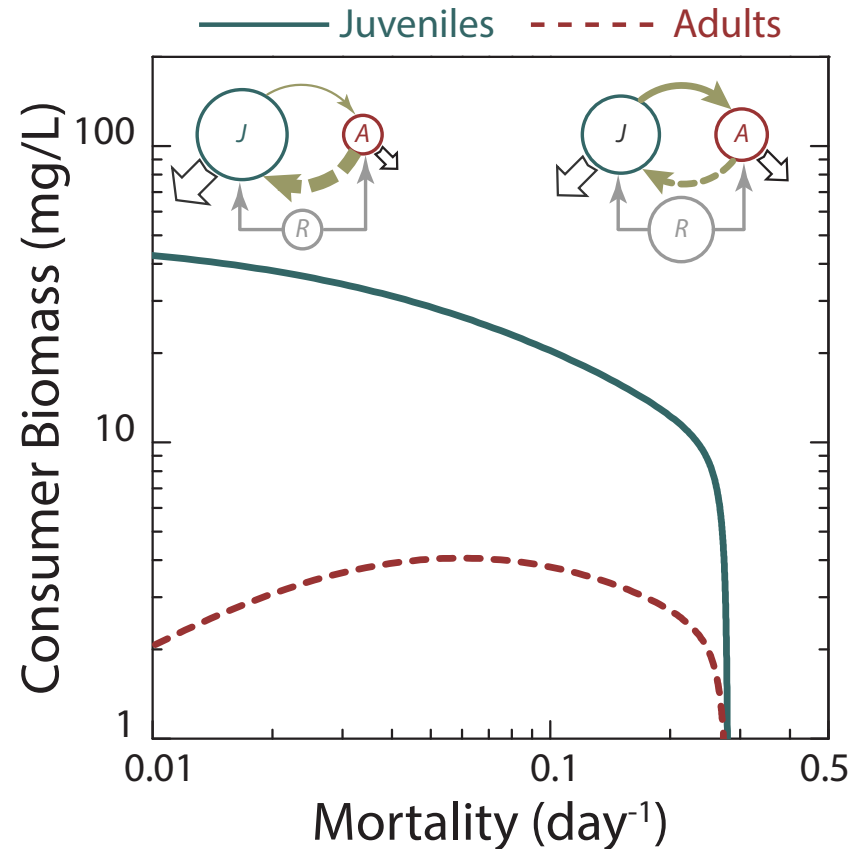
Ontogenetic asymmetry

$$\nu_J(\tilde{R}) > \nu_A(\tilde{R}) > 0$$

$$\nu_A(\tilde{R}) > \nu_J(\tilde{R}) > 0$$



Reproduction control
Mortality increases
juvenile biomass

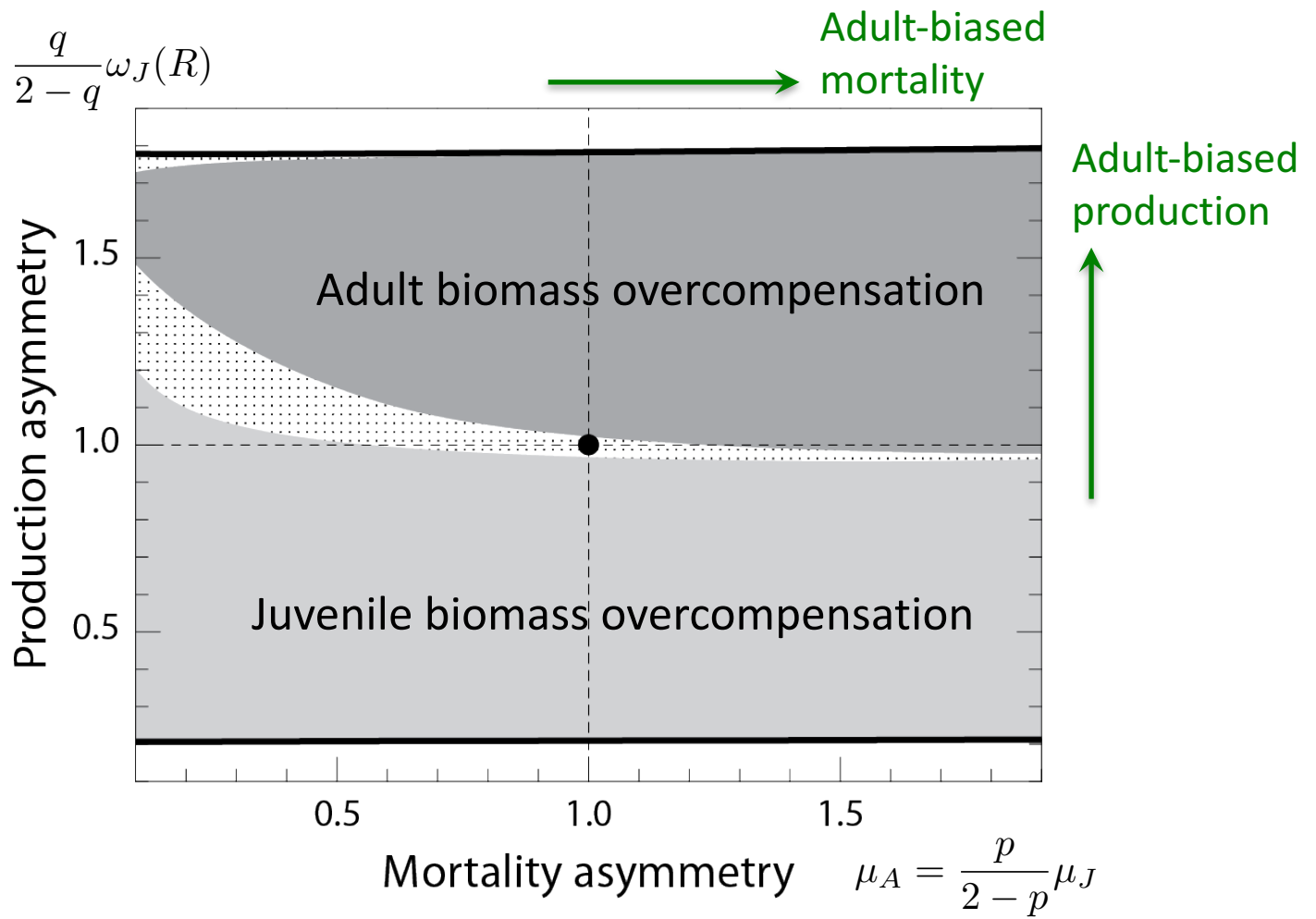


Development control
Mortality increases
adult biomass



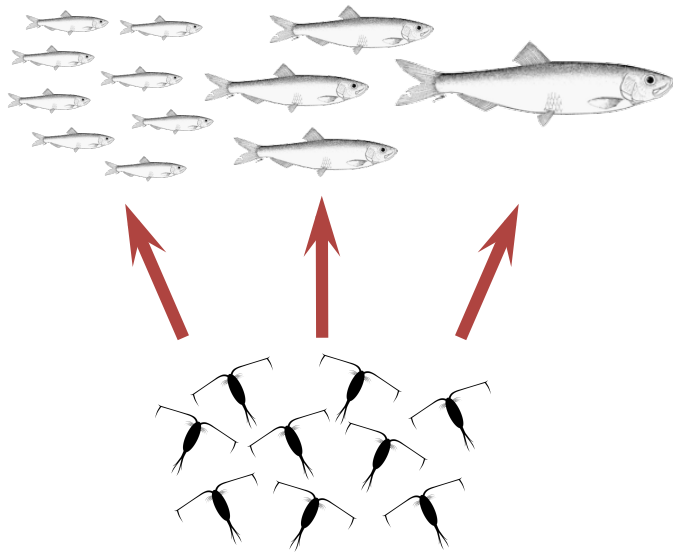
Overcompensation is (almost) everywhere

$$\omega_A(R) = \frac{q}{2-q} \omega_J(R)$$

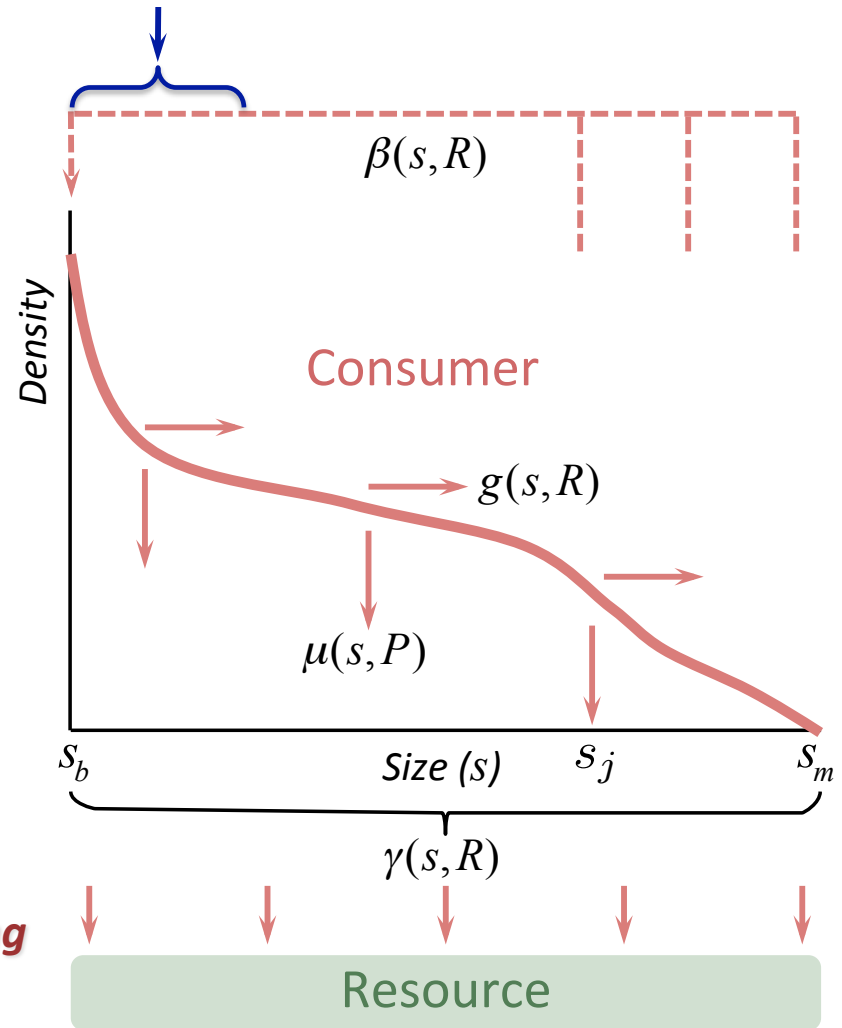


- Predictions for (unstructured) cases with ontogenetic symmetry hold under limited conditions
- Overcompensation mostly influenced by production asymmetry, little influence of mortality asymmetry

Life history based on Kooijman's DEB model



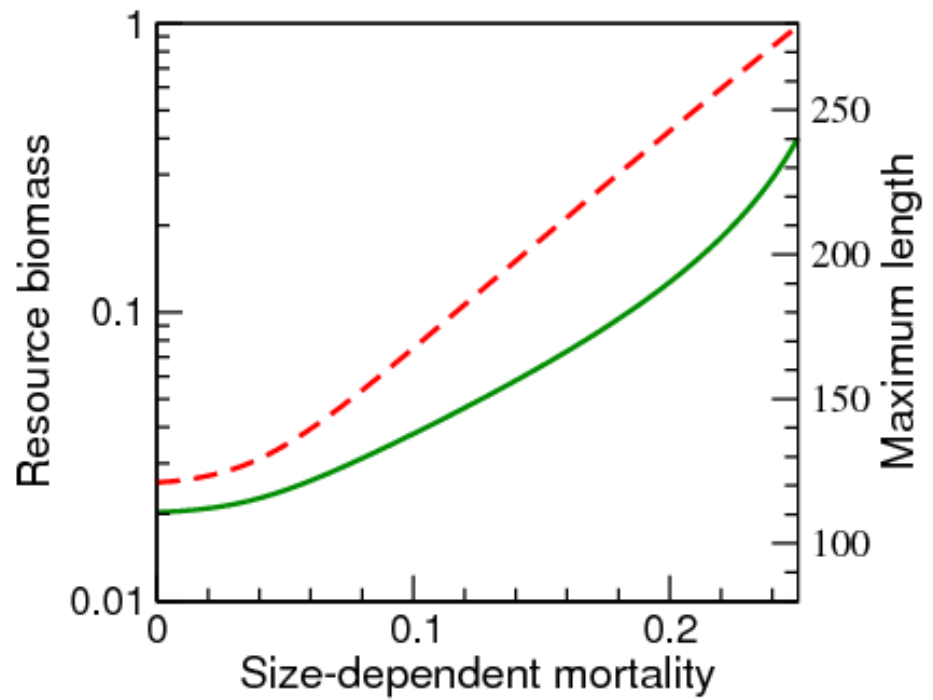
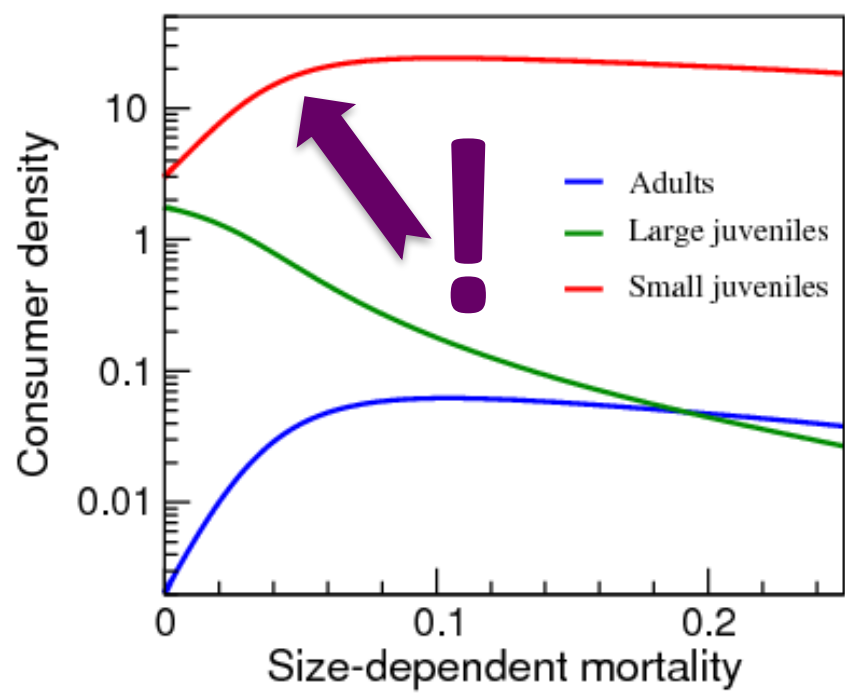
Increased mortality



- *Ingestion scales allometrically with size*
- *Adults continue growing, while reproducing*
- *Food-dependent growth and reproduction*
- *Maturation when reaching size threshold*



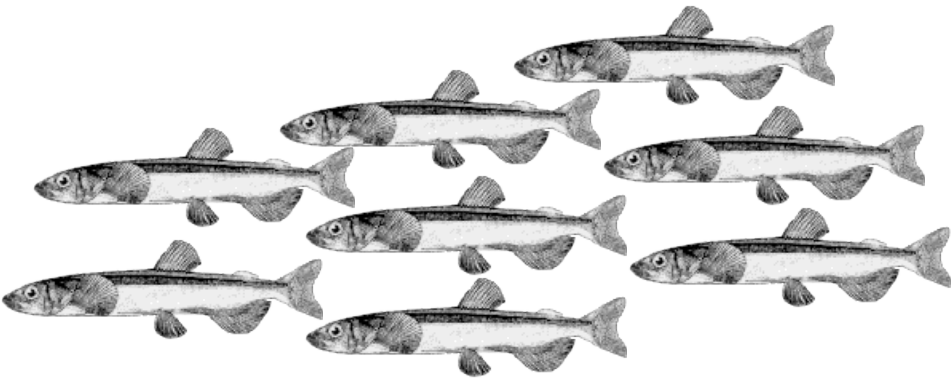
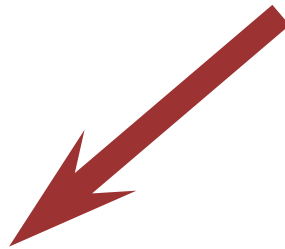
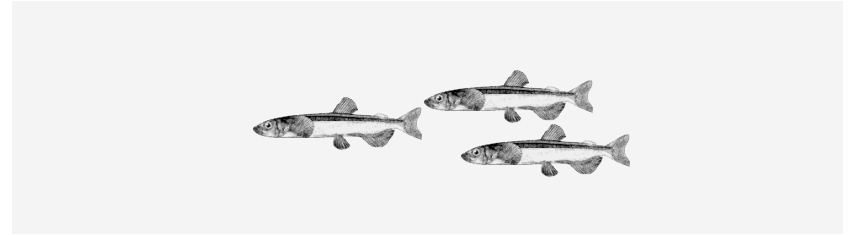
Size-dependent mortality and food-dependent growth effects



Increased mortality on small juveniles increases their and adult density by an order of magnitude



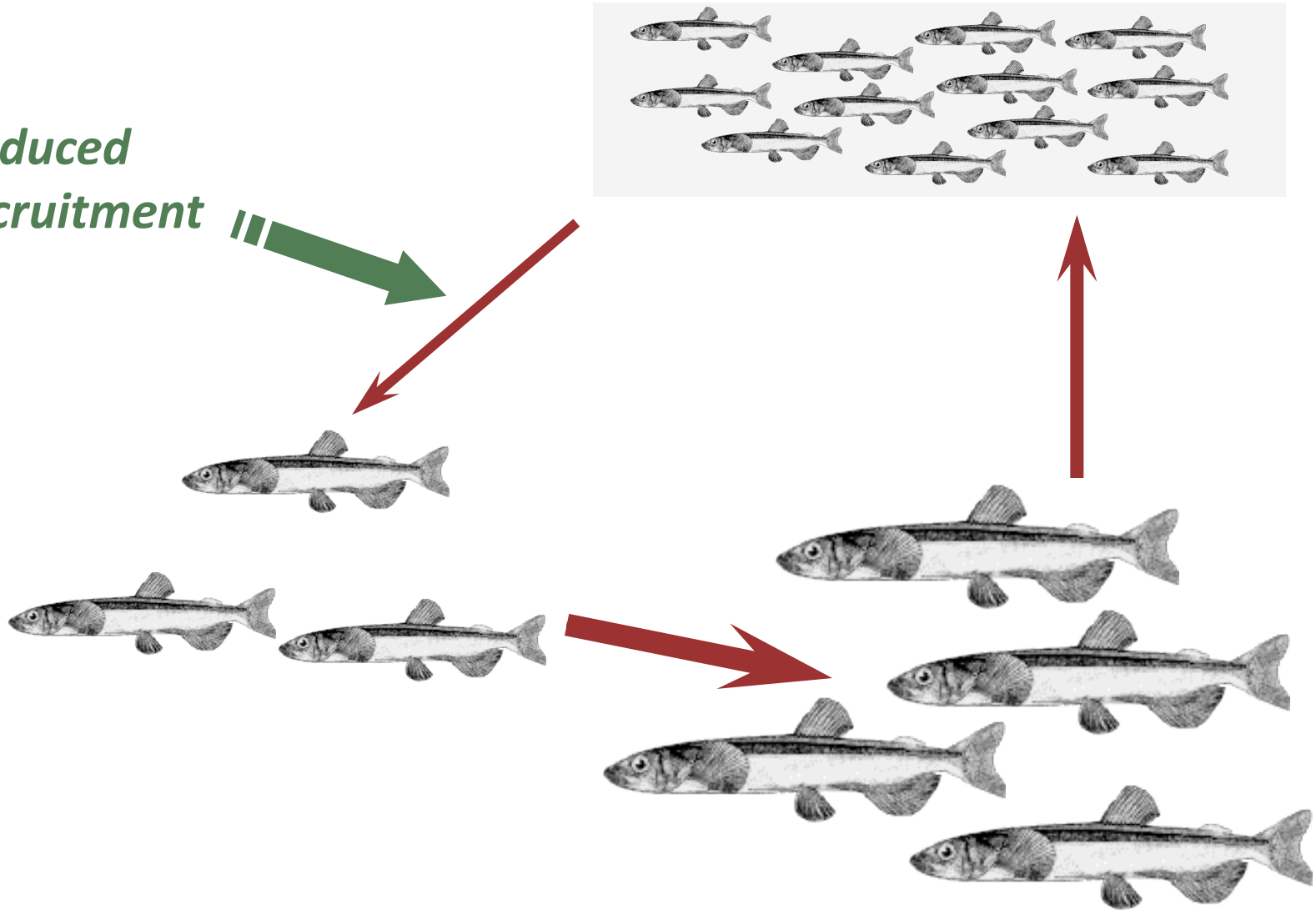
Competition leads to middle class dominance





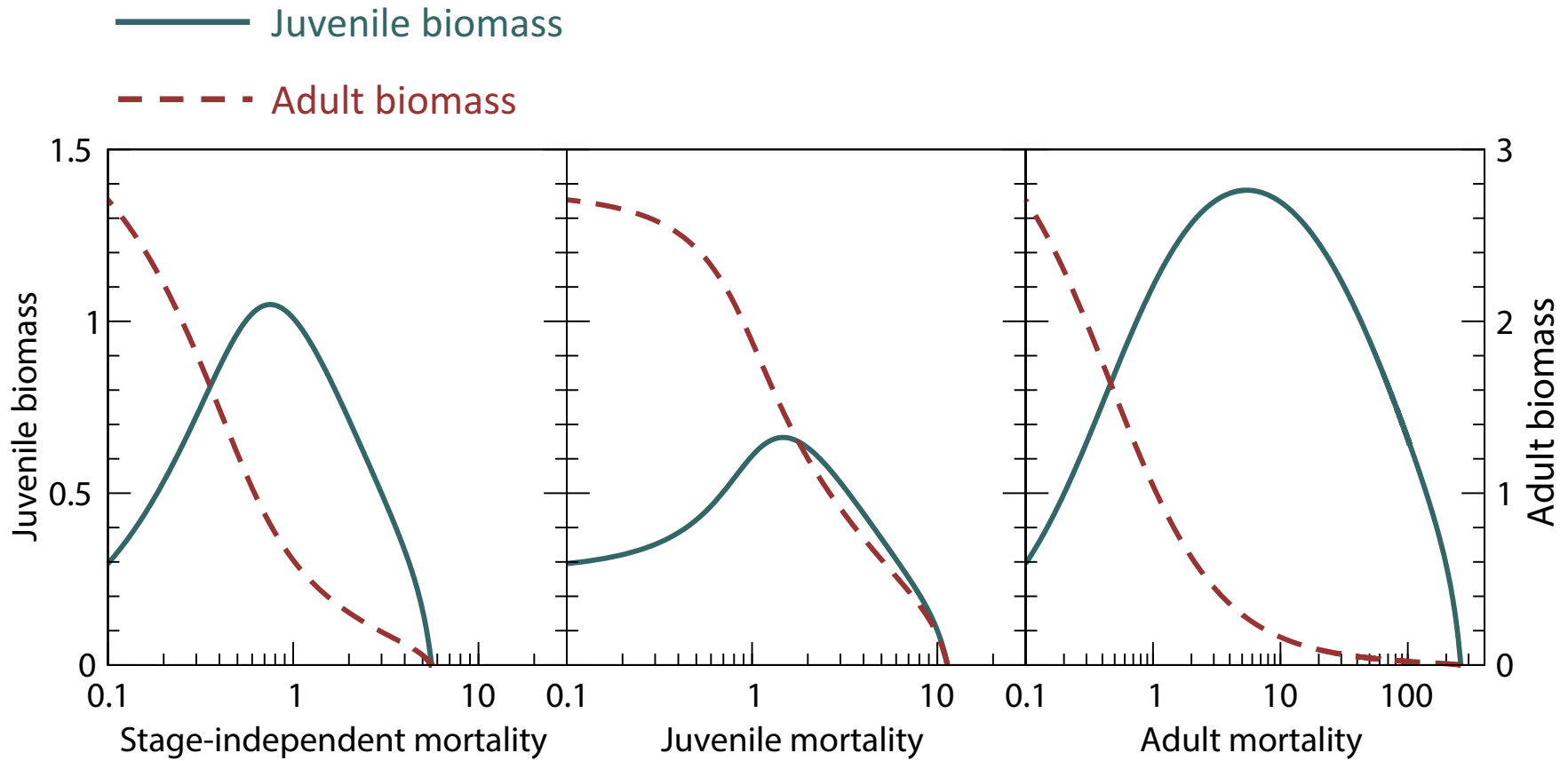
Competition leads to middle class dominance

Reduced recruitment





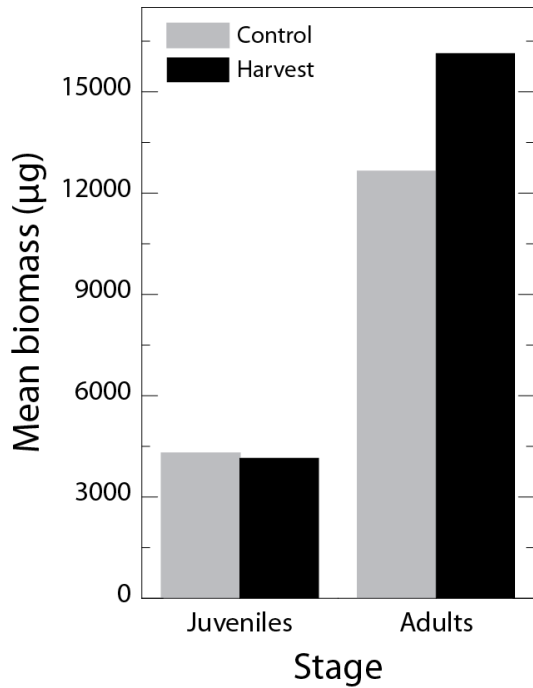
Equilibrium changes with increasing mortality



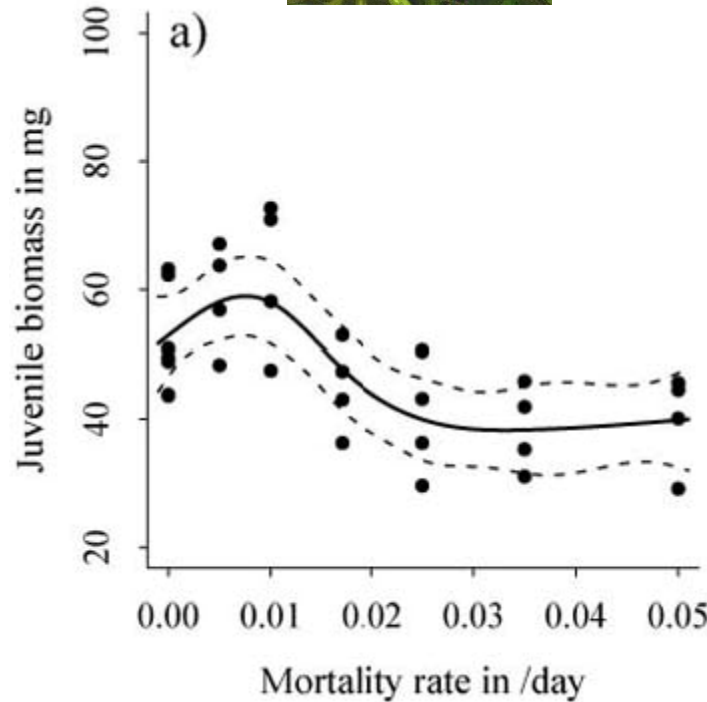
Reproduction control: $\nu_J(\tilde{R}) > \nu_A(\tilde{R}) > 0$



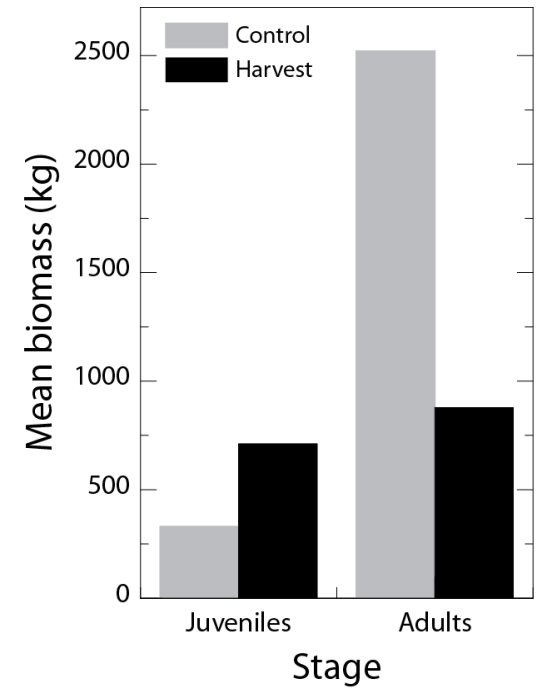
Similar overcompensation for all types of mortality



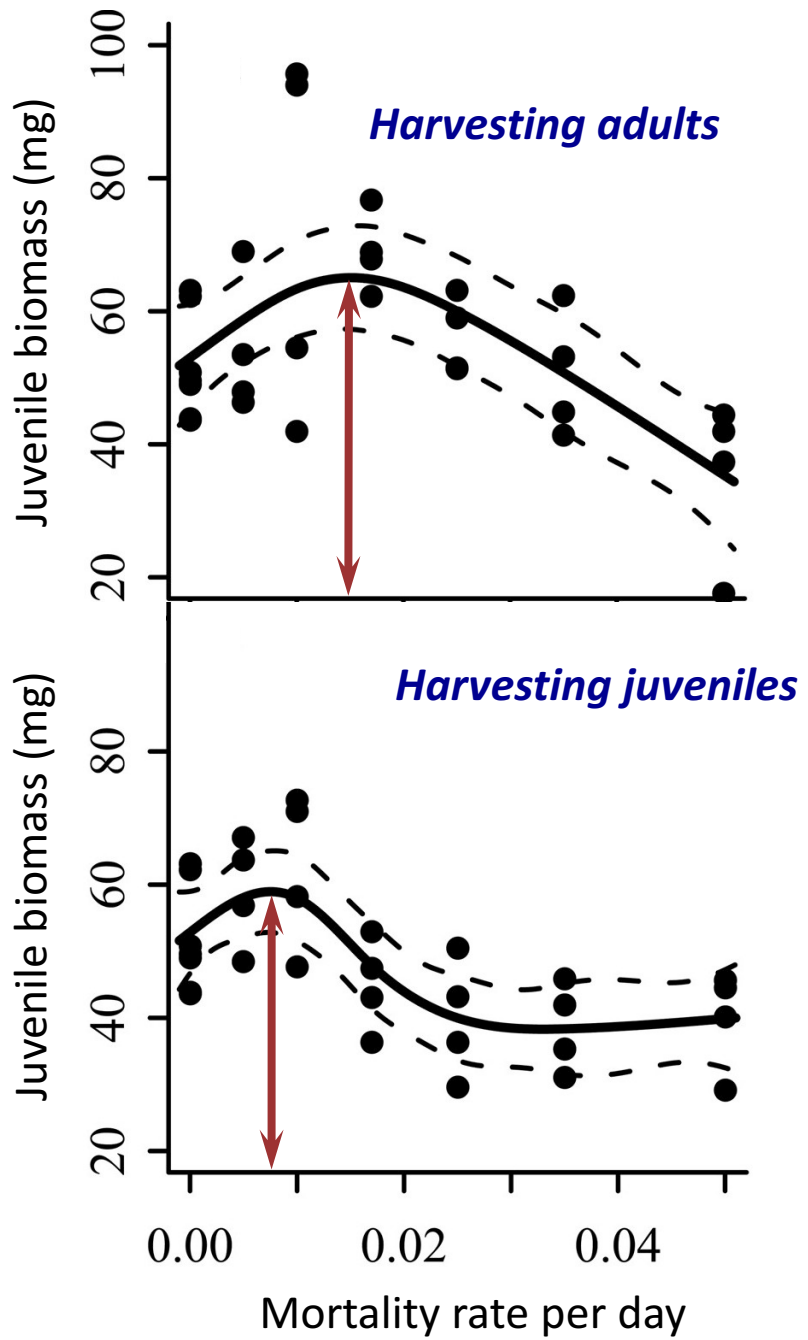
Egg mortality
Adults overcompensation
 Lab experiments



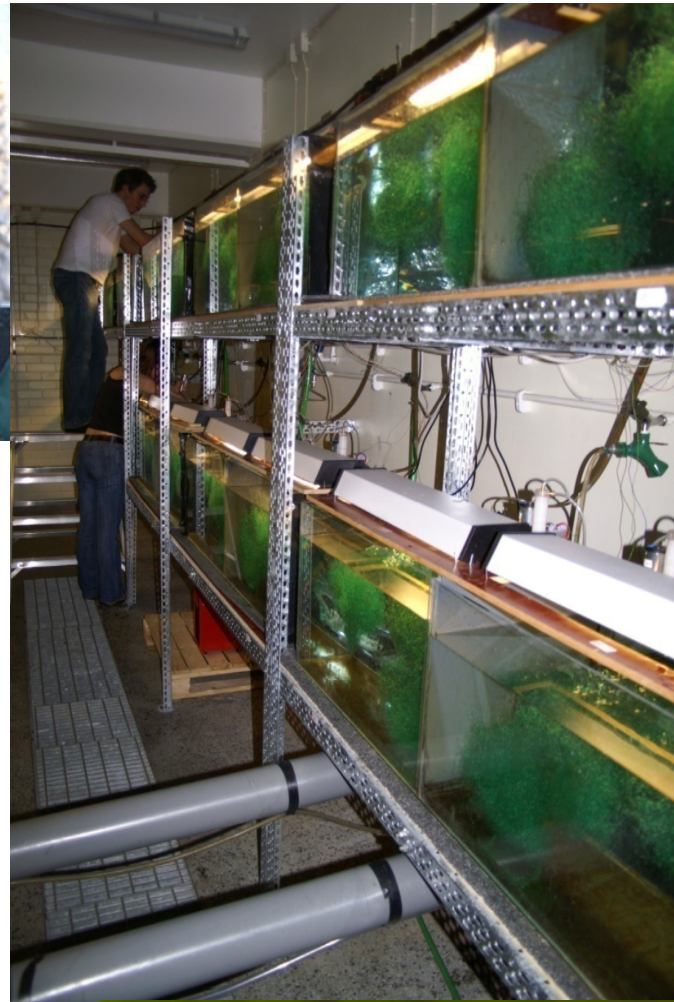
Juvenile mortality
Juvenile overcompensation
 Lab experiments



Adult mortality
Juvenile overcompensation
 Lake Windemere (UK)



**Lennart
Persson**

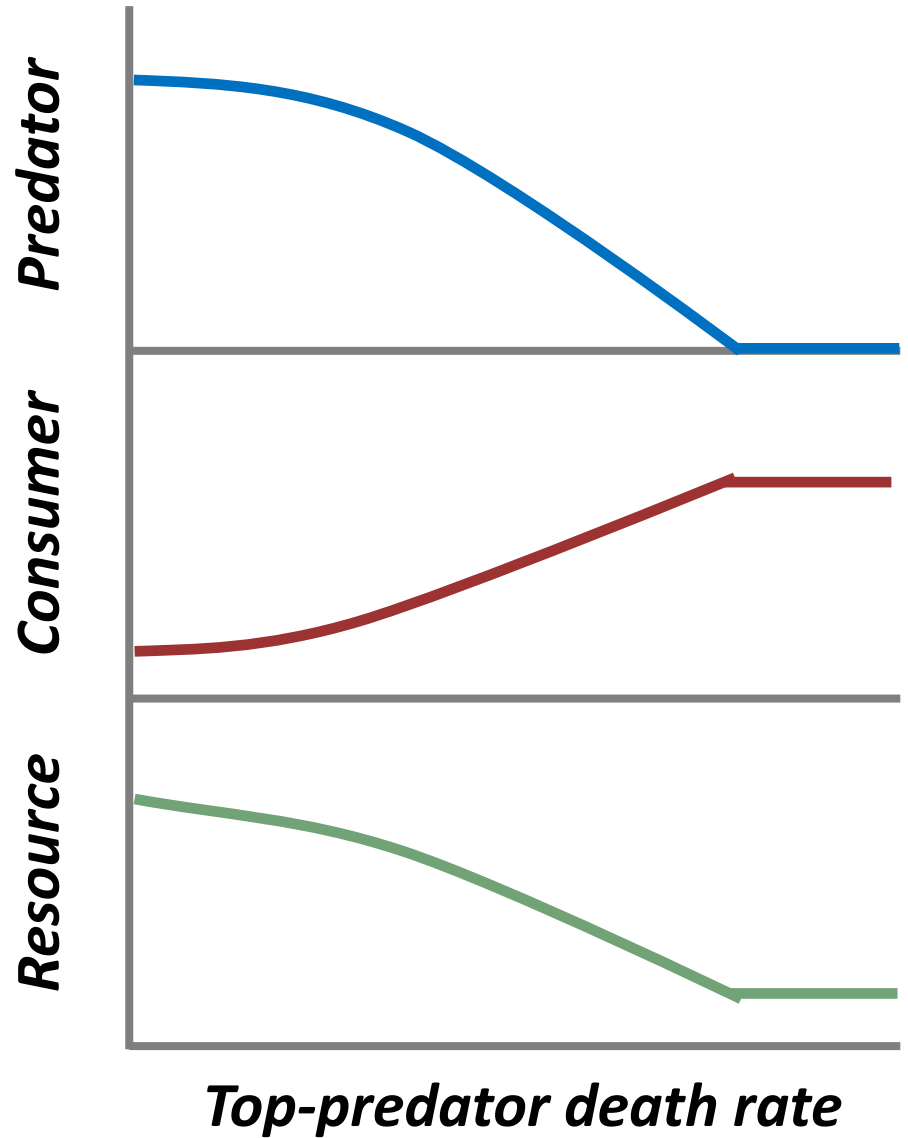
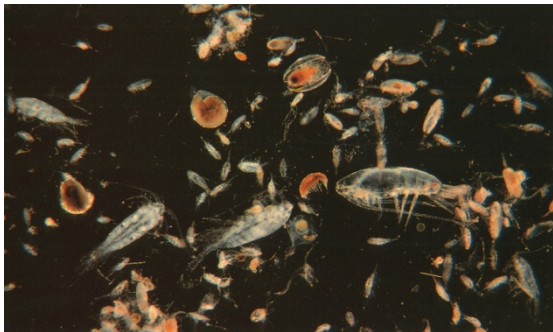




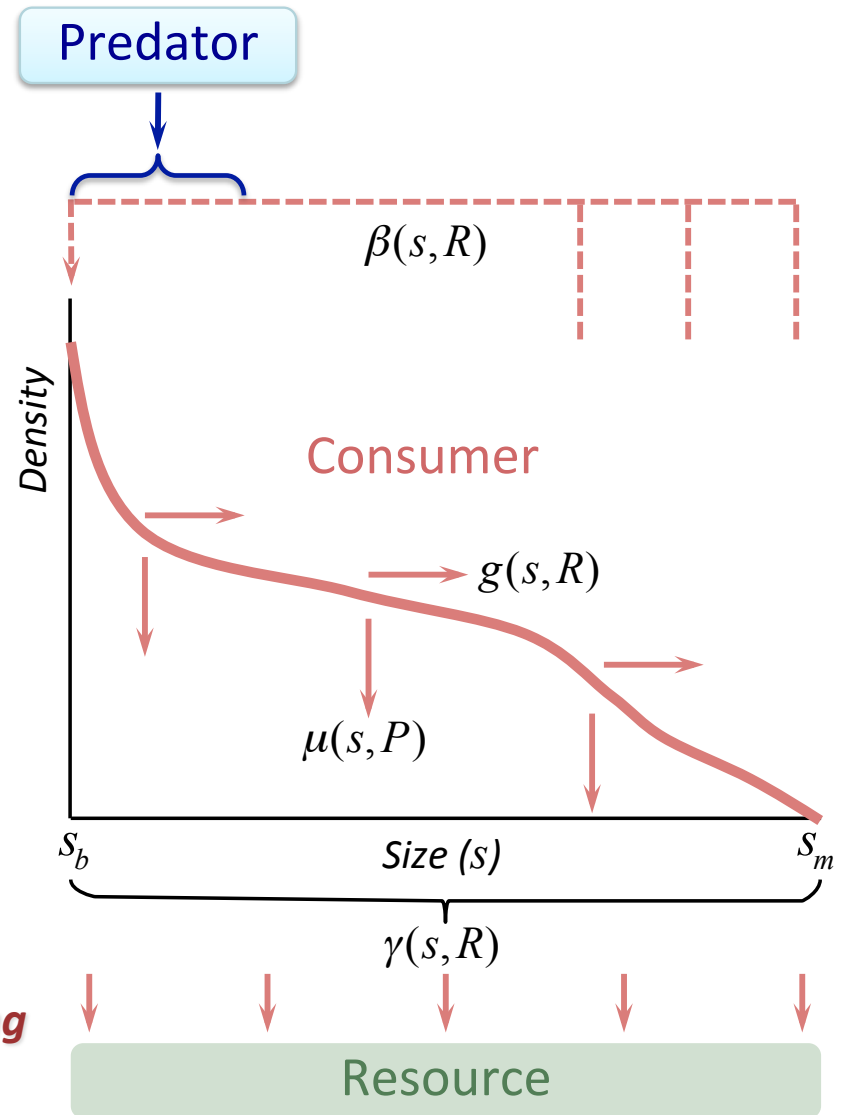
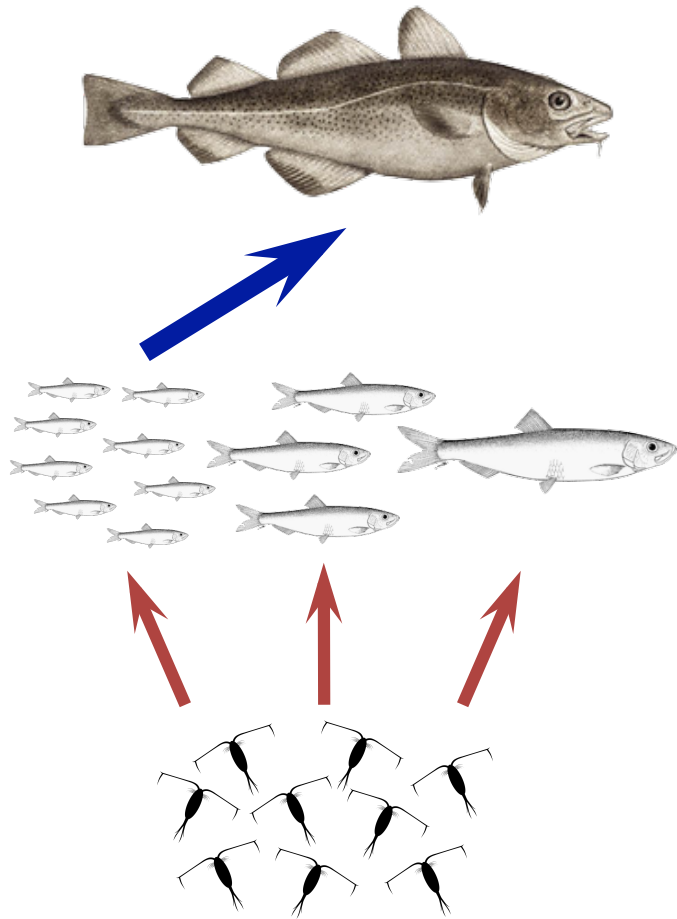
COMMUNITY CONSEQUENCES?



A fundamental ecological principle



Food chain model with size-selective predators



- *Ingestion scales allometrically with size*
- *Adults continue growing, while reproducing*
- *Food-dependent growth and reproduction*
- *Maturation when reaching size threshold*



Food chain with size-selective predation

Resource turnover:

$$\rho(R_{\max} - R)$$

Consumer foraging:

$$\gamma(s, R) = I_m \frac{R}{R_h + R} s^2$$

Consumer growth rate in size:

$$g(s, R) = v \left(s_m \frac{R}{R_h + R} - s \right)$$

Consumer fecundity:

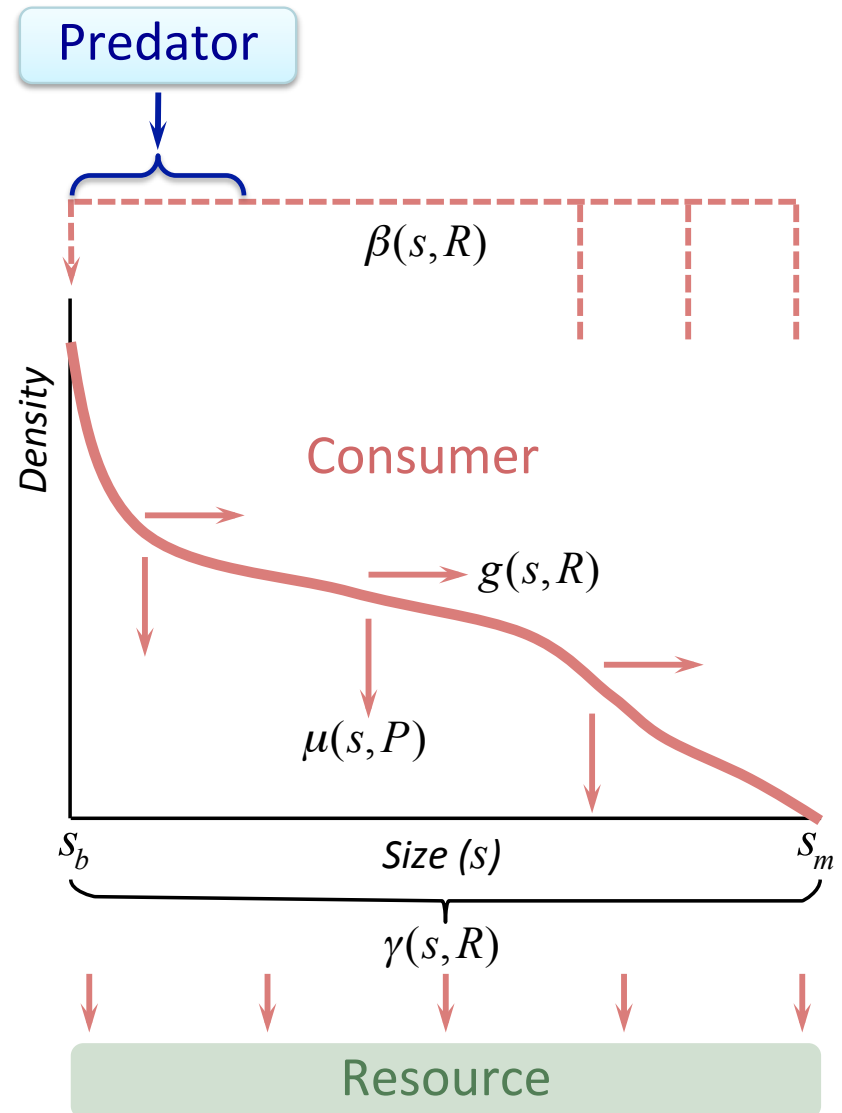
$$\beta(s, R) = r_m \frac{R}{R_h + R} s^2 \quad \text{if } s > s_j$$

Consumer mortality:

$$\mu(s, P) = \begin{cases} \mu_B + \frac{aP}{1 + aT_h B} & \text{if } s < s_v \\ \mu_B & \text{otherwise} \end{cases}$$

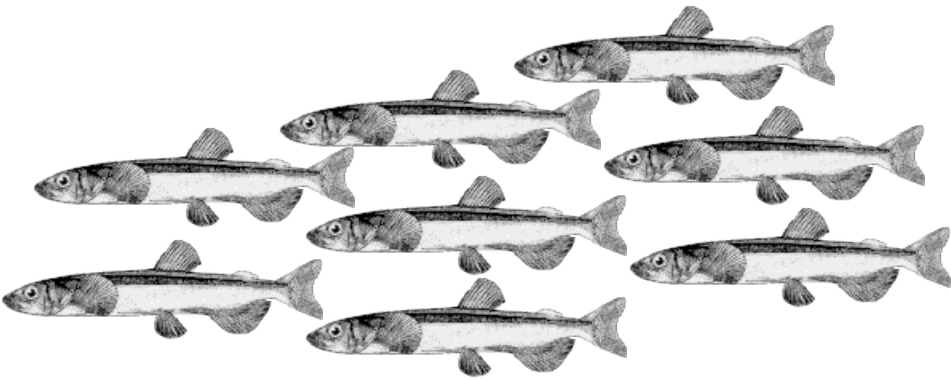
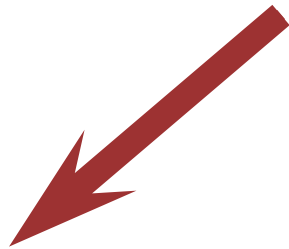
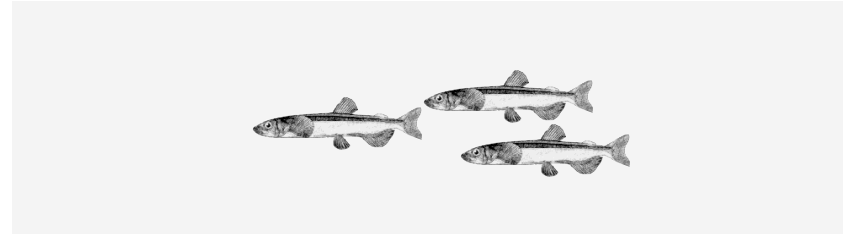
Predator per capita growth rate:

$$\frac{aB}{1 + aT_h B} - \delta$$



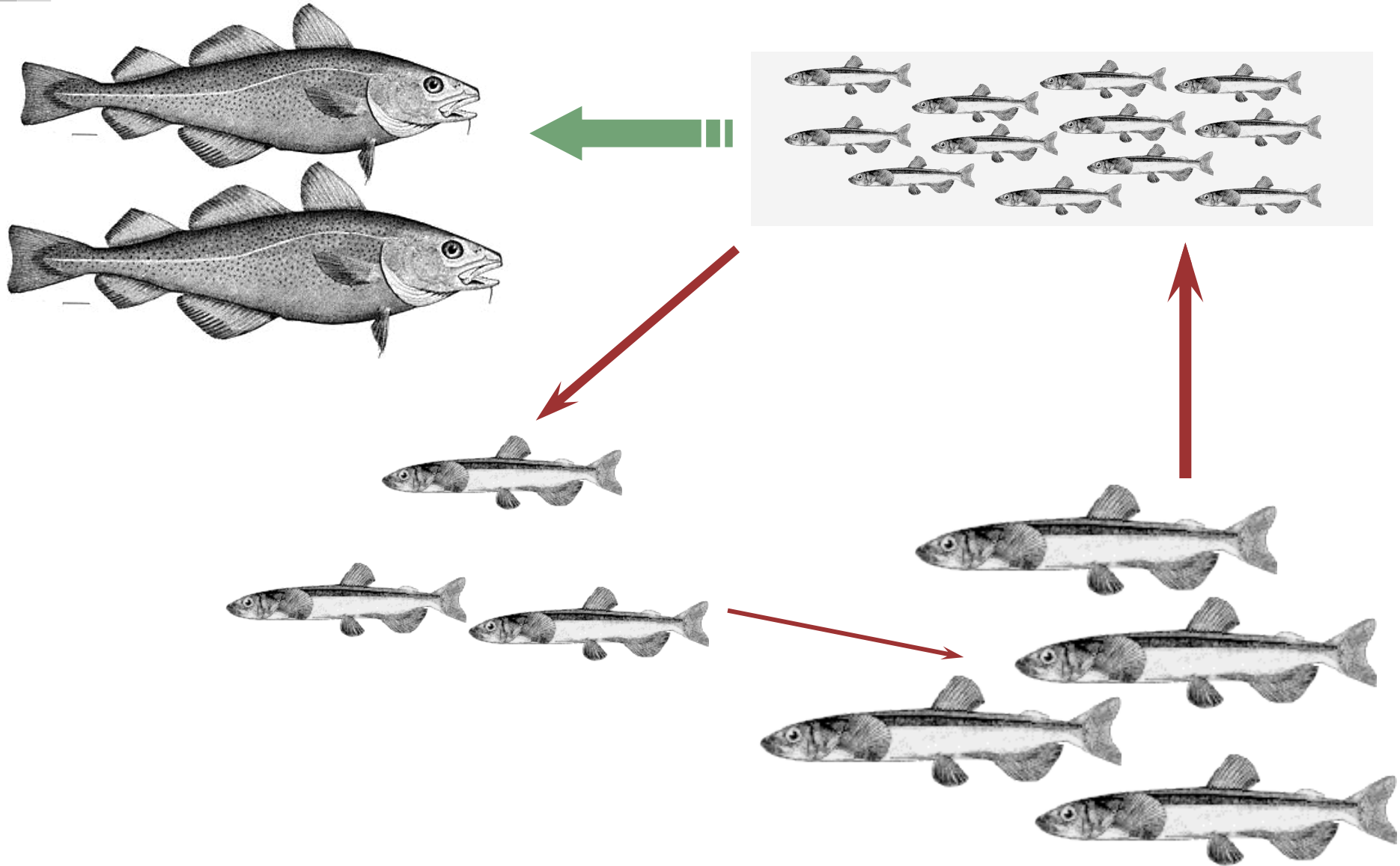


Predators absent



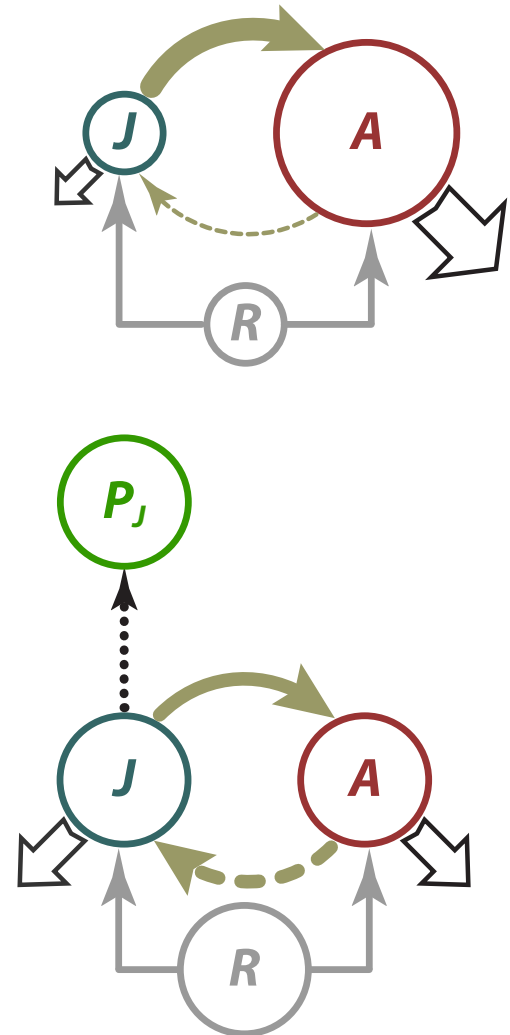
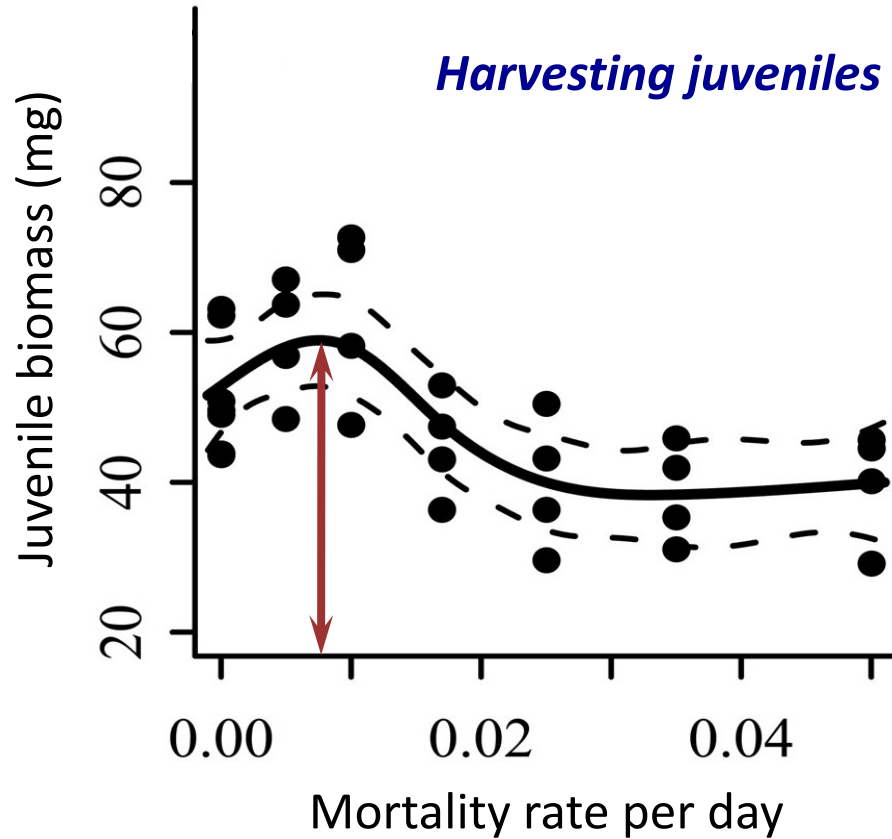


Predators present





Emergent Allee effect

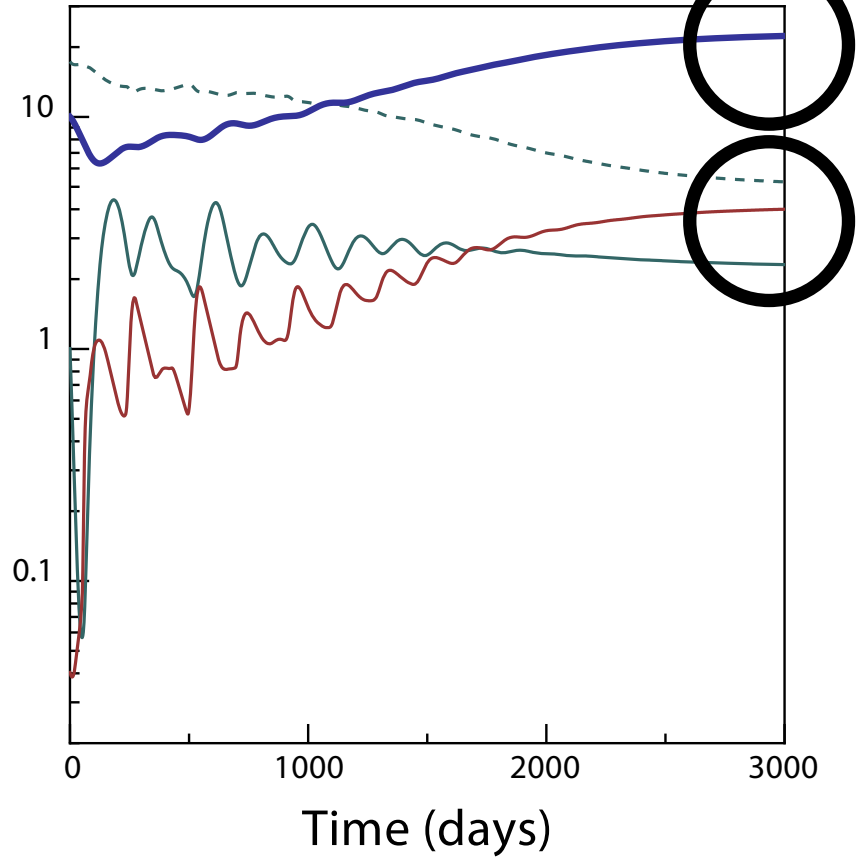
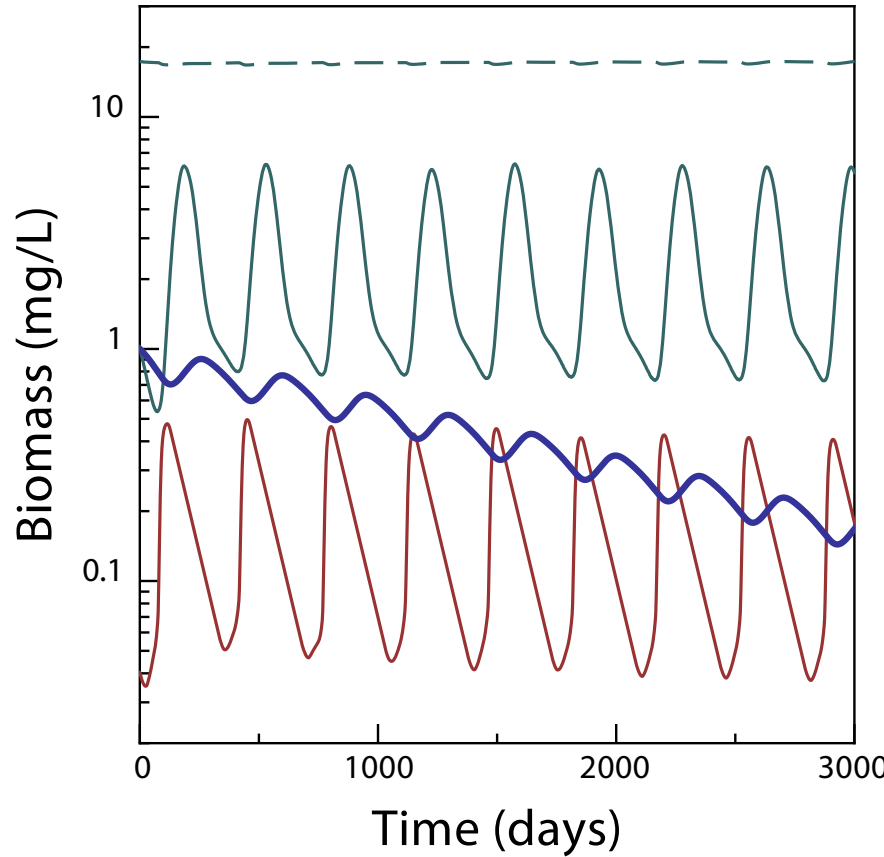


Positive feedback of abundance of predator on their own food availability (positive density dependence)



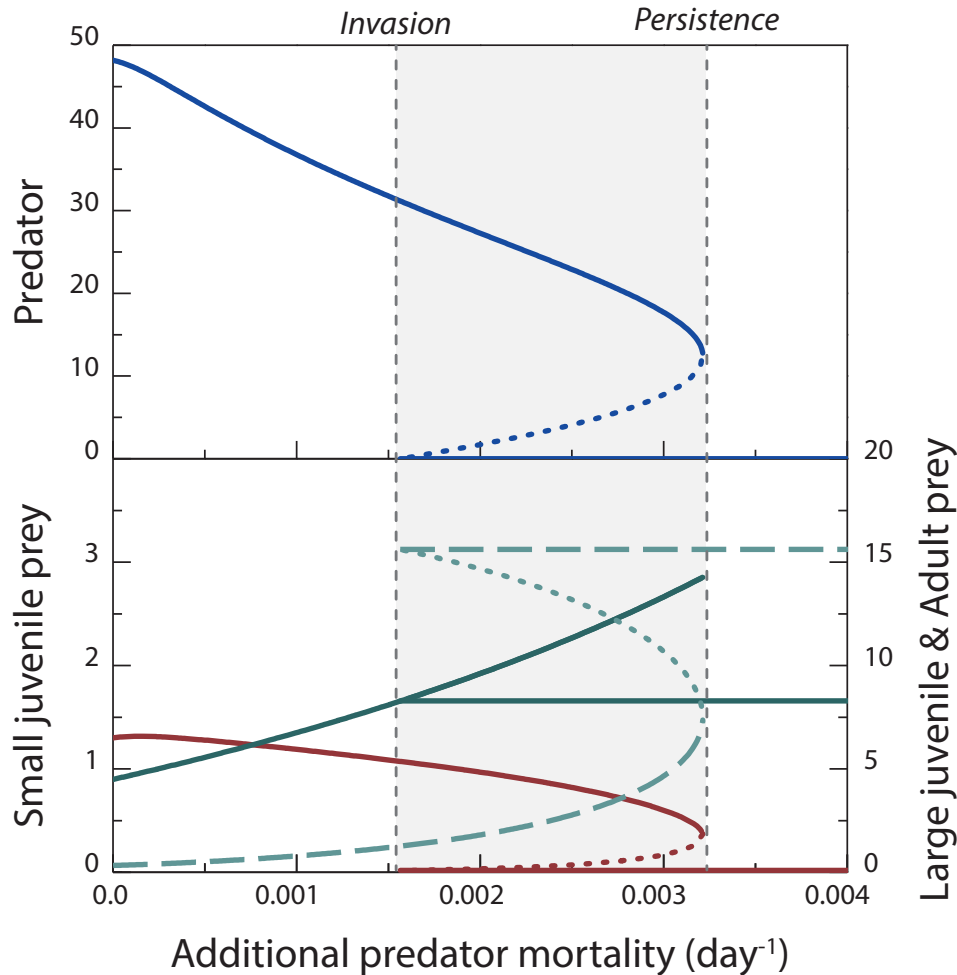
Emergent Allee effect

— Small juvenile prey - - - Large juvenile prey — Adult prey — Predators



- *At low density predators will fail to increase in abundance and go extinct*
- *At higher densities predation is sufficient to change the prey size distribution, leading to **predator recovery***

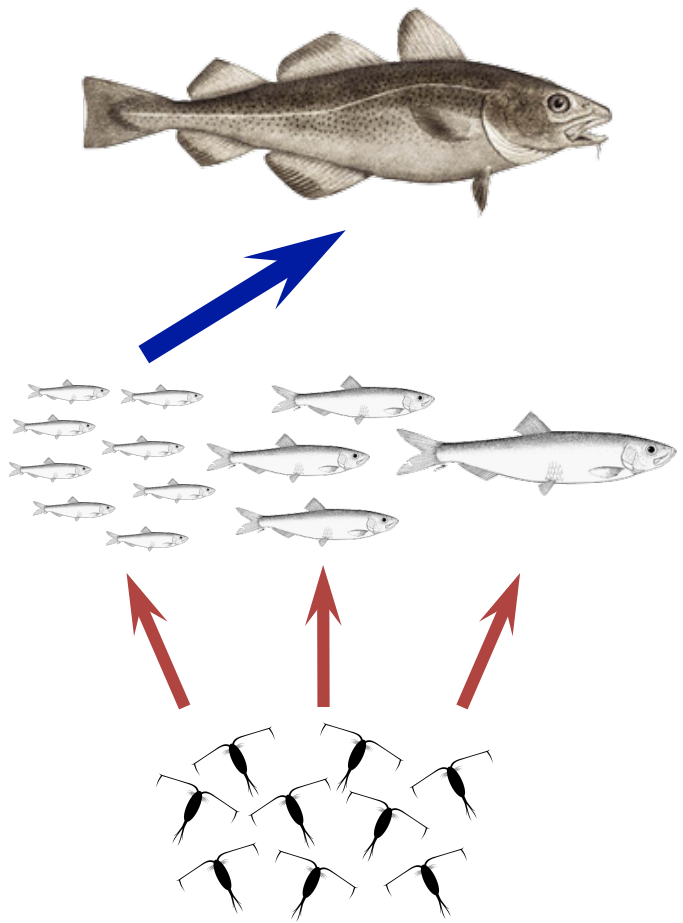
Bistability due to an Emergent Allee effect



- Multiple stable community states (*with/without predators*), if
- Predators forage on **small** prey only and the **prey** equilibrium is controlled through maturation (*reproduction bottleneck*)
- Predators forage on **large** prey only and the **prey** equilibrium is controlled through reproduction (*development bottleneck*)
- Potential for predator population collapse and lack of recovery

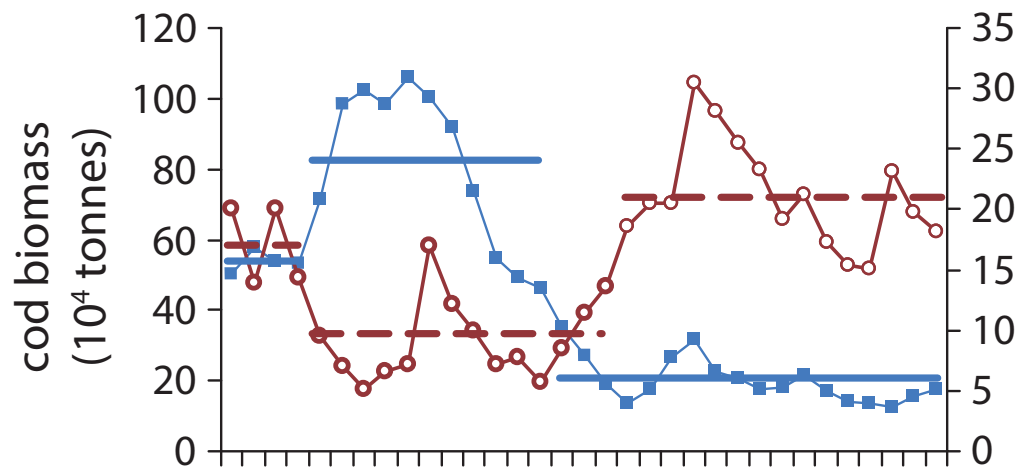
Predators shape their environment to the benefit of themselves and other guild members!

Food chain with size-selective predation

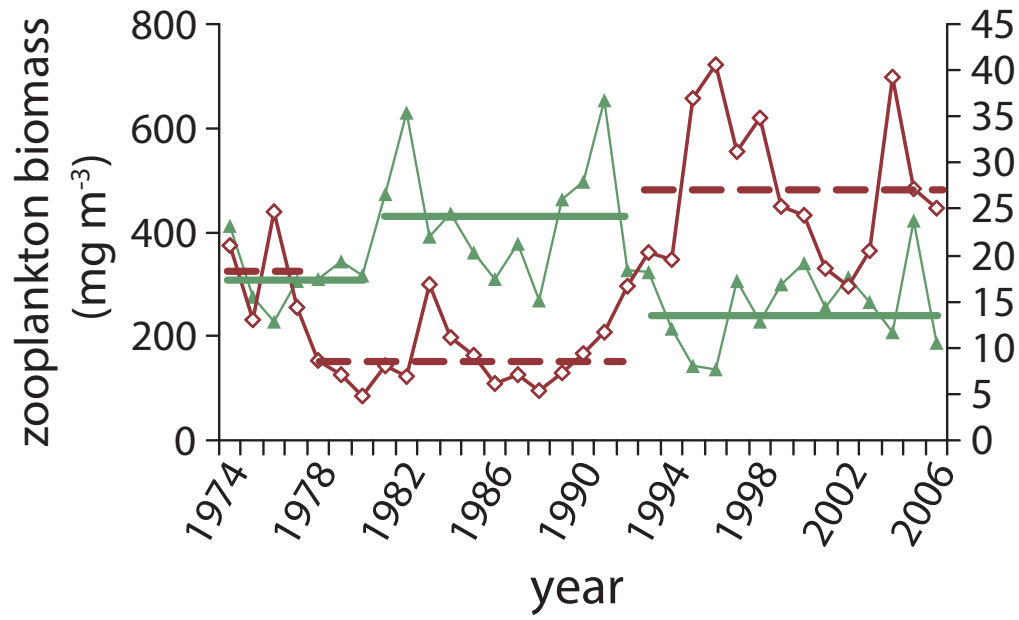
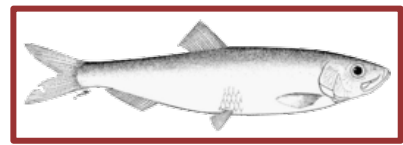




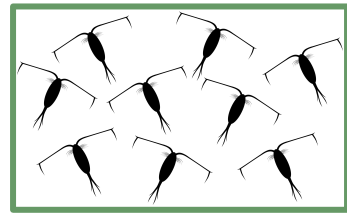
Baltic Sea cod: What slowed its recovery?



sprat biomass (10⁵ tonnes)

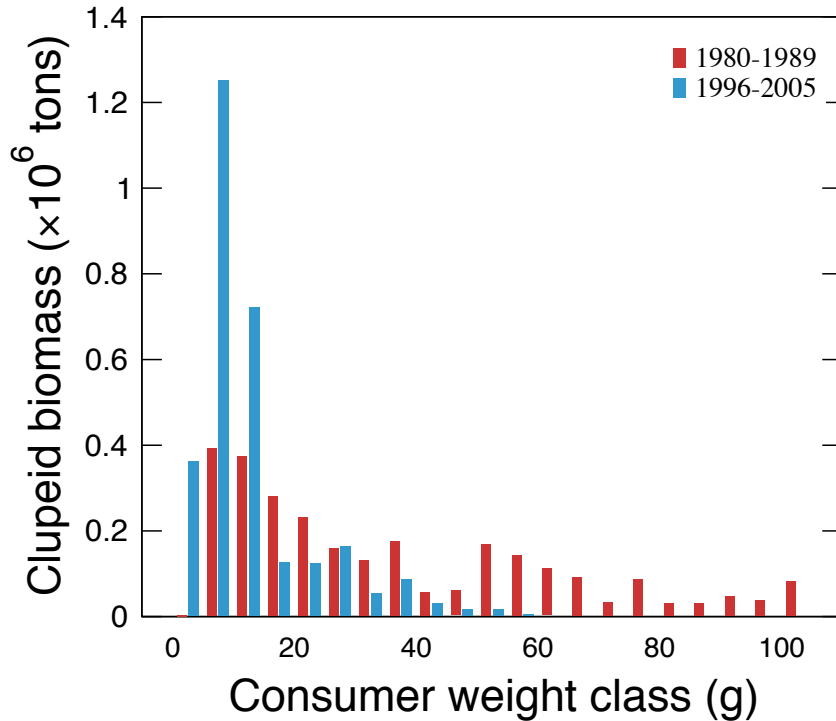


sprat abundance (10¹⁰ ind.)

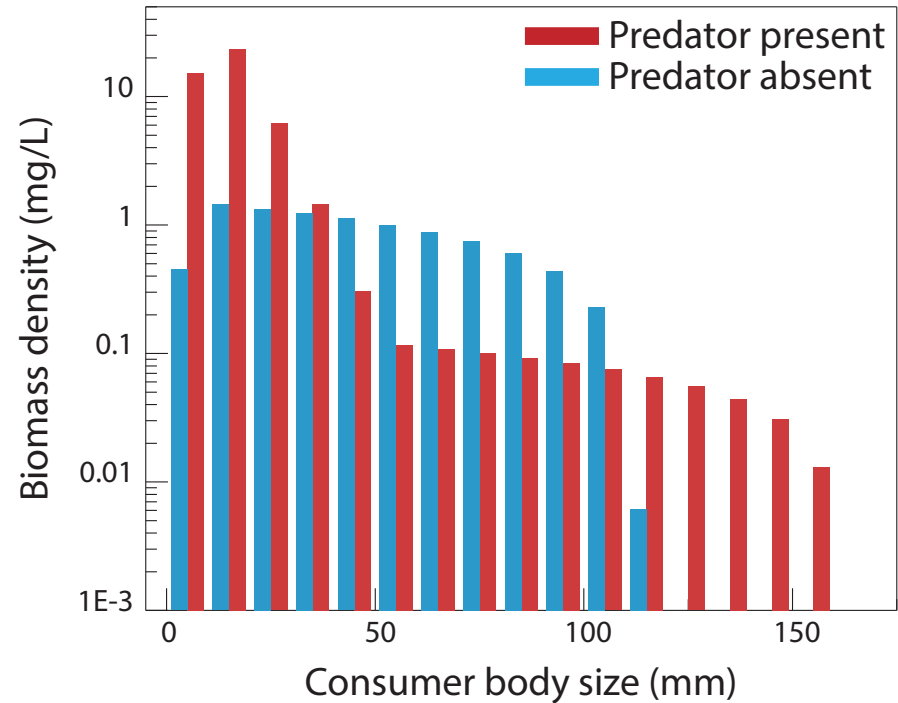




Changes in Baltic clupeid populations: Changes in size distribution



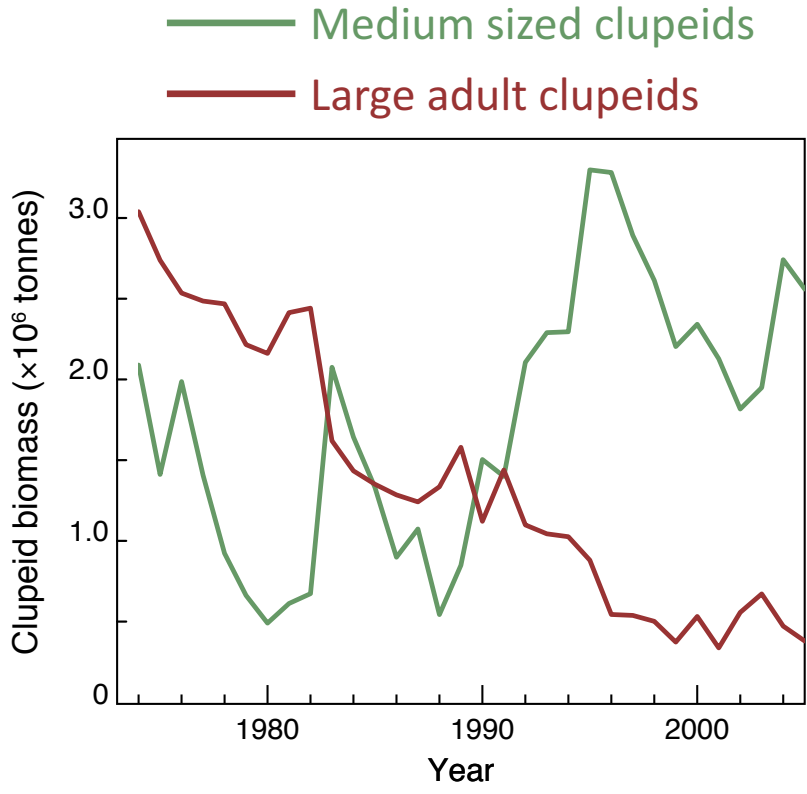
Observed size distribution



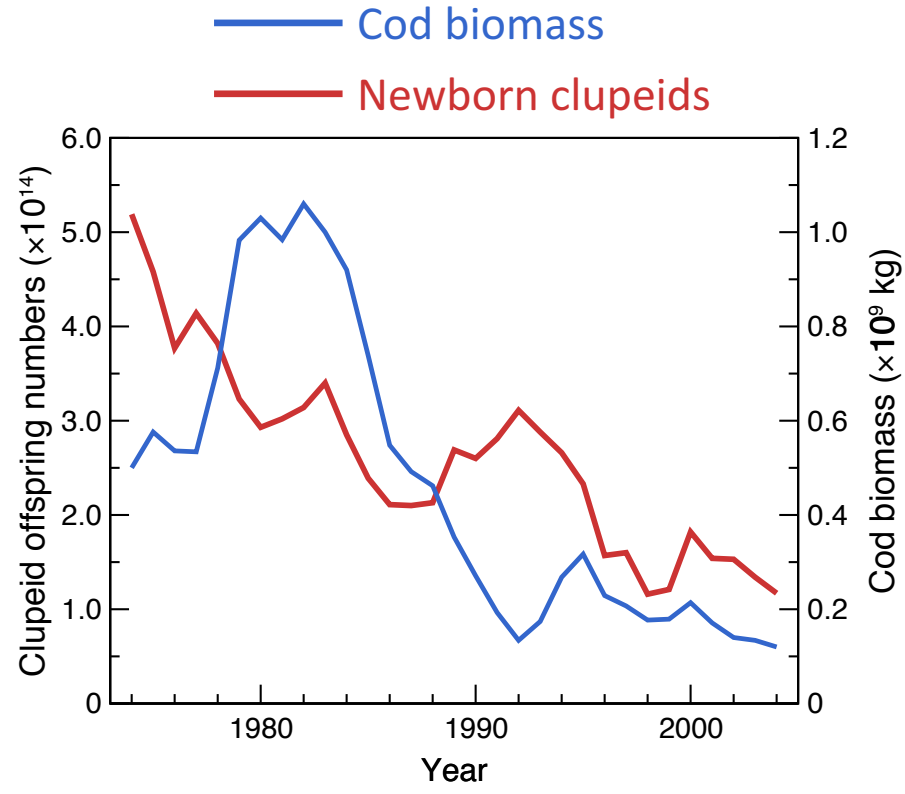
Model predictions



Changes in clupeids (i.e. Cod's food)



Clupeids got smaller



Clupeids produced fewer young

Changes conform with predictions at low clupeid harvesting



Is the cod doomed after collapsing?

No!!

Catch the clupeids!

Decreases the competition....

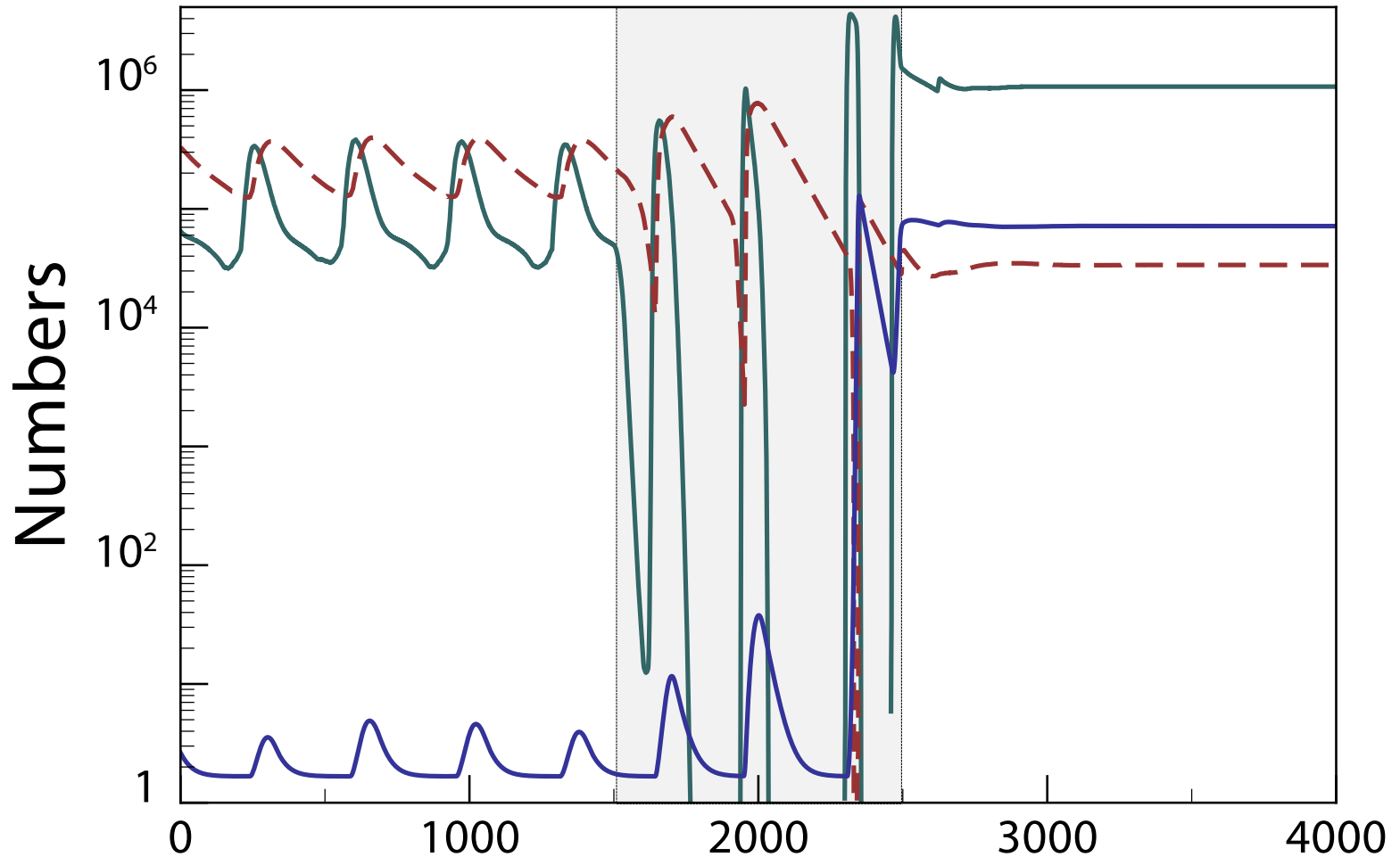
Changes its size distribution....

Provides more food for cod



Culling prey benefits predator recovery

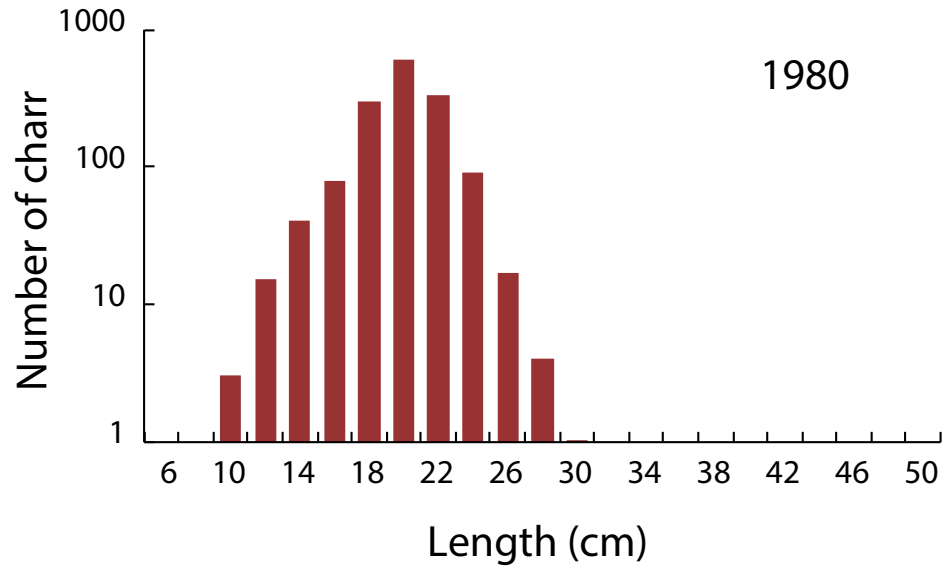
— Vulnerable juveniles - - - Invulnerable juveniles & Adults — Predators



Could this absurd idea possibly work in practice????



Arctic Charr in Lake Takvatn





Experimental thinning of Charr in Takvatn

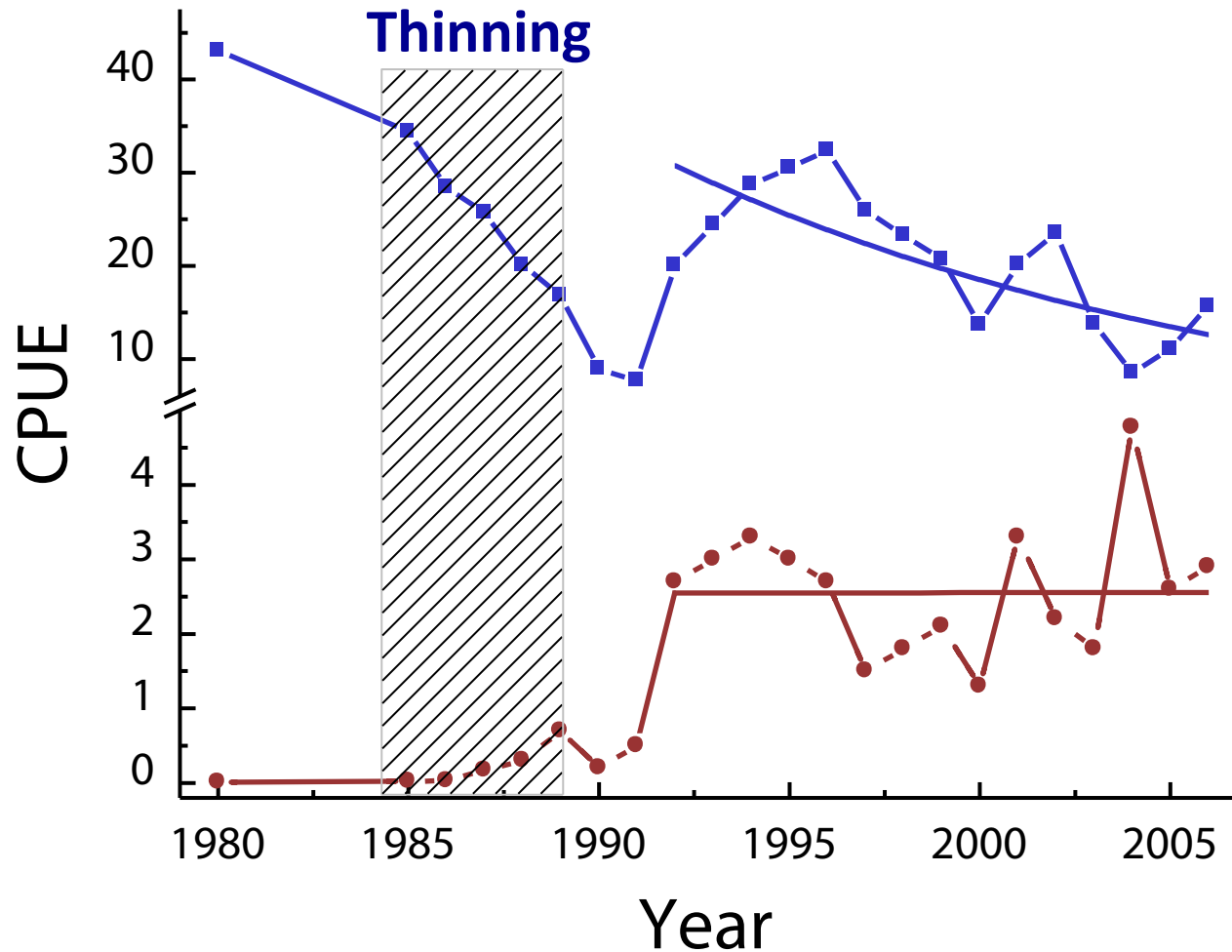


From 1984 to 1989, a total of 666 000 charr (31.3 metric tons) were removed by intensive fishing.....



Harvesting prey for a while

Leads to predator recovery



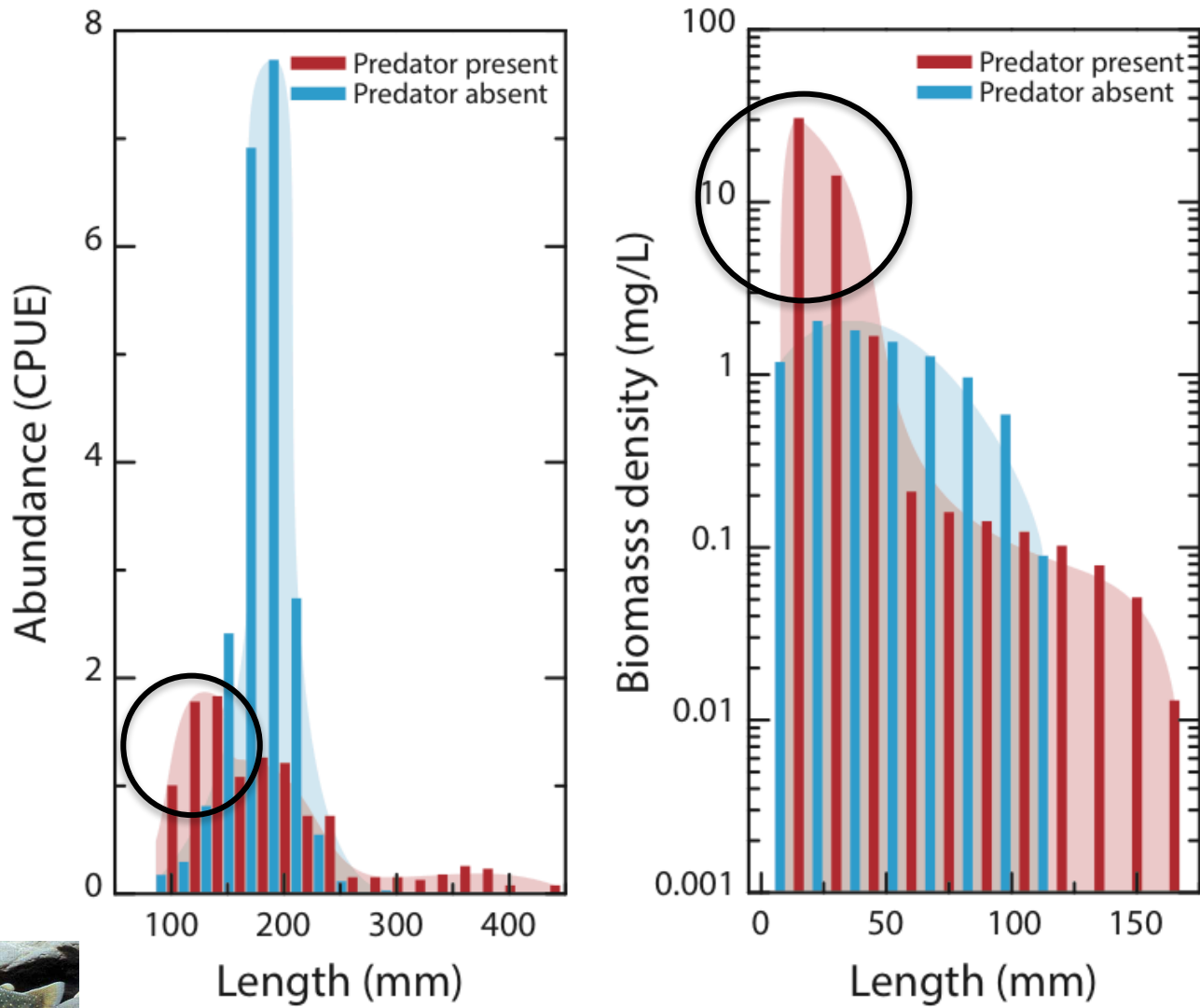
Arctic charr



Brown trout



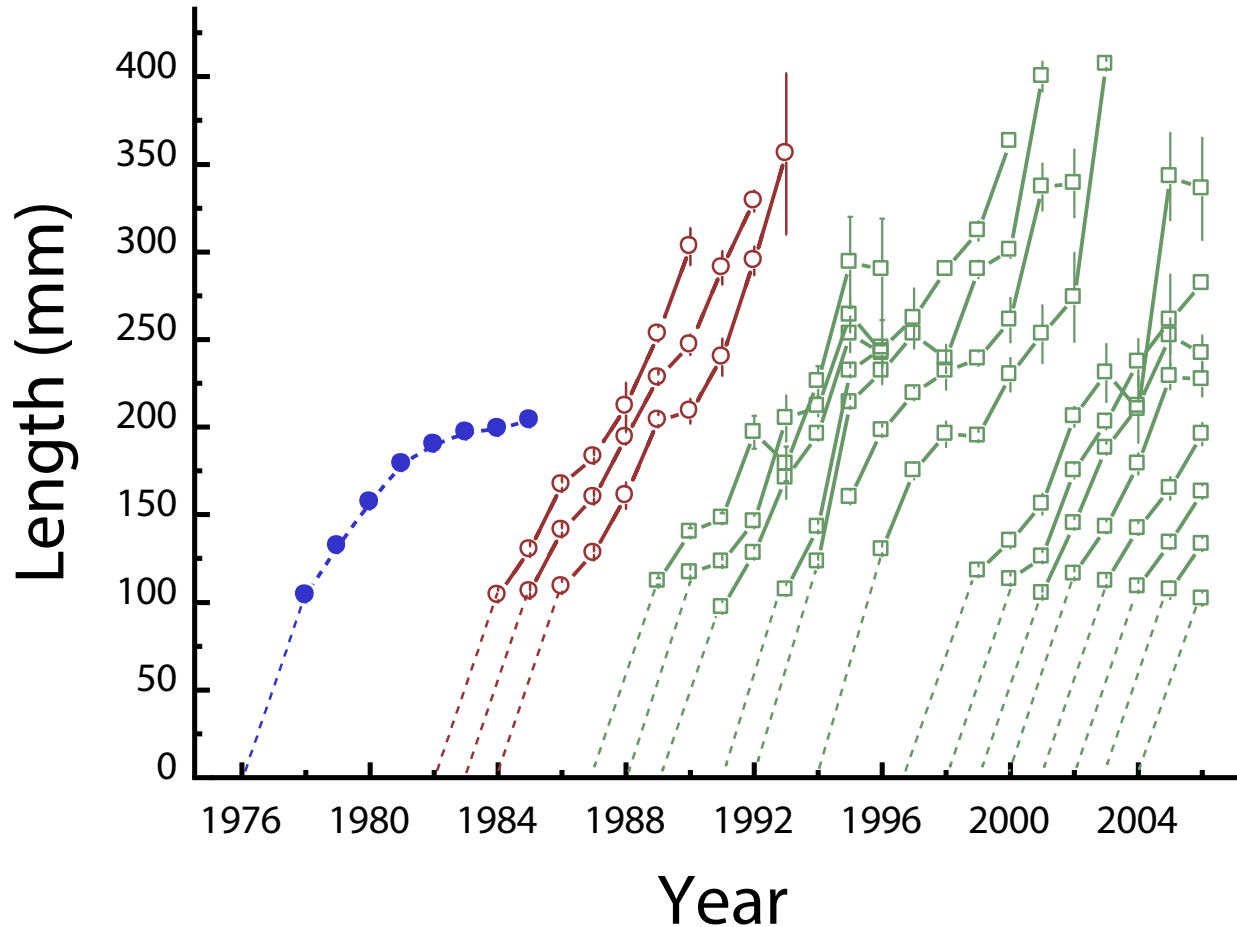
Emergent Allee effect: Takvatn Lake, Norway



Arctic char



Increases in Charr growth



Changed individual growth has remained up to today!

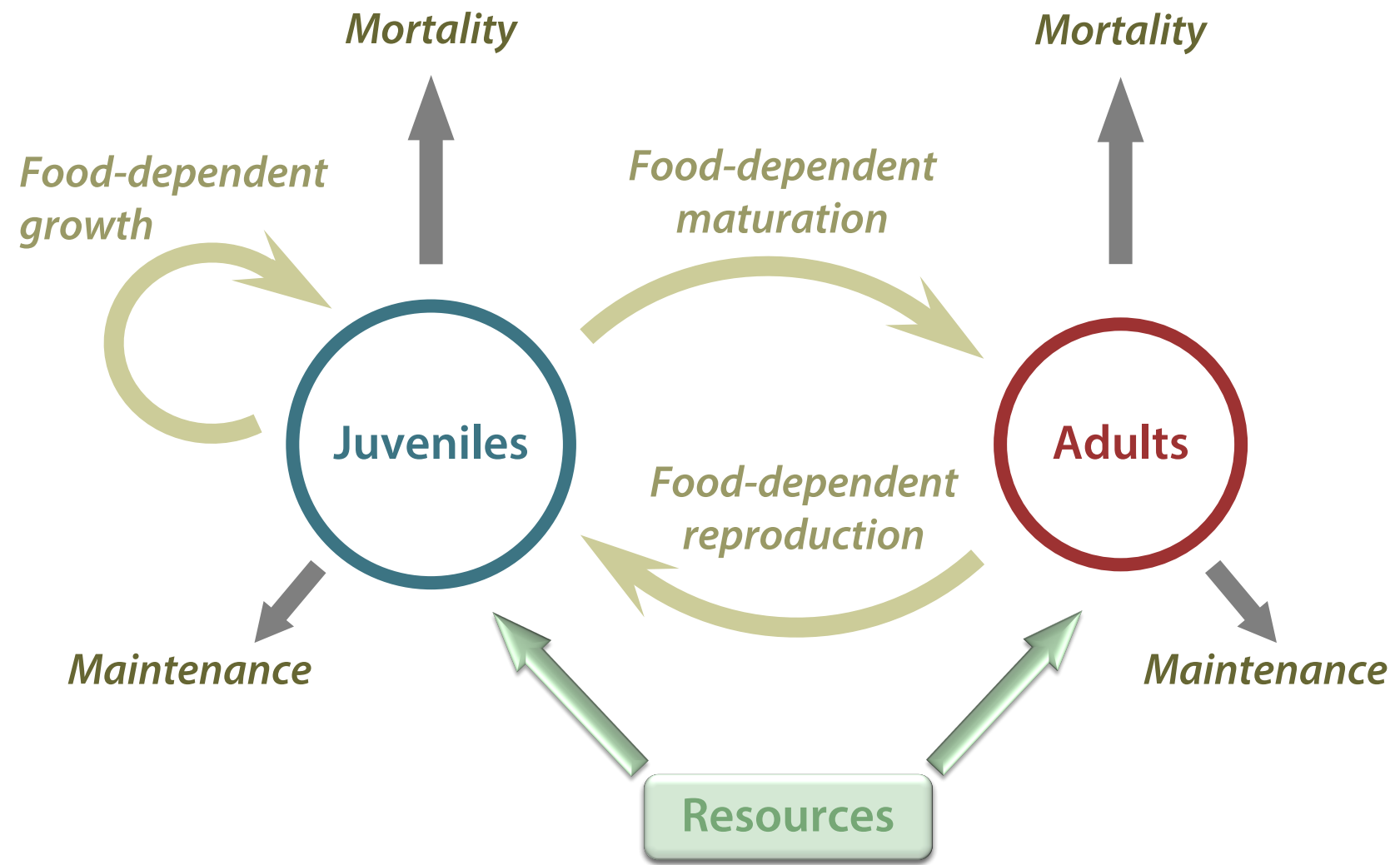
Ontogenetic asymmetry through niche shifts



- **Major mode of life in 80% of all animal species**
 - Metamorphosing species (insects, amphibians)
 - Species exhibiting substantial growth through life (fish)
- **Little diet overlap between stages of same species:**
 - < 8% for species with metamorphosis
 - ~ 40% for species with substantial growth through life

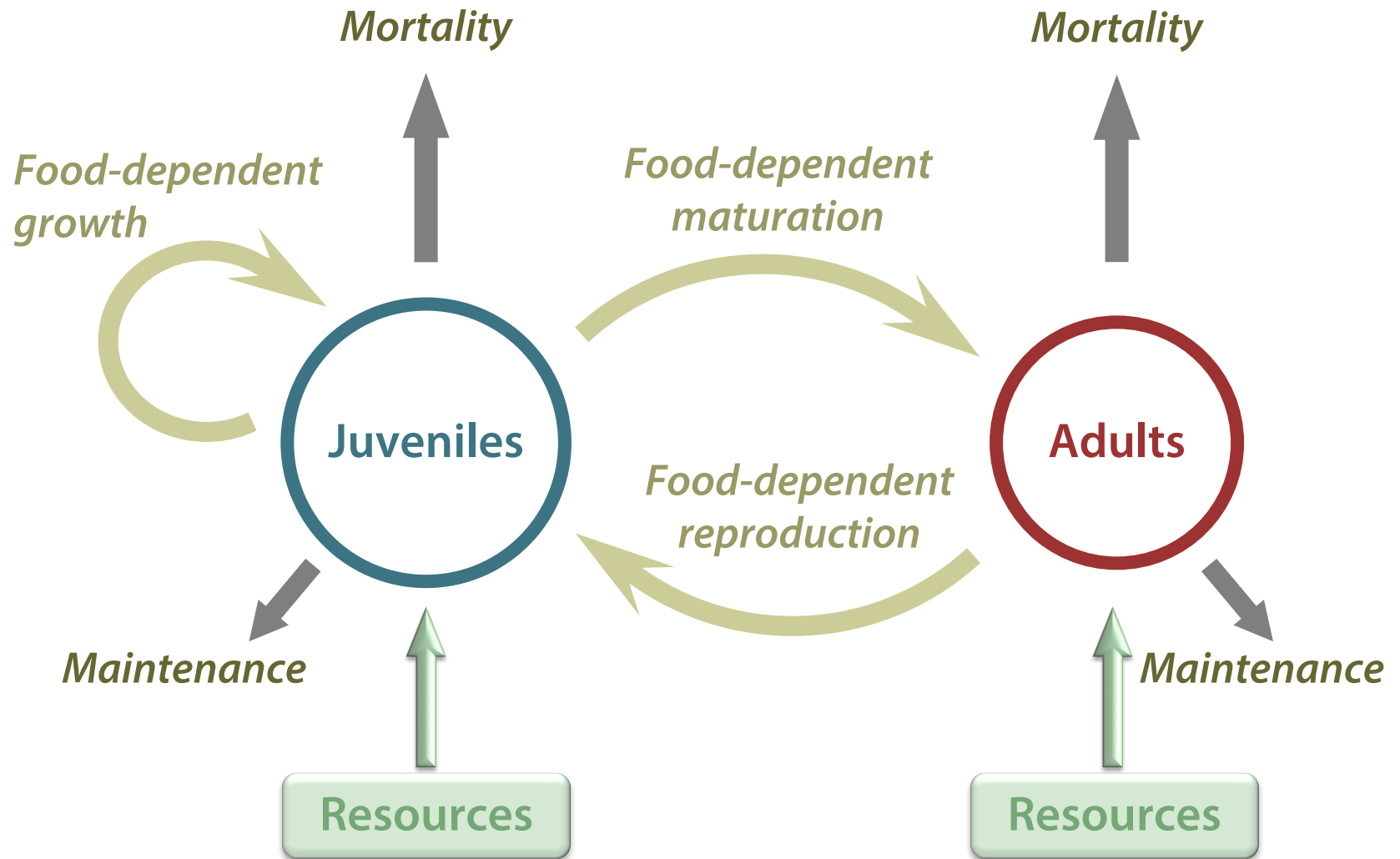


Ontogenetic asymmetry due to niche shifts



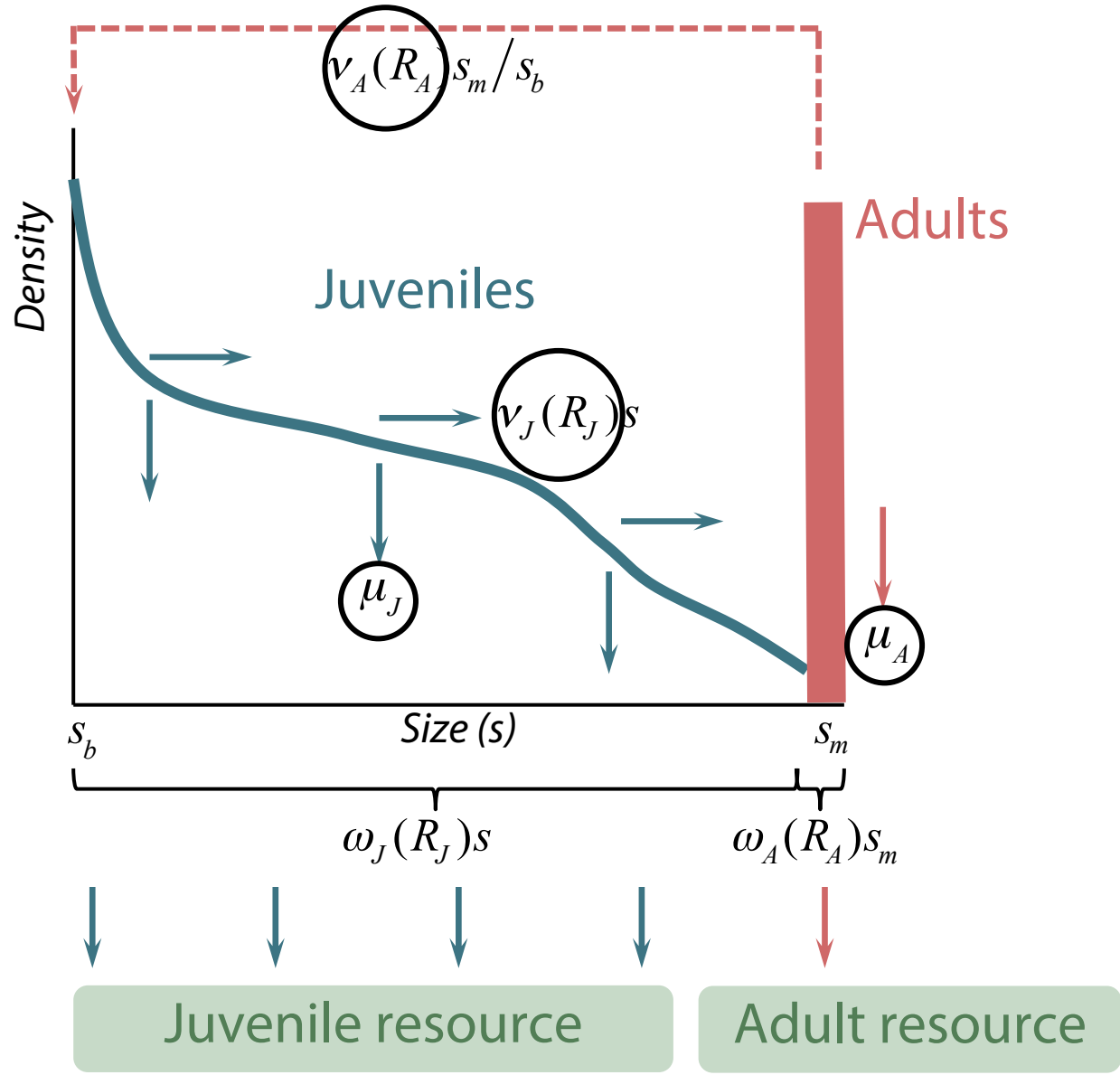


Ontogenetic asymmetry due to niche shifts





The size-structured population model





Size-structured population model equations

$$\frac{\partial c(t, s)}{\partial t} + \nu_J(R_J) \frac{\partial (sc(t, s))}{\partial s} = -\mu_J c(t, s) \quad \text{for } s_b \leq s < s_m$$

$$\nu_J(R_J) s_b c(t, s_b) = \frac{\nu_A(R_A) s_m}{s_b} C_A(t)$$

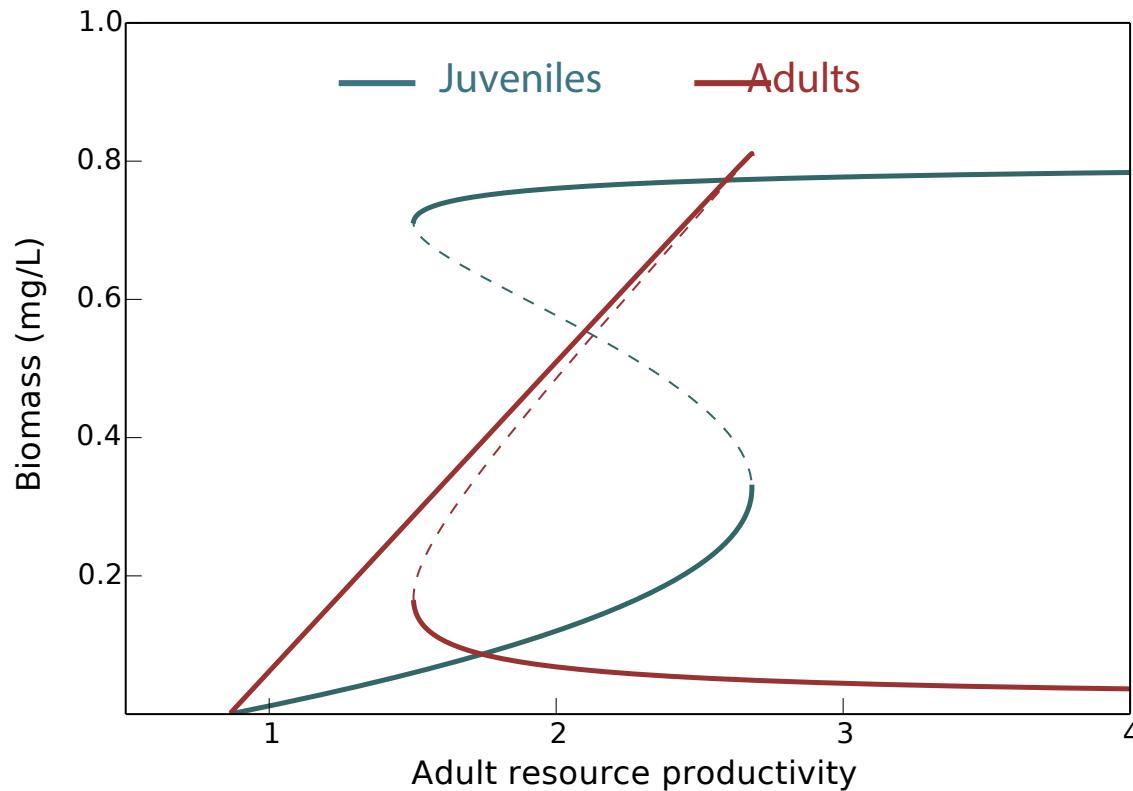
$$\frac{dC_A}{dt} = \nu_J(R_J) s_m c(t, s_m) - \mu_A C_A(t)$$

$$\frac{dR_J}{dt} = \rho(R_{J,max} - R_J) - \omega_J(R_J) \int_{s_b}^{s_m} sc(t, s) ds$$

$$\frac{dR_A}{dt} = \rho(R_{A,max} - R_A) - \omega_A(R_A) s_m C_A(t)$$



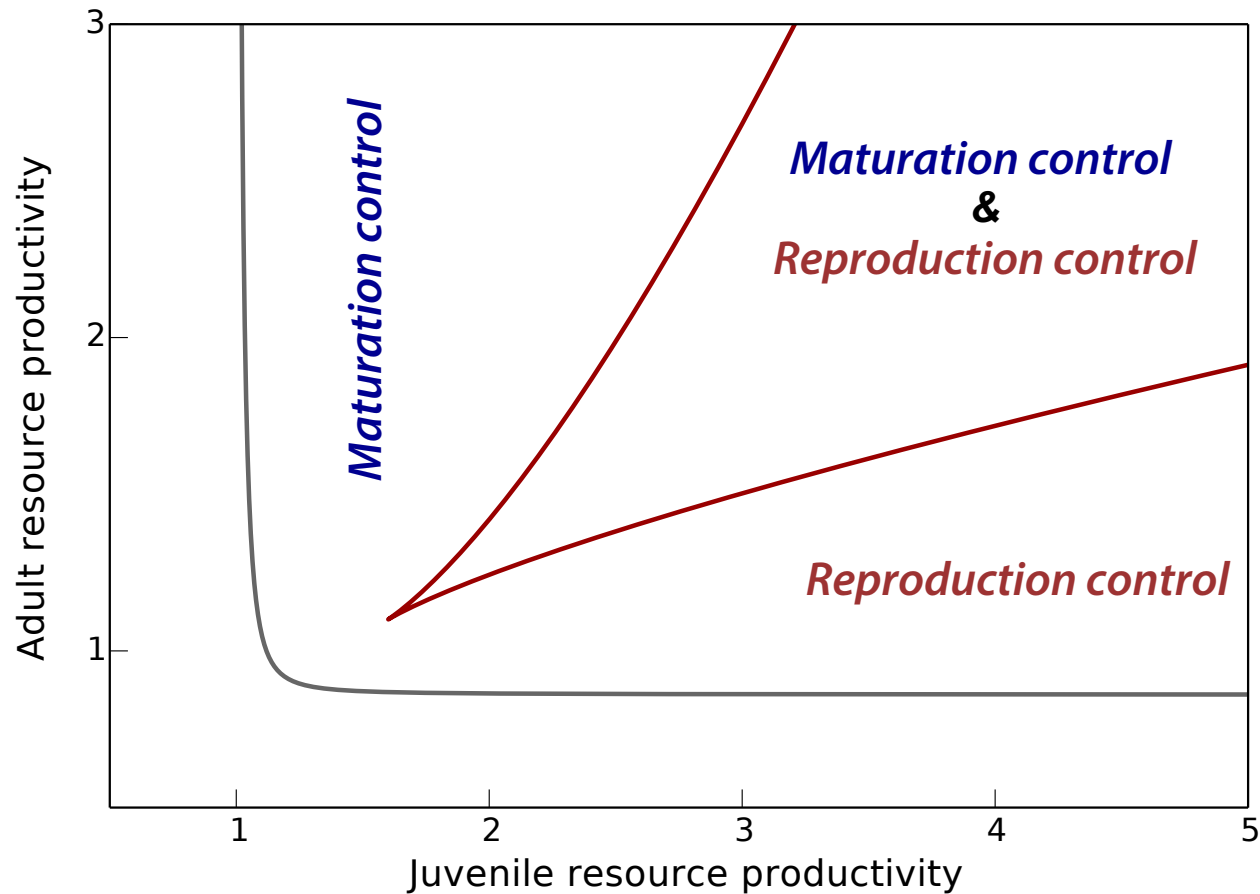
Maturation versus reproduction control



- At **low adult resource productivity** equilibrium is dominated by adult biomass controlled by **limited reproduction**
- At **high adult resource productivity** equilibrium is dominated by juvenile biomass controlled by **limited maturation**
- Both types of equilibria co-occur at intermediate productivity



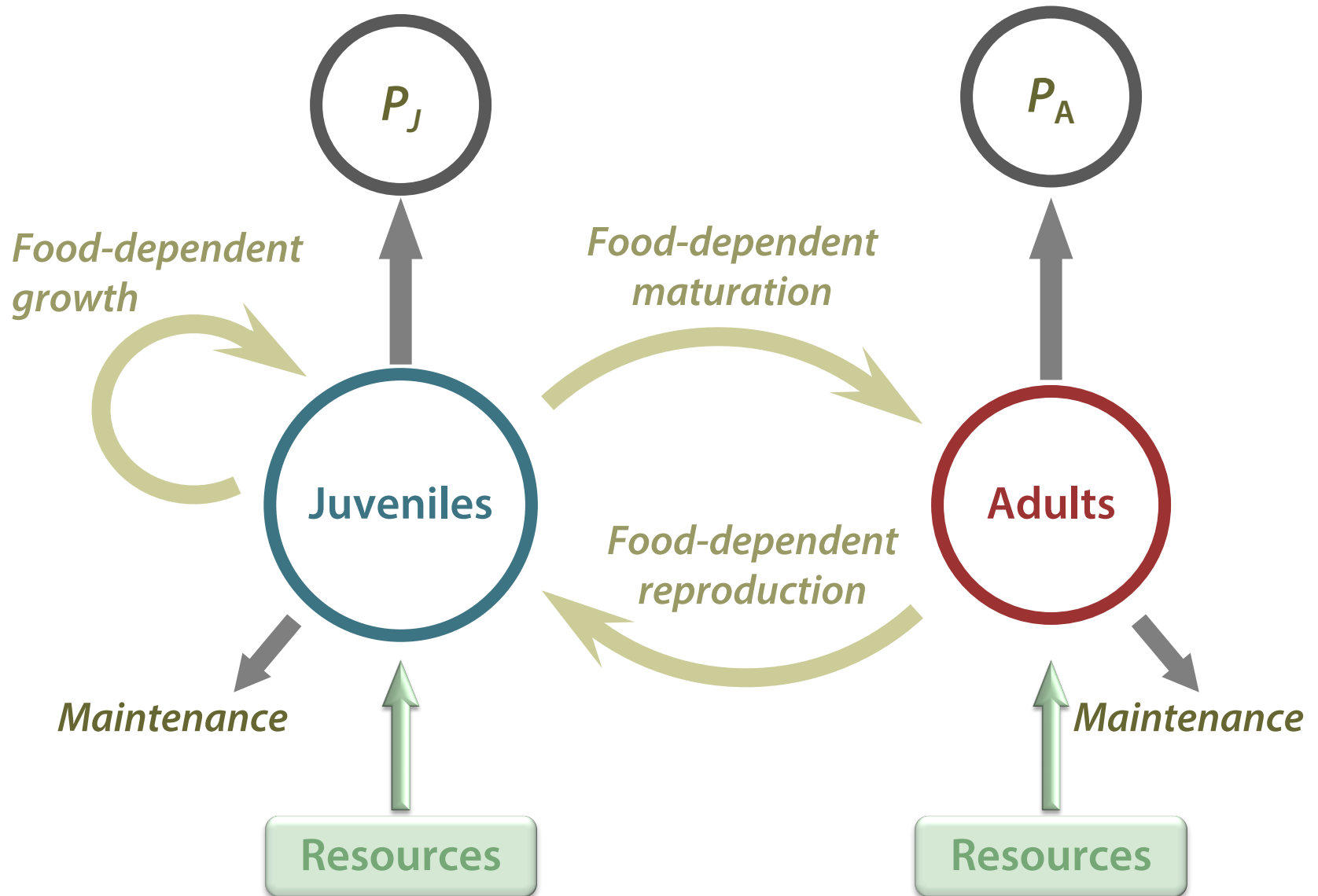
Two types of equilibria



Maturation-controlled, juvenile-dominated equilibrium and reproduction-controlled, adult-dominated equilibrium co-occur over large productivity ranges

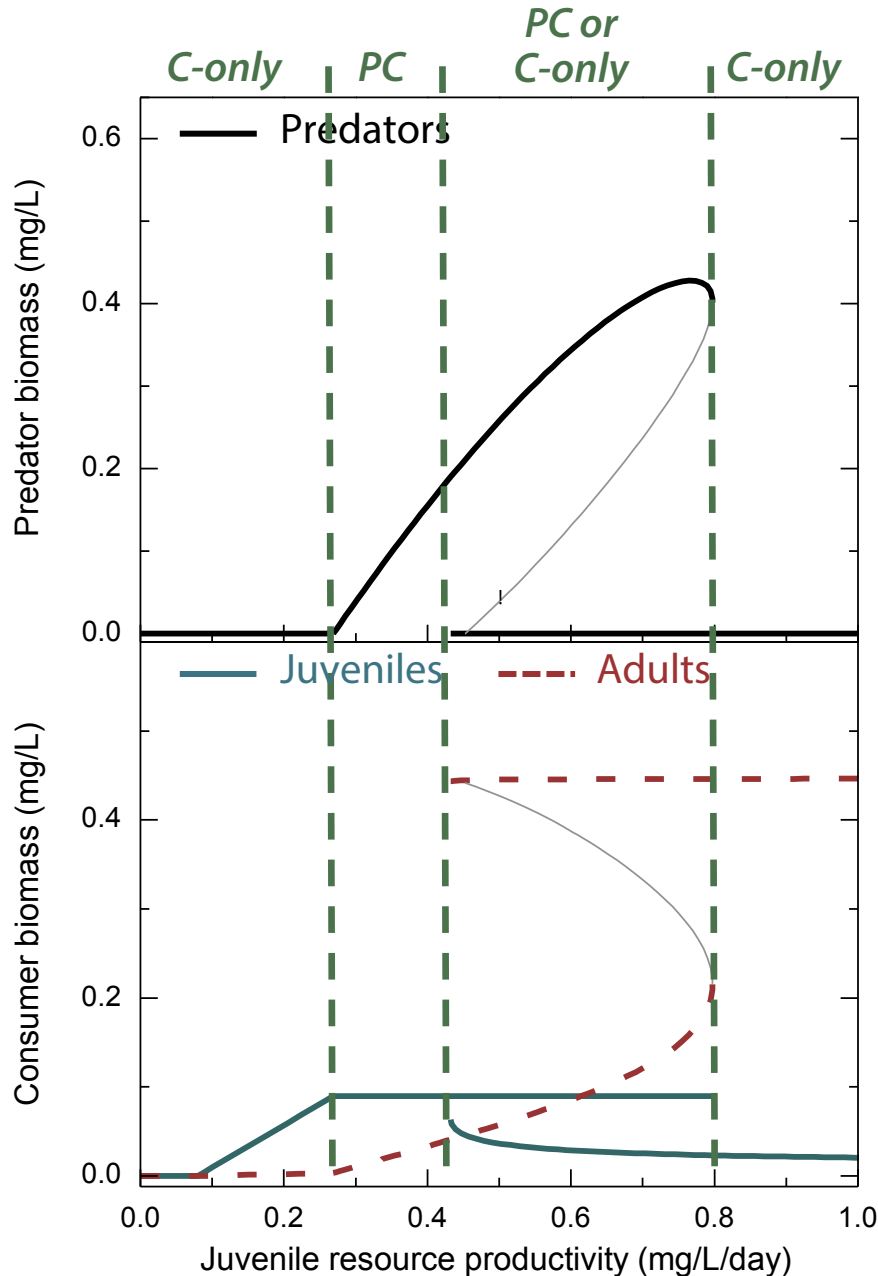


Adding specialist predators



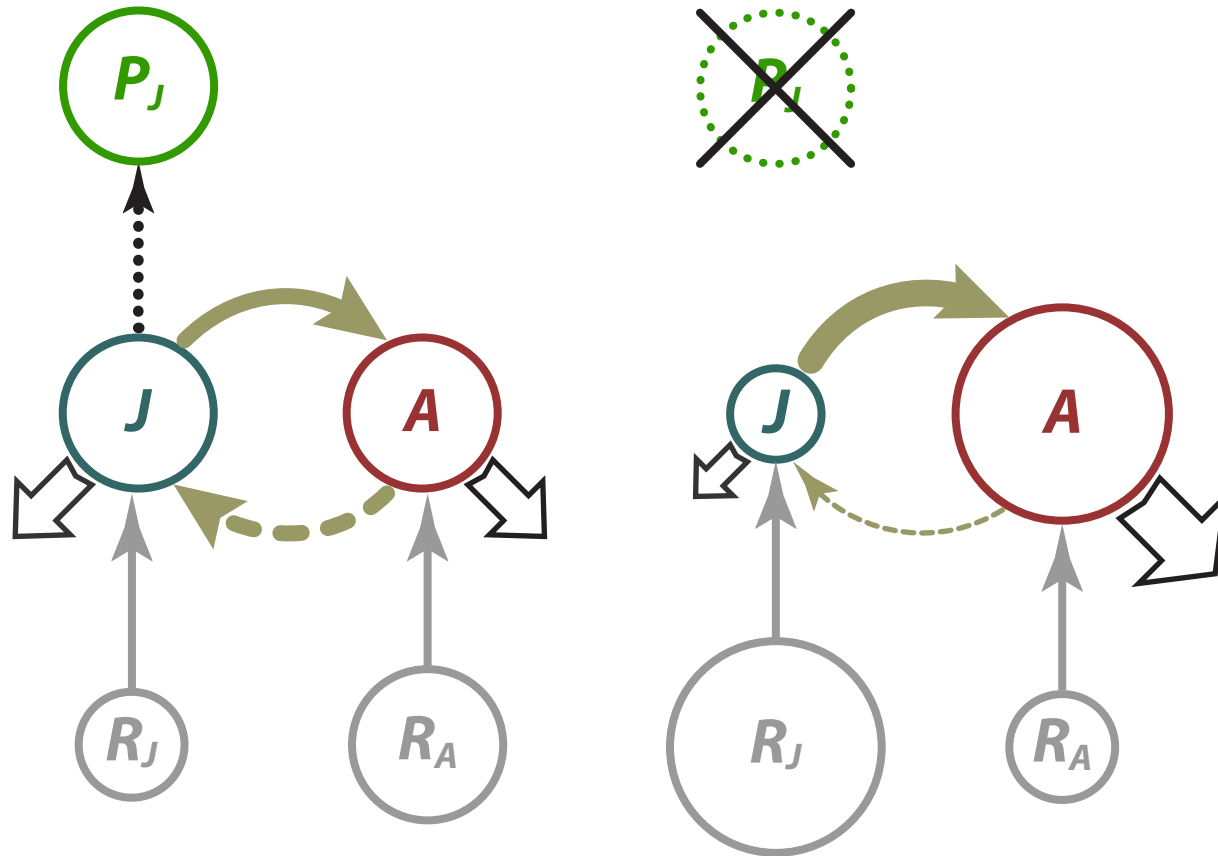


Juvenile specialist

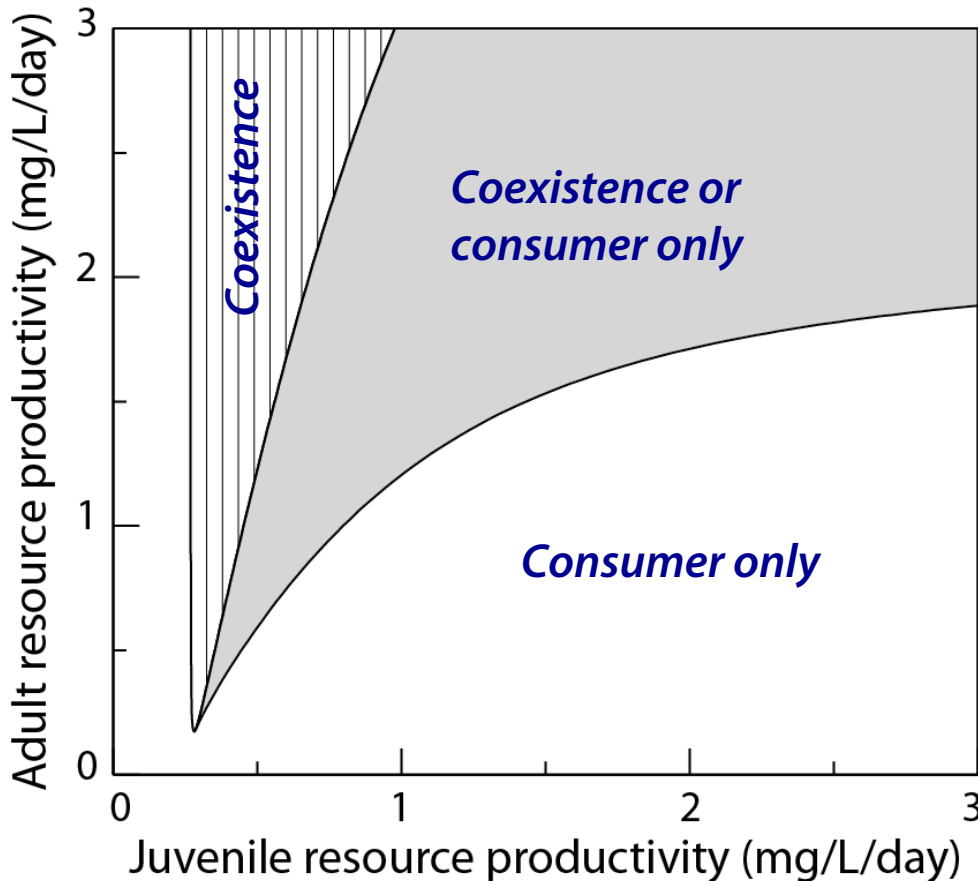


- Increasing **juvenile resource productivity**:
 - Coexistence** of consumers and a *juvenile-specialist predator*
 - Bistability** between coexistence equilibrium and consumer-only equilibrium dominated by adults (*reproduction controlled*)
 - Extinction** of predators

Emergent Predator Exclusion



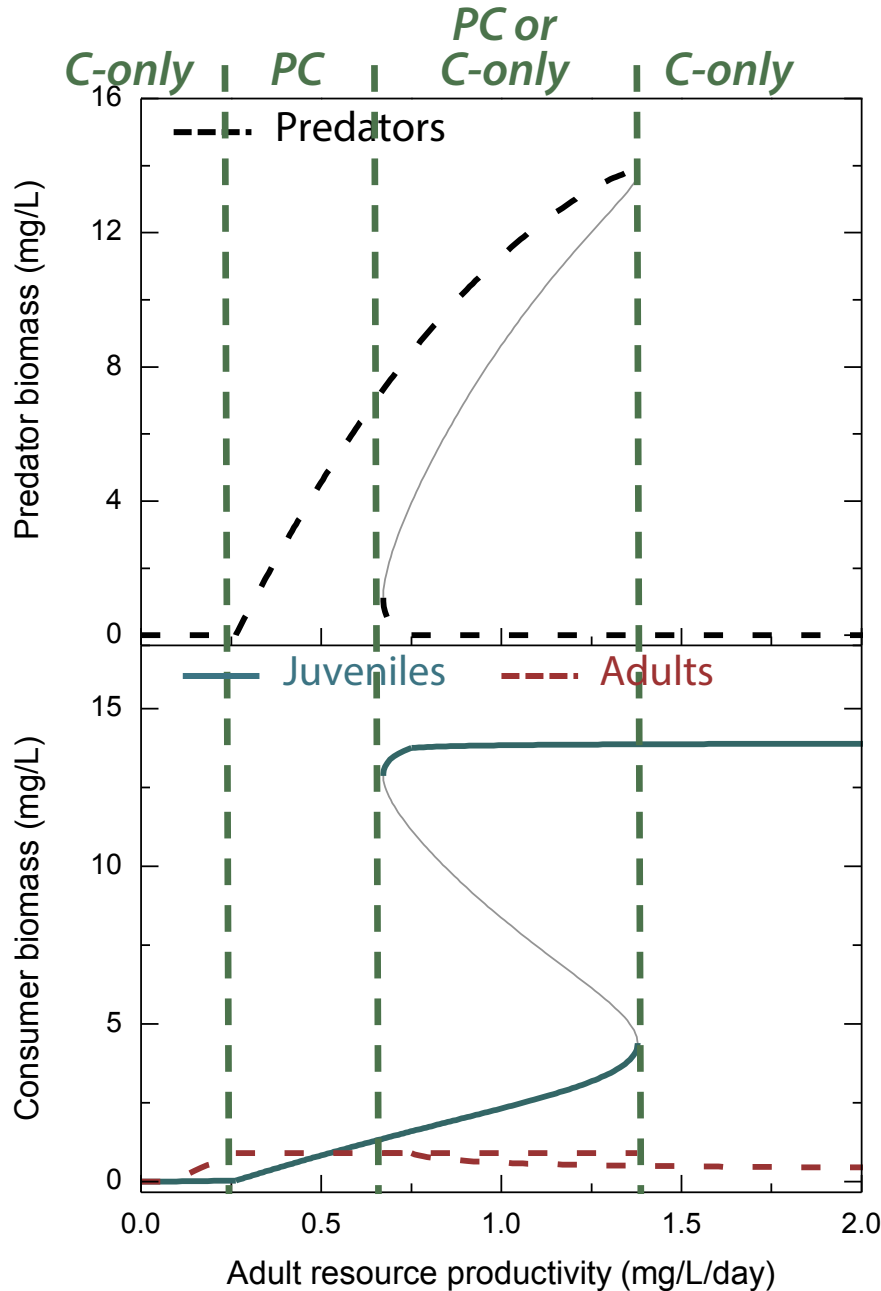
Persistence of juvenile-specialist predators



- **Predator persistence** only guaranteed at *low productivity of juvenile resource* (main prey) relative to adult resource productivity
- **Predator goes extinct** when *increasing resource availability of its main prey* (juvenile consumers) (**Inverse bottom-up effect!**)



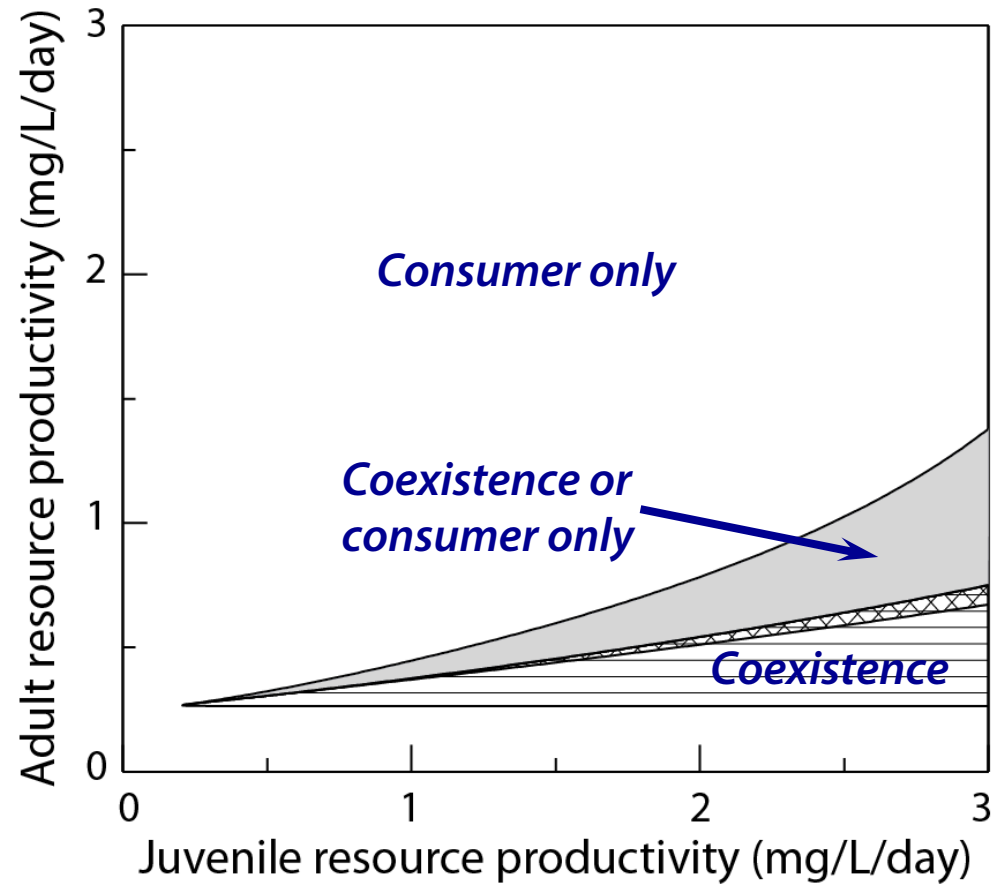
Adult specialist



- Increasing **adult resource productivity**:
 - **Coexistence** of consumers and an *adult-specialist predator*
 - **Bistability** between coexistence equilibrium and consumer-only equilibrium dominated by juveniles (*maturation-controlled*)
 - **Extinction** of predators

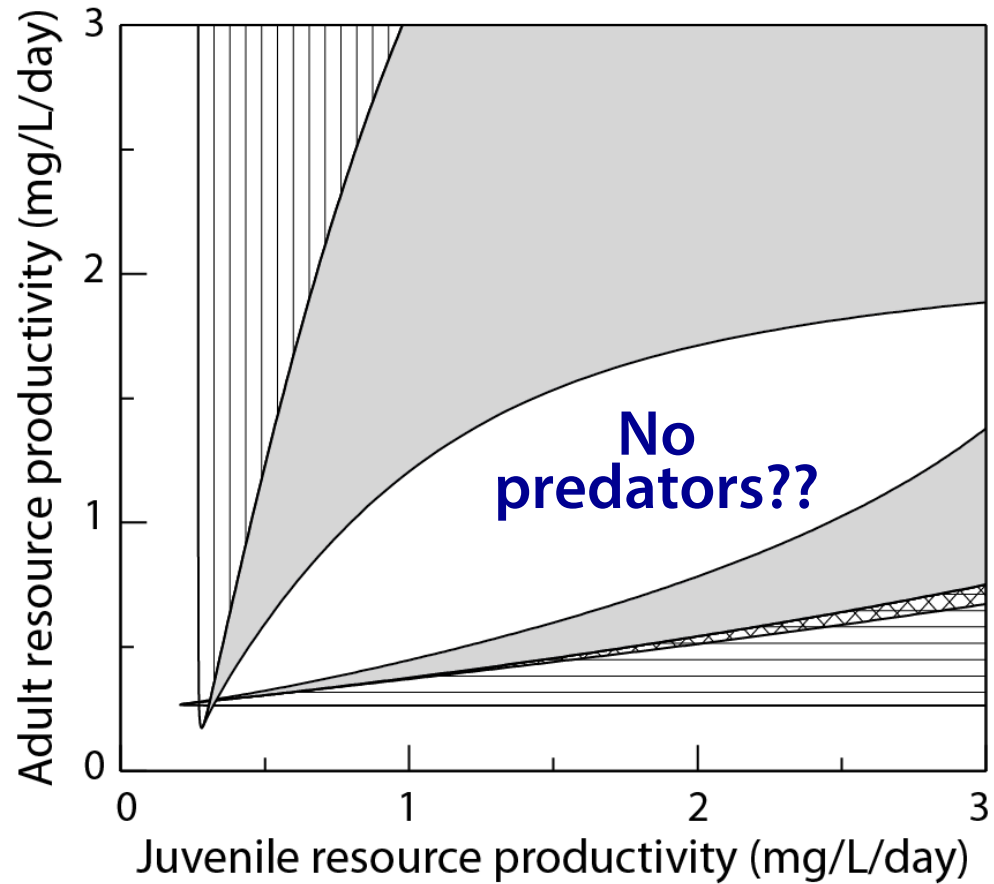
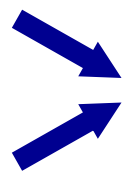
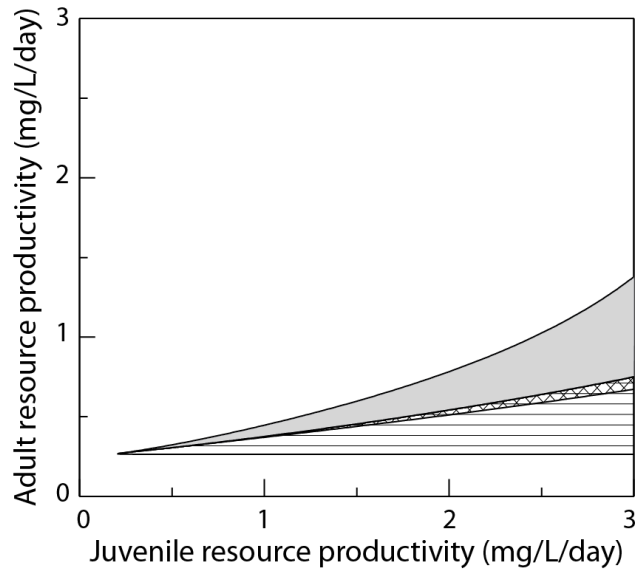
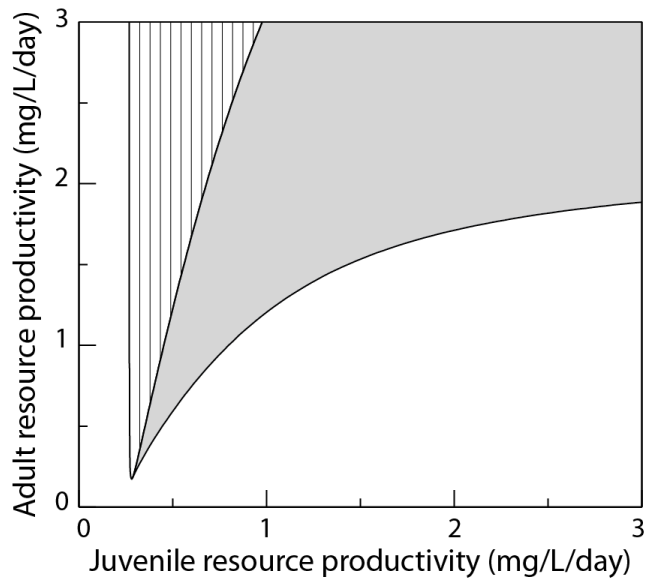


Persistence of adult-specialist predators



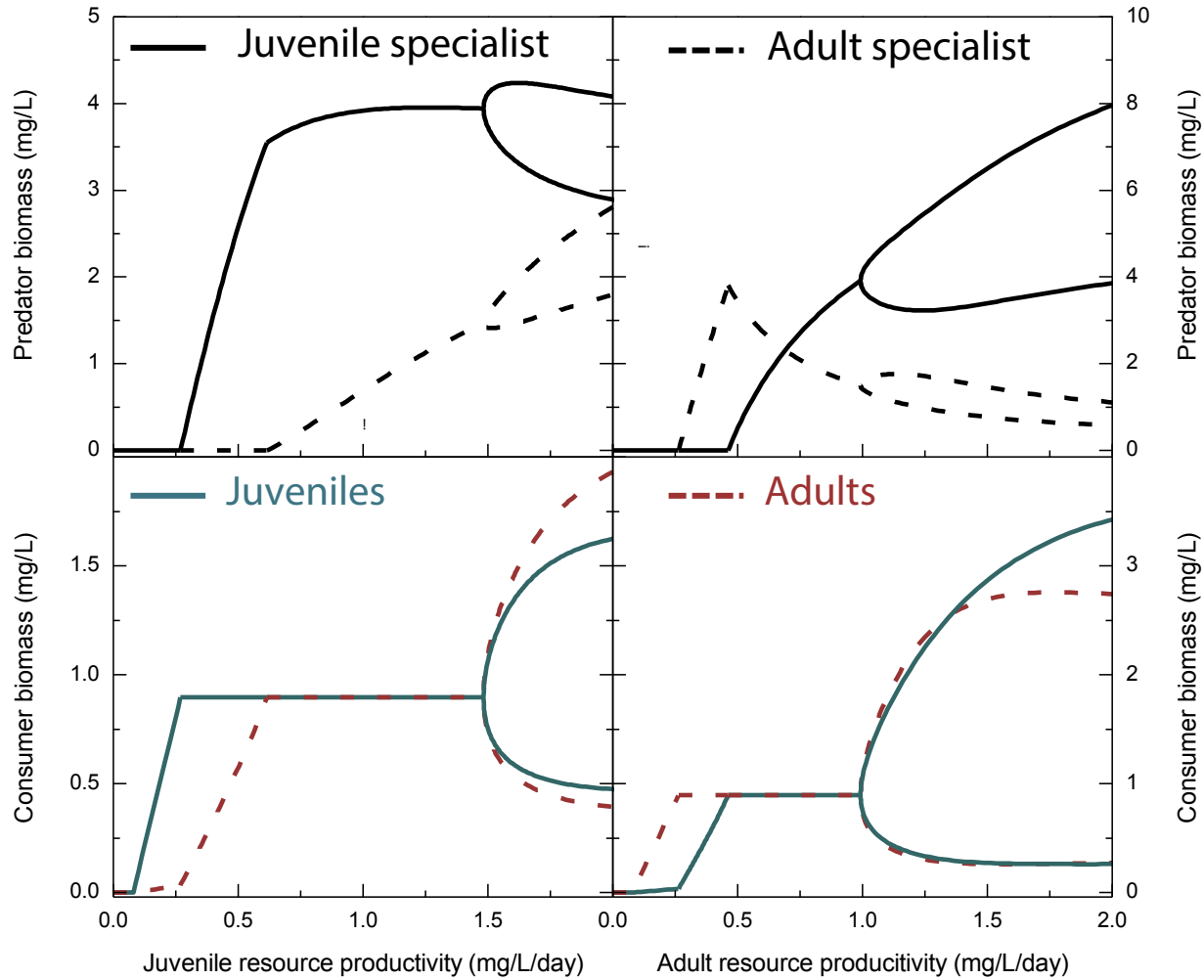
- **Predator persistence** only guaranteed at *low productivity of adult resource* (main prey) relative to juvenile resource productivity
- **Predator goes extinct** when *increasing resource availability of its main prey* (adult consumers) (**Inverse bottom-up effect!**)

What about predator coexistence?





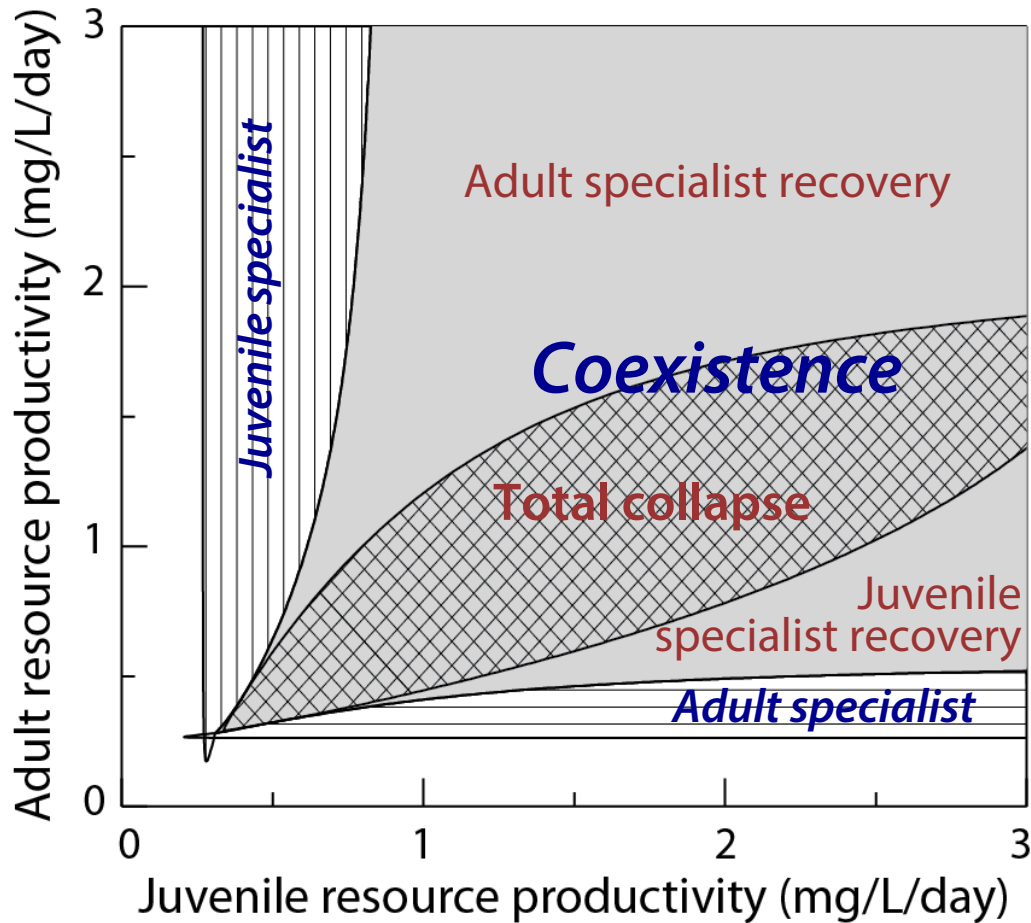
Stable coexistence of both specialist predators



Coexistence of both predators in stable equilibrium or stable limit cycle **over large ranges of productivity**, irrespective of which of the two resource productivities is increased



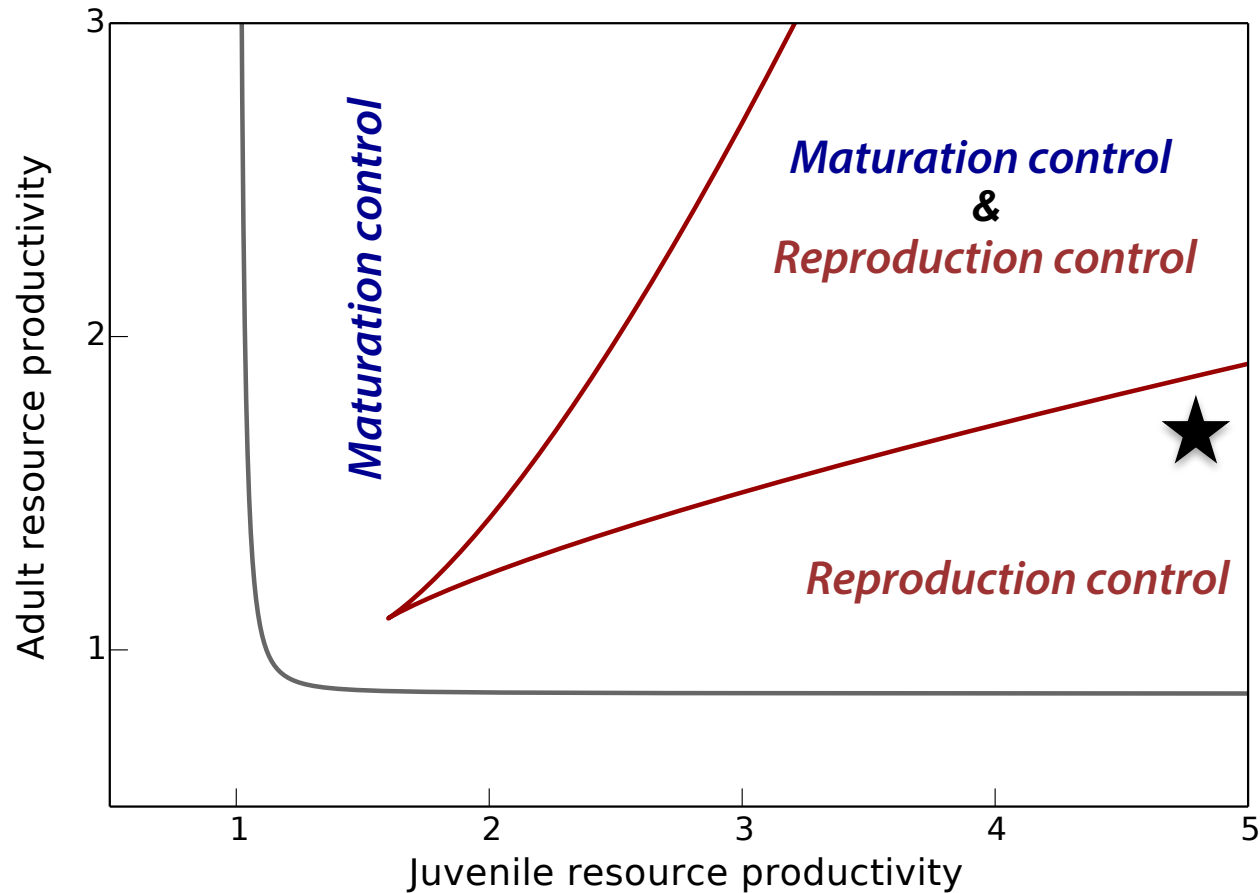
Stable coexistence of both specialist predators



- **Competitive dominance** of specialist predator at **low resource productivity of its main prey**
- **Coexistence** of specialist predators in stable equilibrium or stable limit cycle **over large ranges of productivity**
- **Extinction** of one of the specialist predators may lead to recovery or **total collapse**



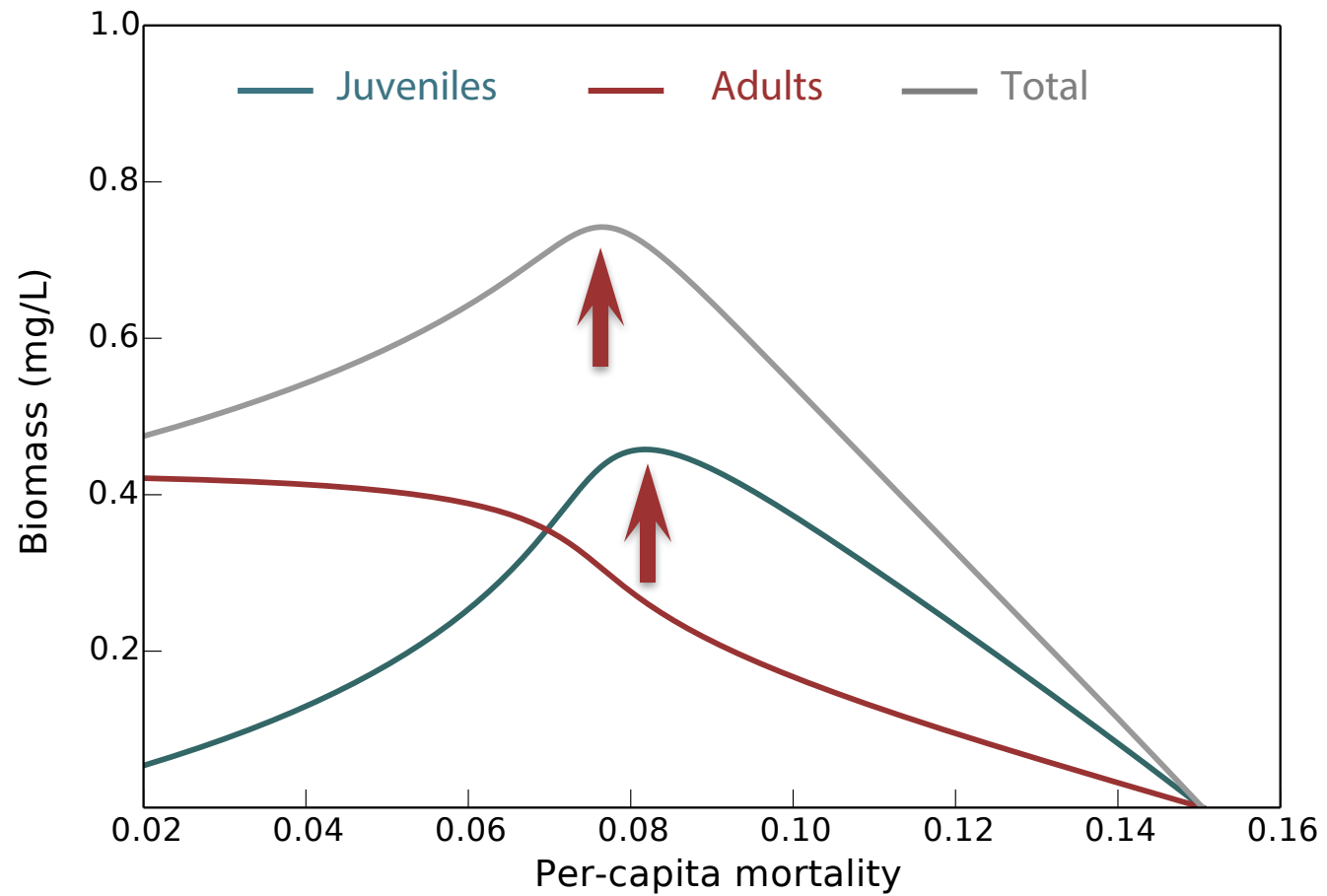
Two types of equilibria



Maturation-controlled, juvenile-dominated equilibrium and reproduction-controlled, adult-dominated equilibrium co-occur over large productivity ranges



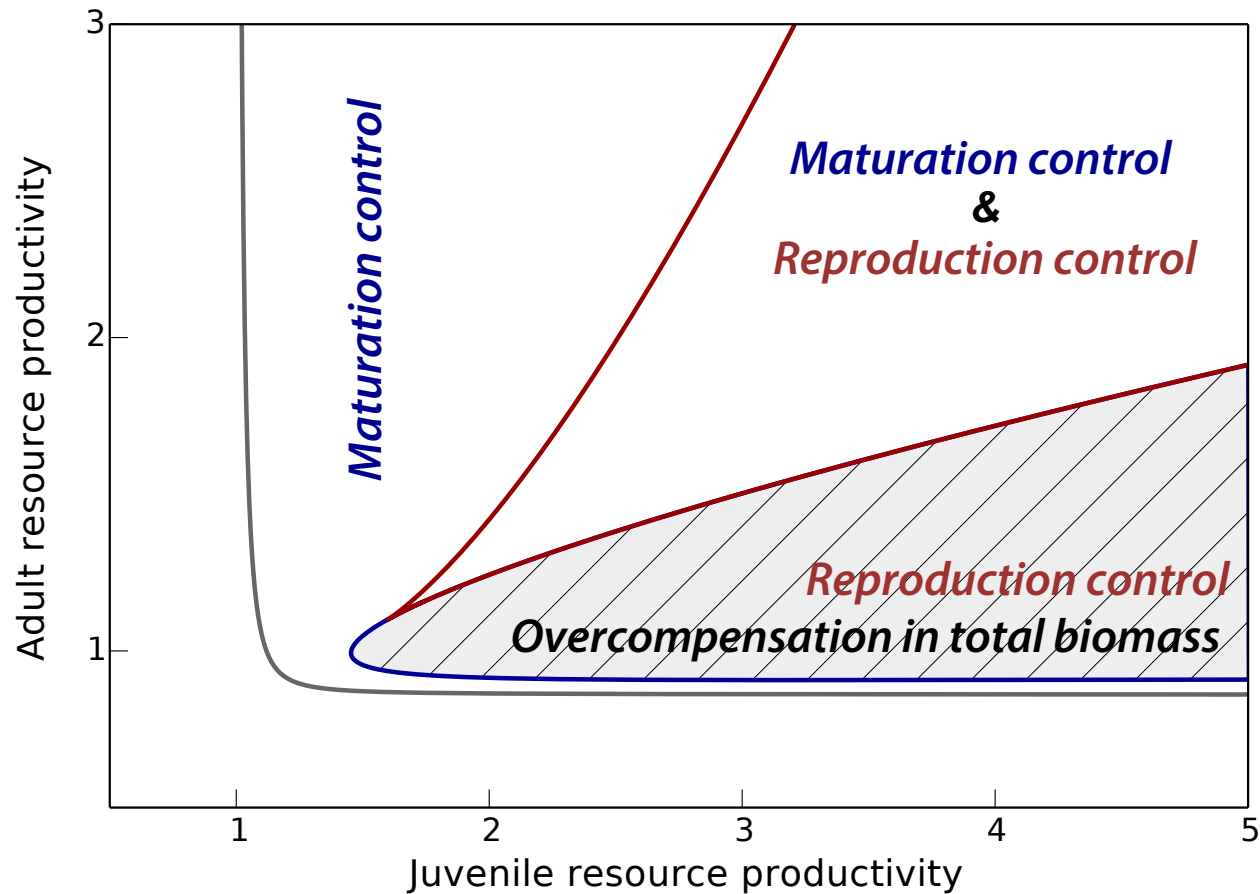
Overturning a basic ecological principle



Energetic asymmetry over ontogeny leads to counter-intuitive, positive biomass-mortality relations



Overcompensation in total biomass

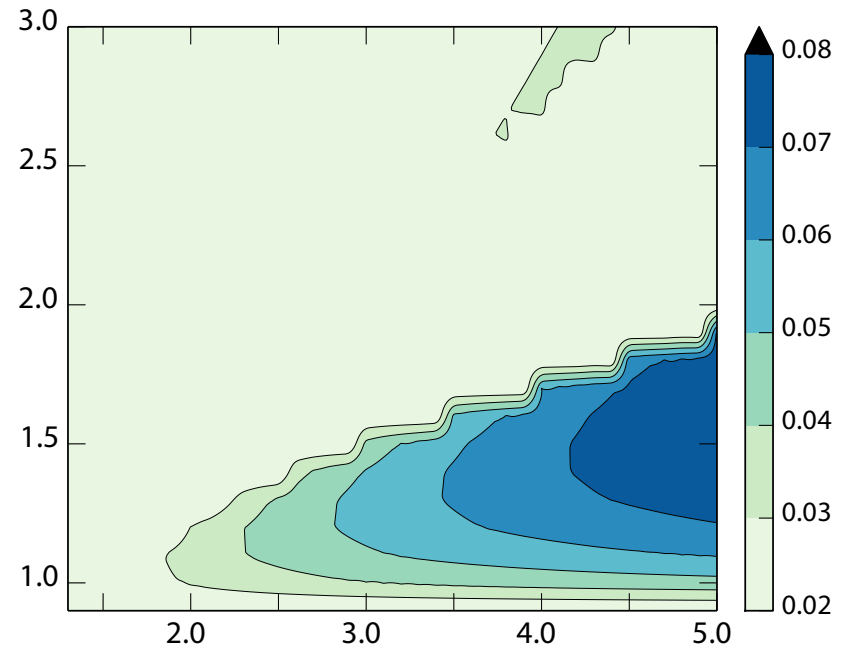
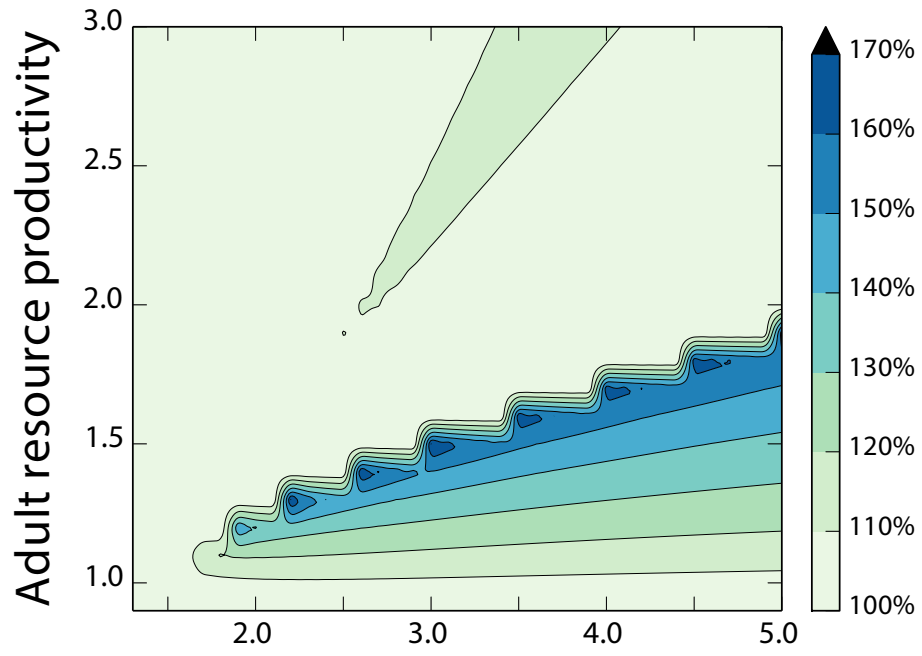




Higher biomass at higher mortality

Up to 60% more biomass

at up to 4 times background mortality

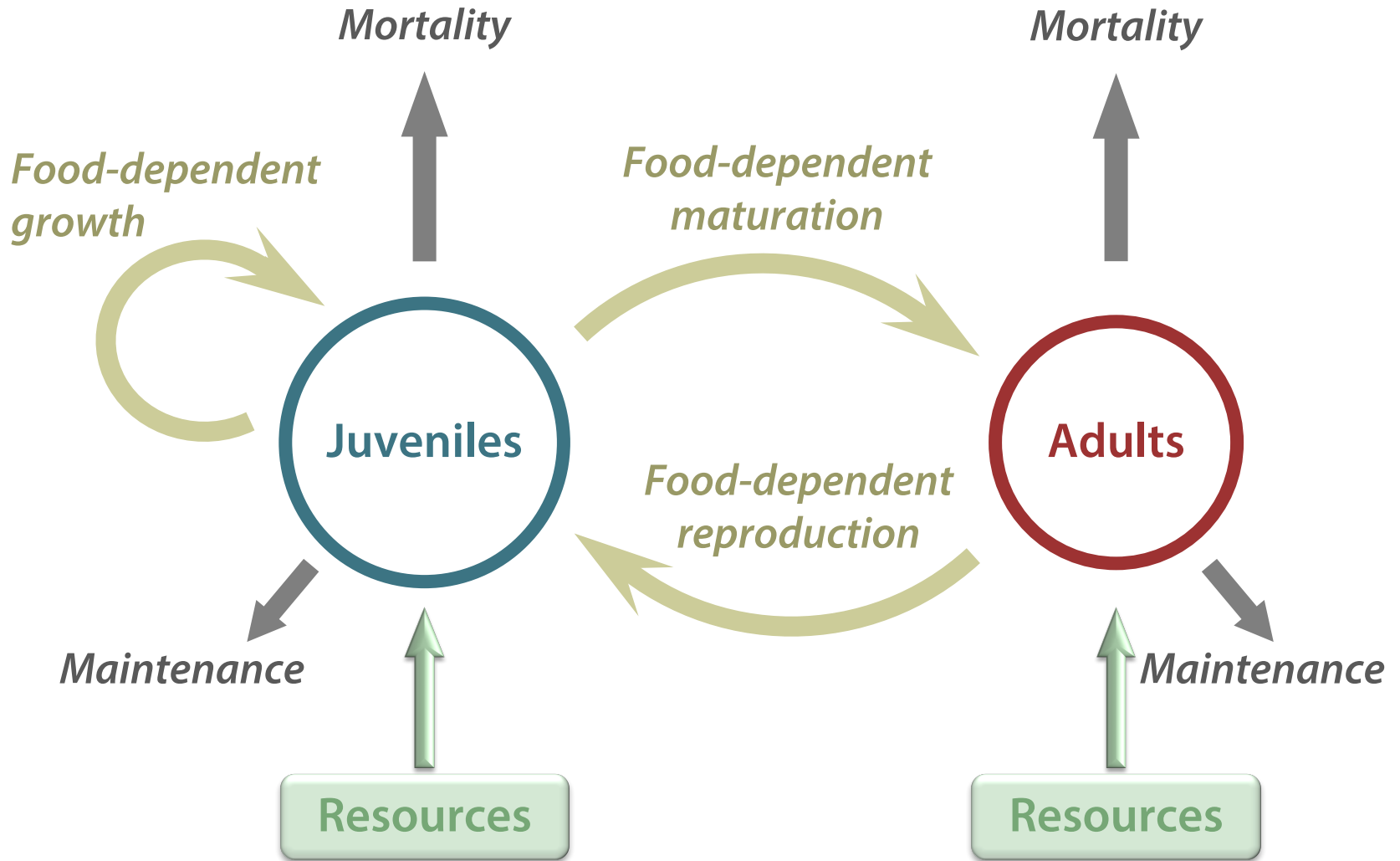


Juvenile resource productivity

Flexible population structure more in tune with resource supply at higher mortality, increasing efficiency

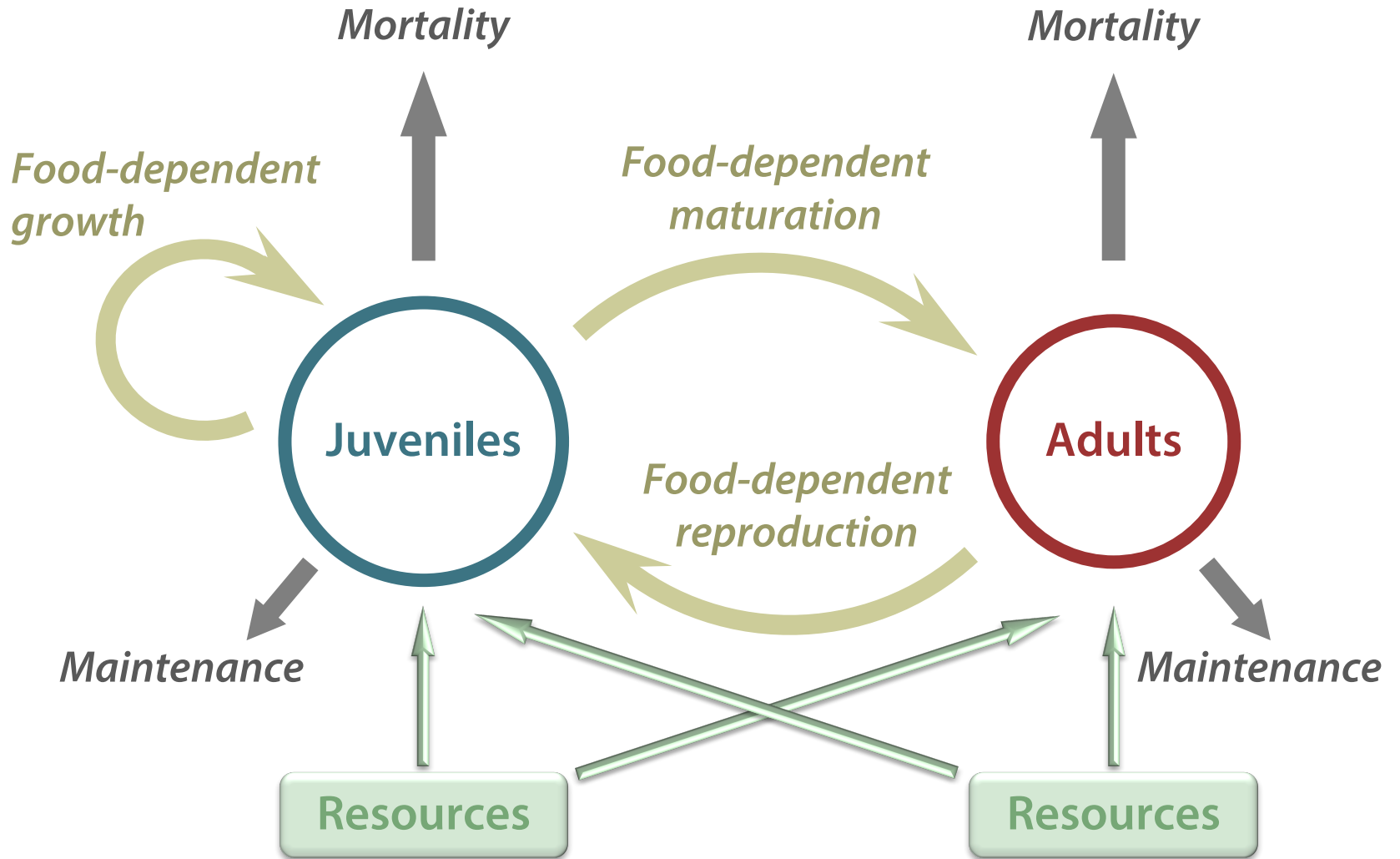


Ontogenetic specialist



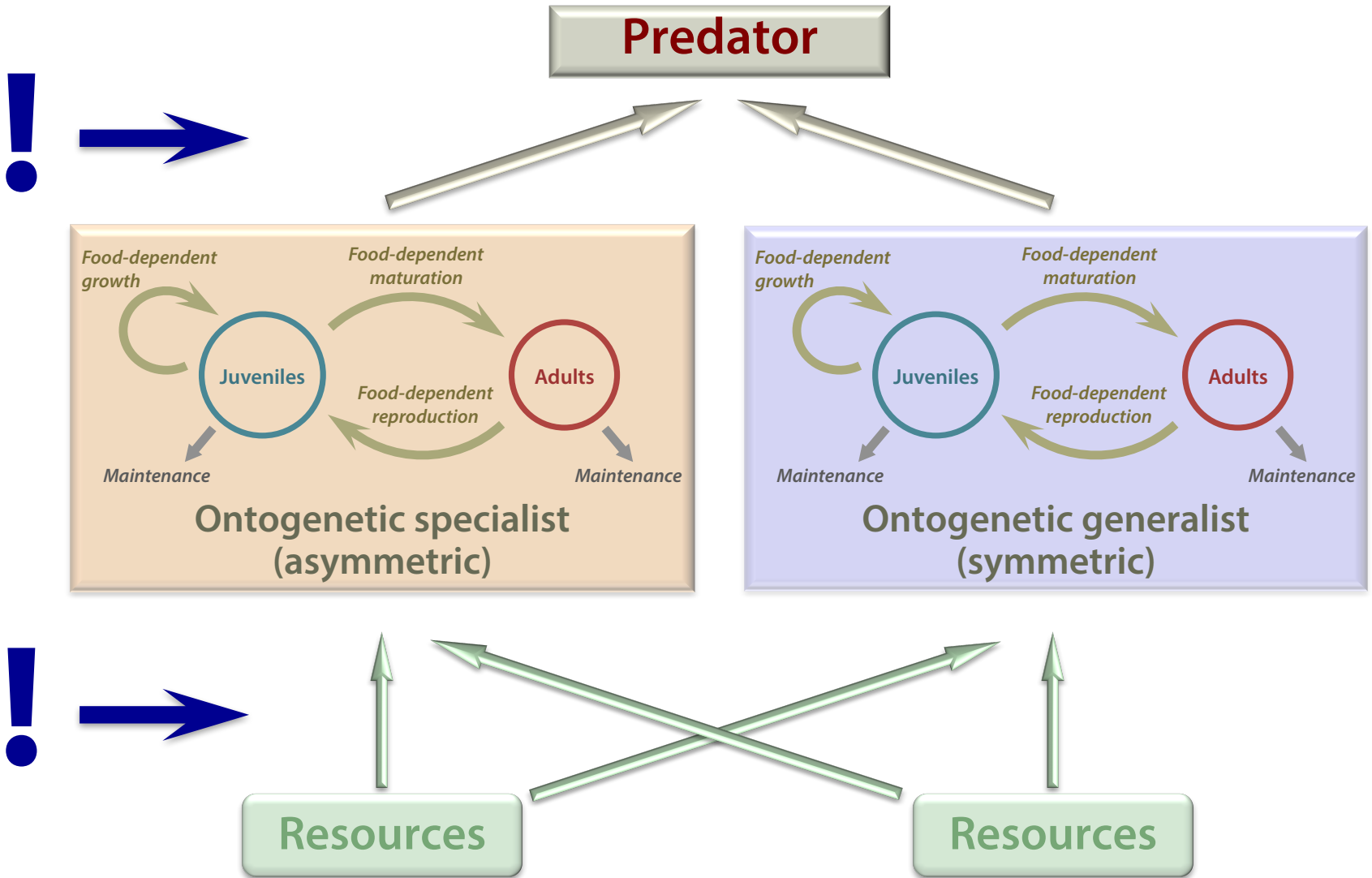


Ontogenetic generalist



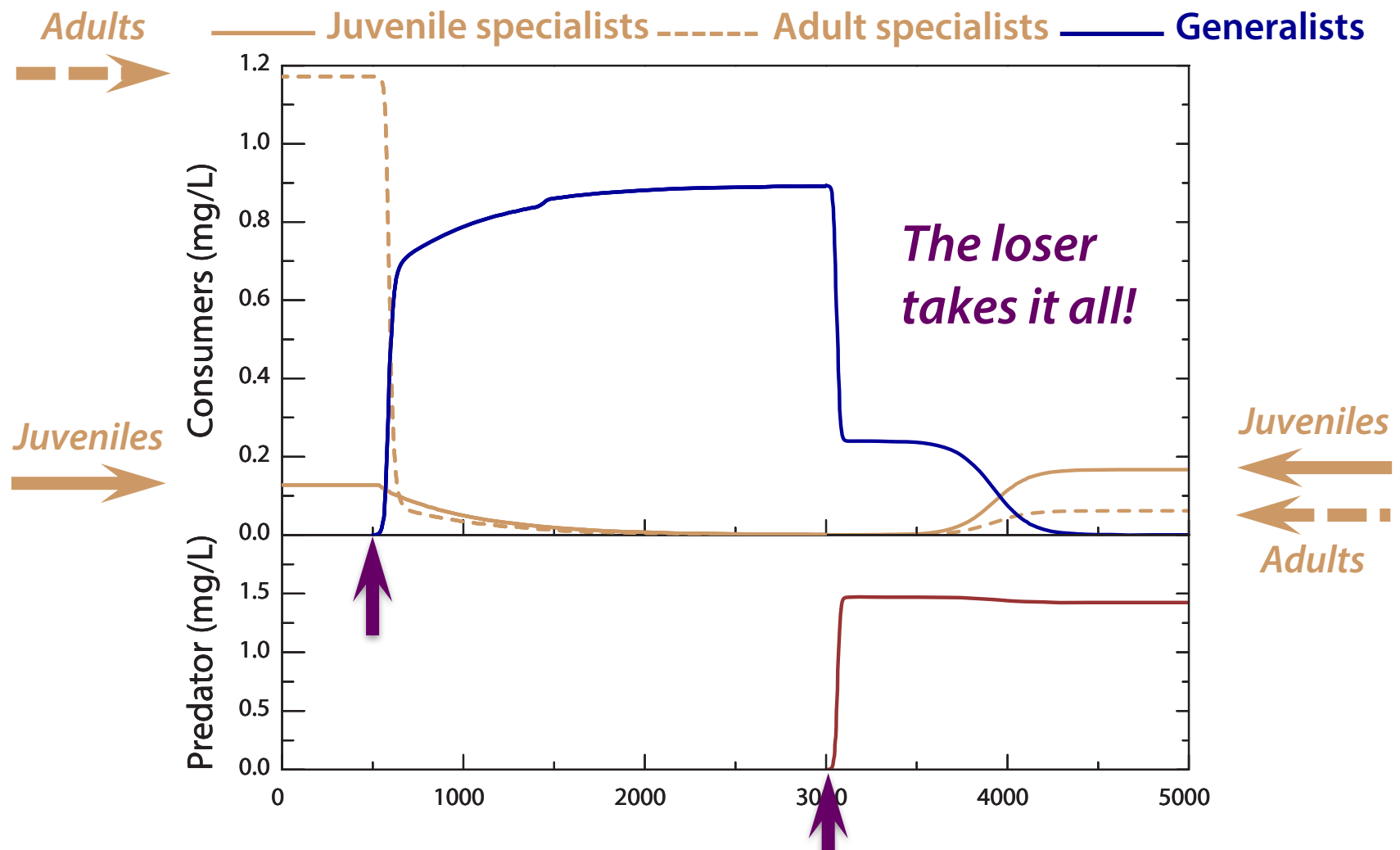


Competing as a double-handicapped consumer





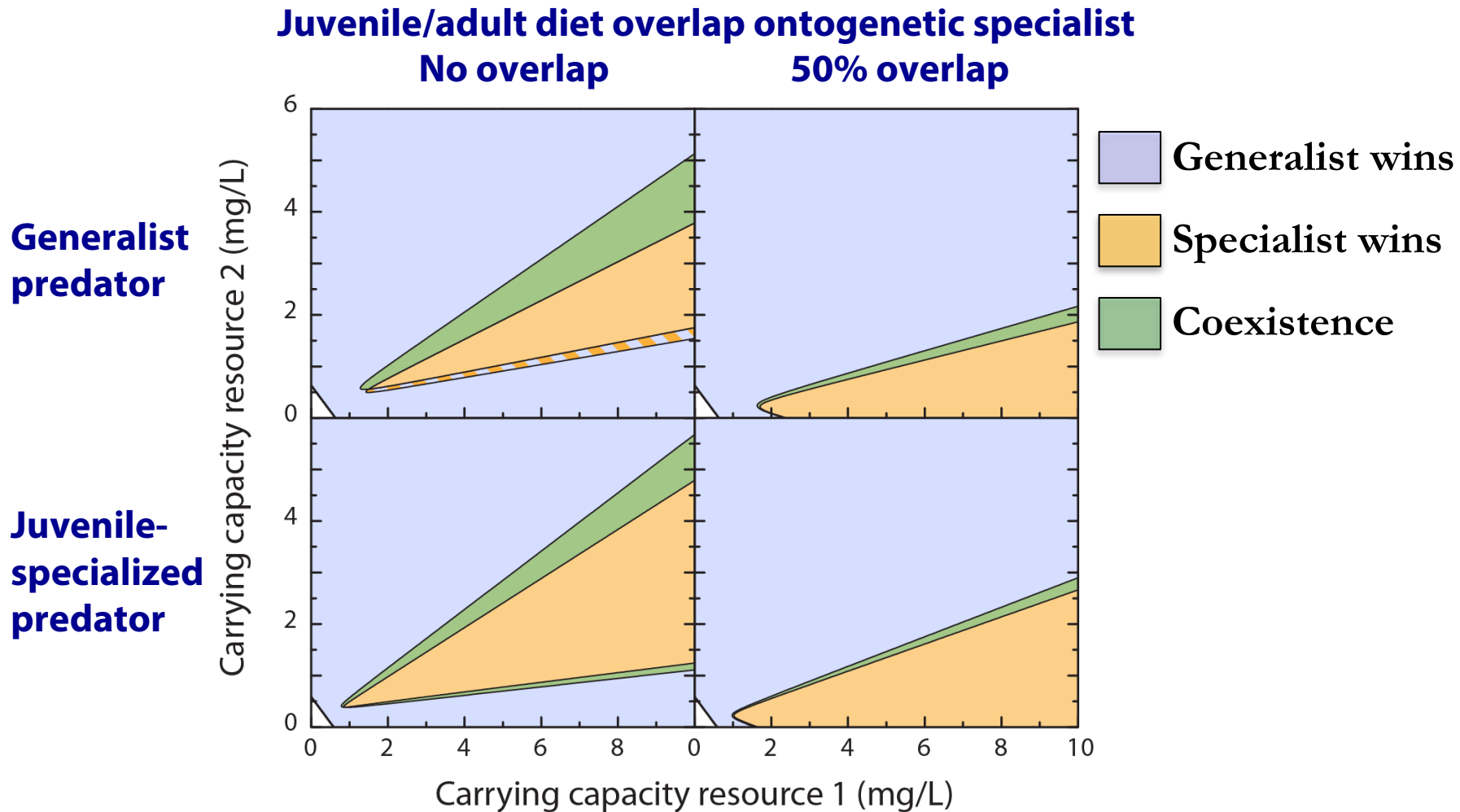
The fate of a double-handicapped loser



Double-handicapped loser wins under substantial ranges of productivity due to flexible population stage structure



The loser takes it all: a robust phenomenon



Irrespective of linear/non-linear functional responses, semi-chemostat/logistic resource dynamics, generalist/specialist predators, complete/partial niche shifts



Core ecological insights overturned

- Mortality decreases population abundance
Mortality increases stage-specific or total population biomass
- Food chains: productivity uniquely determines food chain length
Alternative stable equilibria in case of size-selective predation
- Predators foraging on the same prey will competitively exclude each other
Predators feeding on different size ranges of prey need each other to persist
- Persistence requires balancing competitive advantages against predatory disadvantages
In case of ontogenetic niche shifts, double-handicapped consumers with both a competitive and predatory disadvantage can outcompete competitors