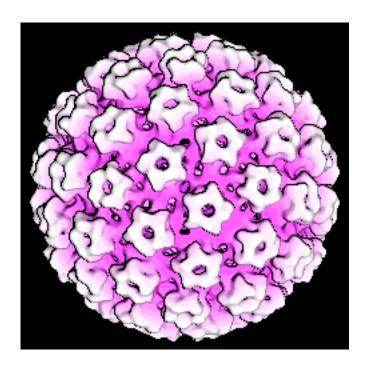
Evaluating HPV vaccination for children vs. adults

Robert Smith?

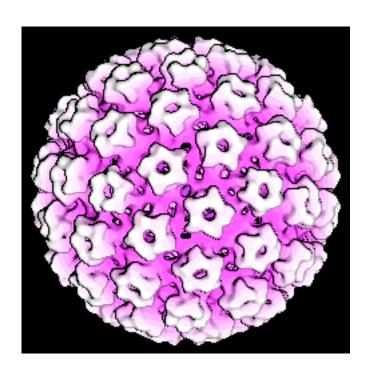
Departments of Mathematics and Faculty of Medicine
The University of Ottawa



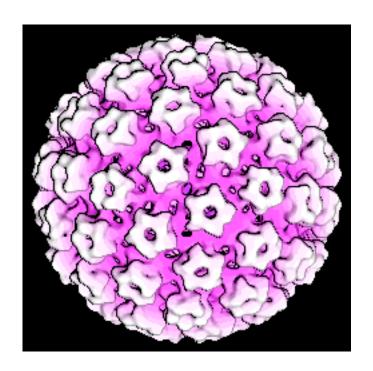
Epidemiology of HPV



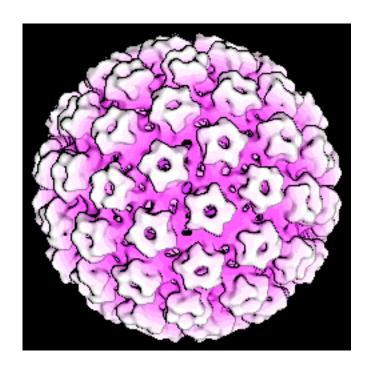
- Epidemiology of HPV
- Details of the vaccine



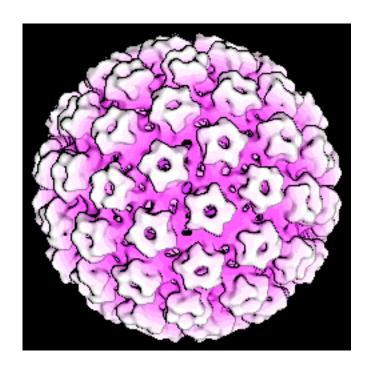
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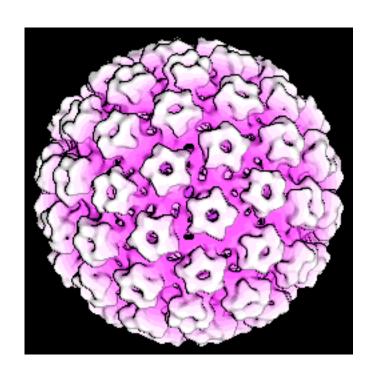
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- Research questions
- The mathematical model



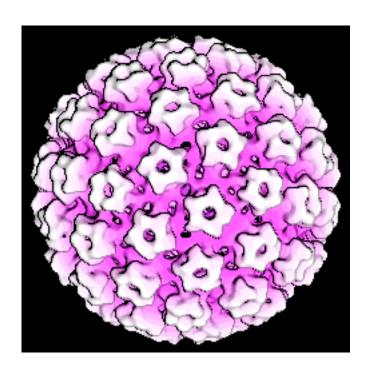
- Epidemiology of HPV
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- Research questions
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- Derive thresholds



- Epidemiology of HPV
- Details of the vaccine
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- What could go wrong?



- Epidemiology of HPV
- Details of the vaccine
- Research questions
- The mathematical model
- Derive thresholds
- What could go wrong?
- Recommendations.

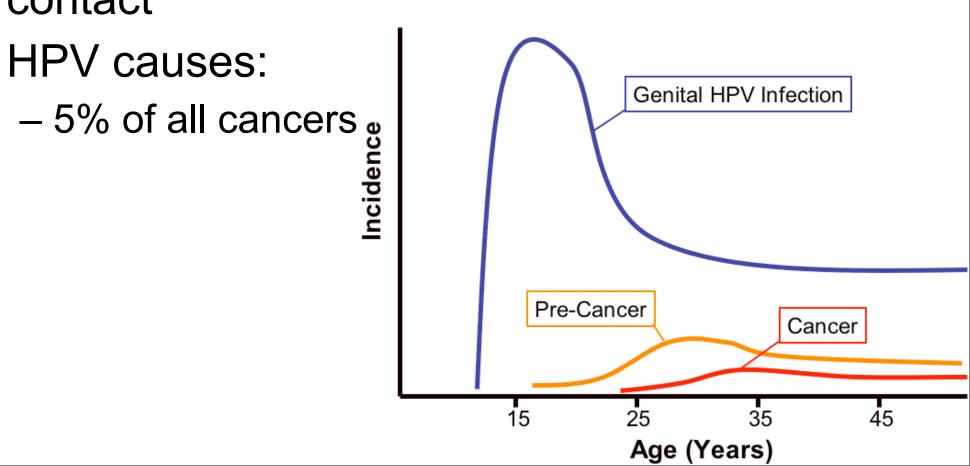


Over 100 different strains

- Over 100 different strains
- 30-40 strains are transmitted through sexual contact

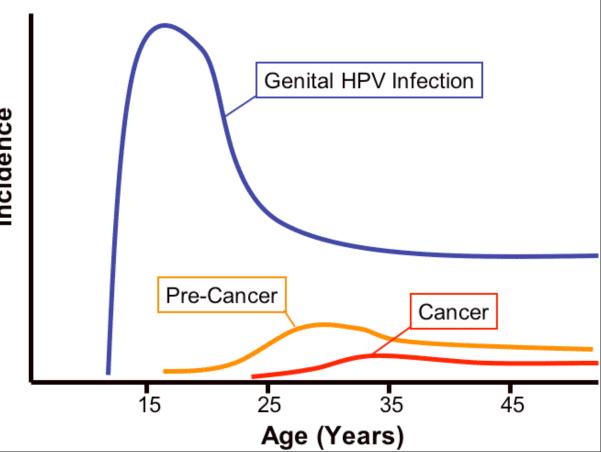
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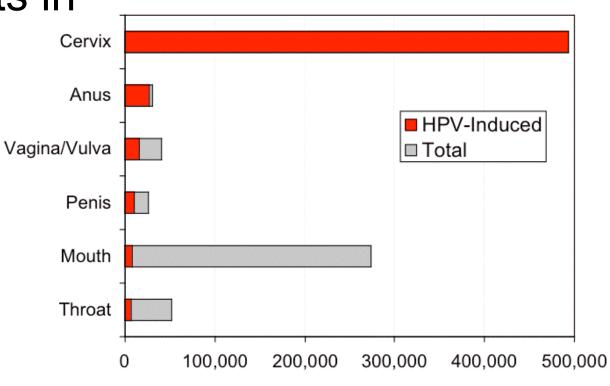
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 5% of all cancers women.

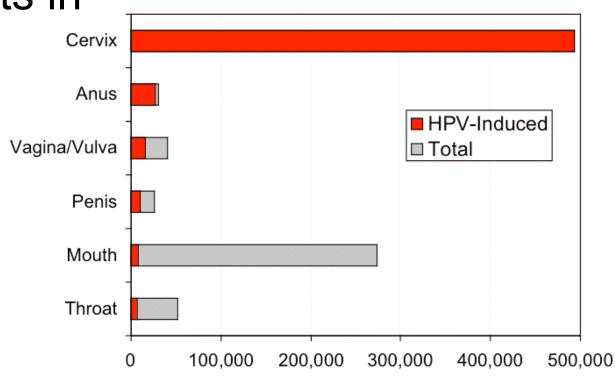




Annual number of cases worldwide

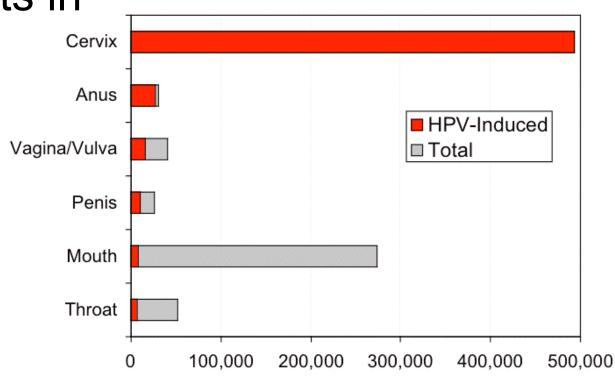
HPV infection results in

genital warts



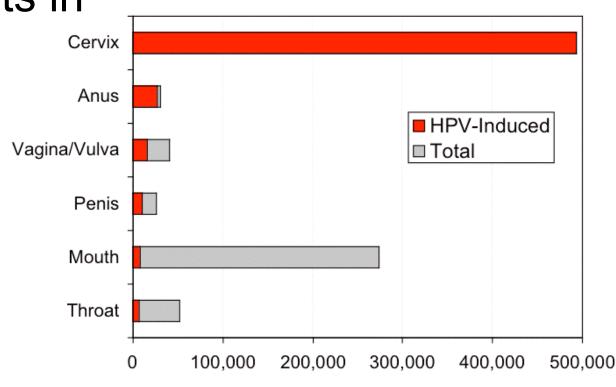
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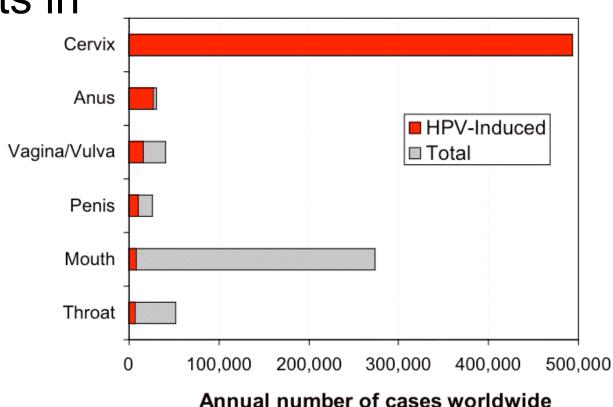
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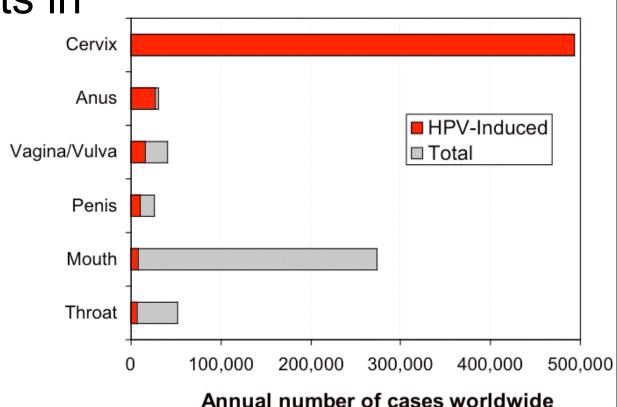


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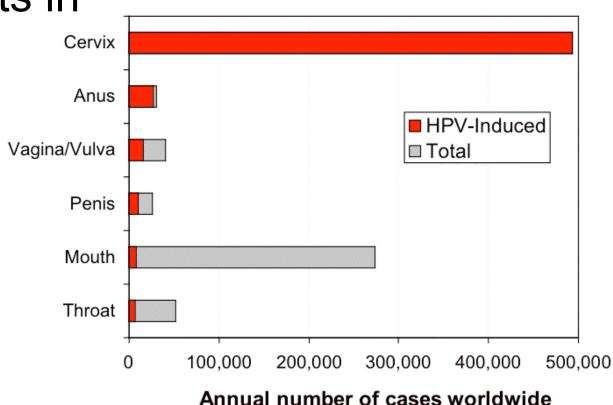
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- cervical cancer
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- genital warts
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- penile cancer
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- genital warts
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- penile cancer
- anal cancer
- respiratory Thromatory papillomatosis (vertical transmission)

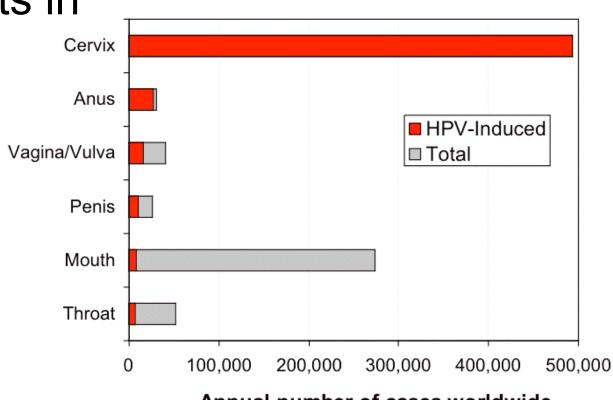


HPV infection results in

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- cervical cancer
- penile cancer
- anal cancer
- respiratory papillomatosis

(vertical transmission)

...requiring frequent surgery.



Annual number of cases worldwide

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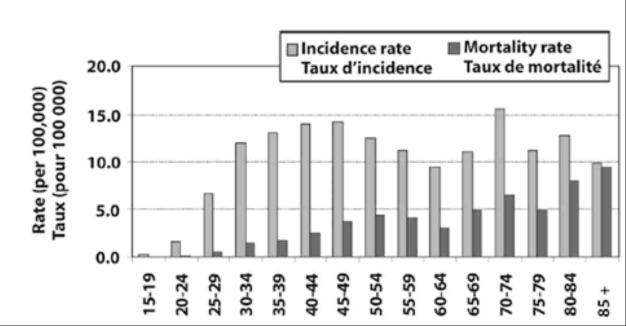
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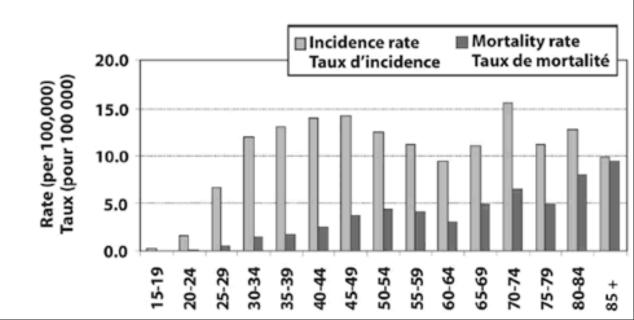
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 (detection relies upon the pap smear, which detects cellular abnormalities caused by HPV)
- Acquisition to malignancy takes >10 years
- Cervical cancer is the second most common cause of death from cancer in women.

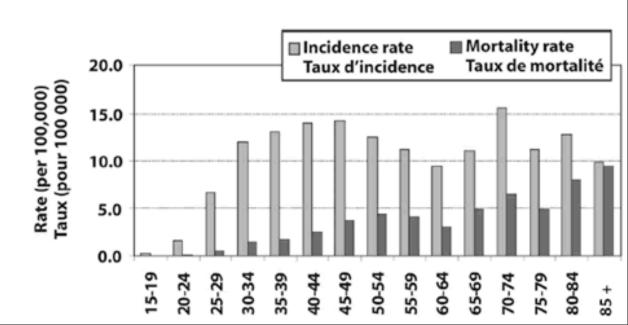
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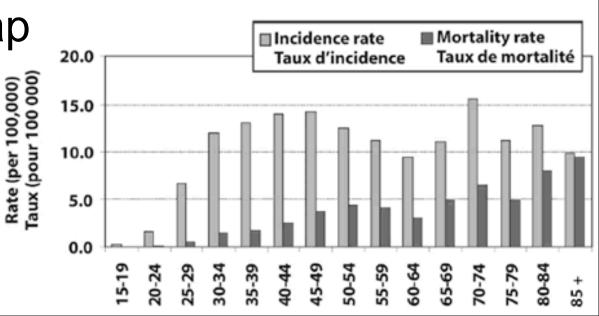


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- 3,900 deaths

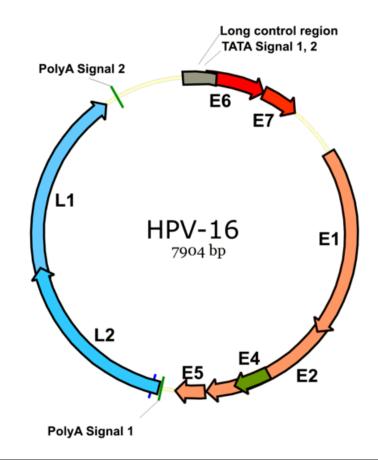


- 6,200,000 infections per year
- 14,000 women diagnosed with cervical cancer each year, leading to...
- 3,900 deaths
 (many fewer than would be caused by HPV,

due to effective pap smear screening and precancer treatments).

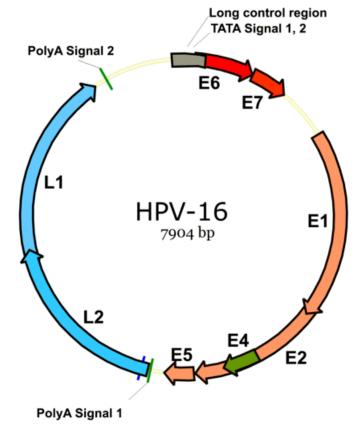


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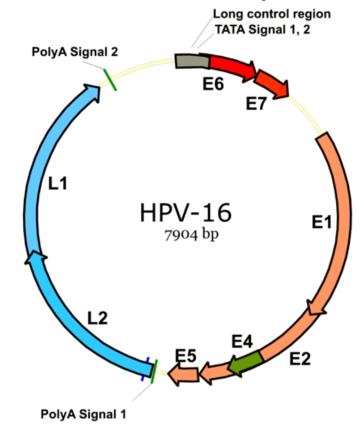
(as well as respiratory papillomatosis)



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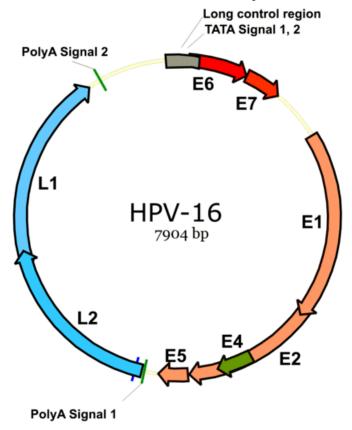
Types 16, 18, 31 and 45 lead to cancer



Types 6 and 11 account for 90% of genital wart infections

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- Types 16, 18, 31 and 45 lead to cancer
- Types 16 and 18 are responsible for 65% of cervical cancer cases.



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- Vaccines are estimated at 90-100% efficacy.



 Gardasil (Merck) protects against strains 6, 11, 16 and 18

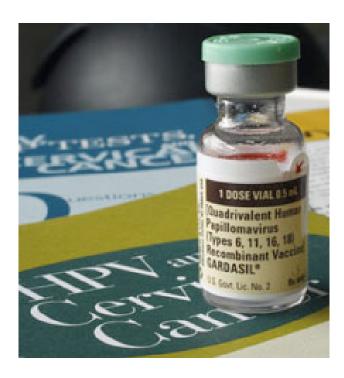
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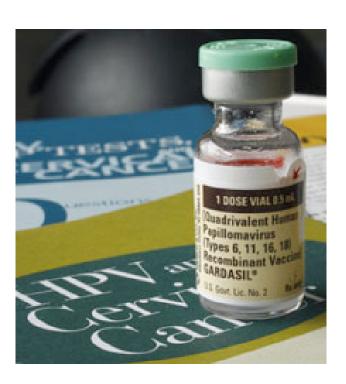
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- Cervarix (GSK) protects against strains 16 and 18 (the two most common cancer-causing strains)
- Some evidence of cross-protection against strains 31 and 45 (the other cancer strains).

Protects against both persistent and incident infections



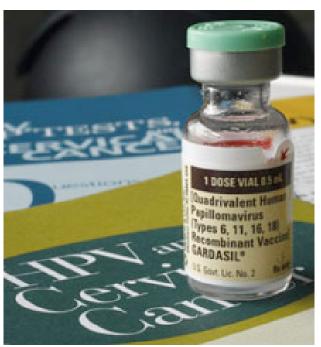
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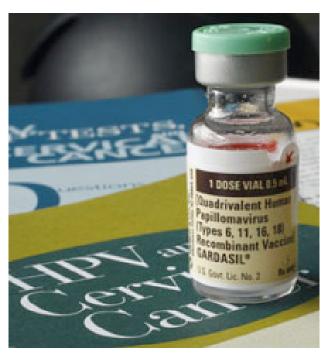
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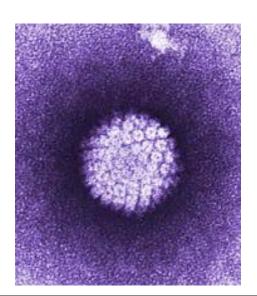
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- Three shots over six months, costing \$US360
- Recommended for women aged 9-26
- Highly immunogenic (98%)
- No evidence of waning (so far).



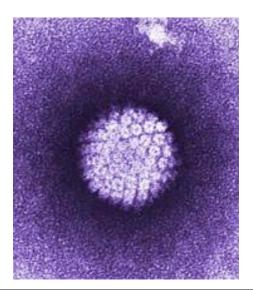
Men?

The vaccine has recently been approved for men



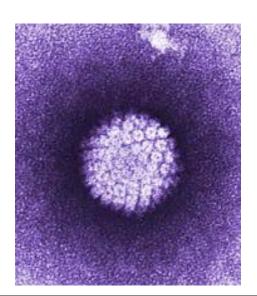
Men?

- The vaccine has recently been approved for men
- However, uptake rates are low



Men?

- The vaccine has recently been approved for men
- However, uptake rates are low
- Thus, we'll assume vaccinated men have a negligible effect on the outcome.



The rollout program

 Most provinces are now vaccinating girls aged 9-13

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(ie before they become sexually active)

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- Most provinces are now vaccinating girls aged 9-13
 - (ie before they become sexually active)
- The vaccine is available to women aged 14-26, but is not covered by Canadian health plans.

Coverage levels

 Initial surveys suggested that the majority of parents (77%) would be receptive to their children being vaccinated, if suitably informed about HPV



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In the first year, Ontario reported only 53%

vaccination coverage.



Can a childhood-only vaccination program eradicate HPV?

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- Should an adult vaccination program supplement childhood vaccination?

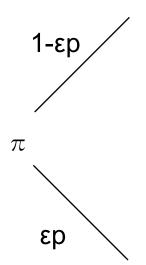
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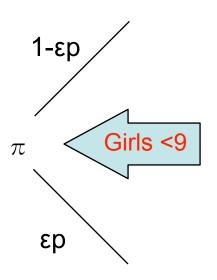
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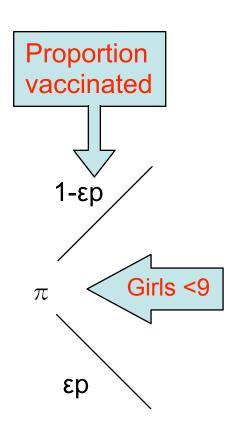
(ie the vaccine doesn't always protect)

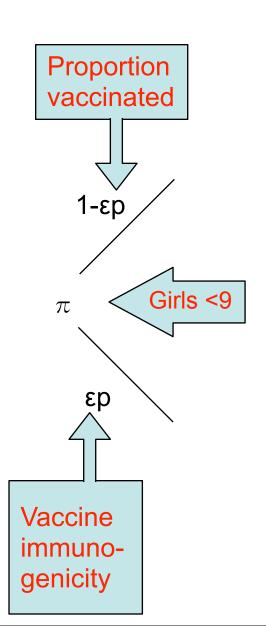
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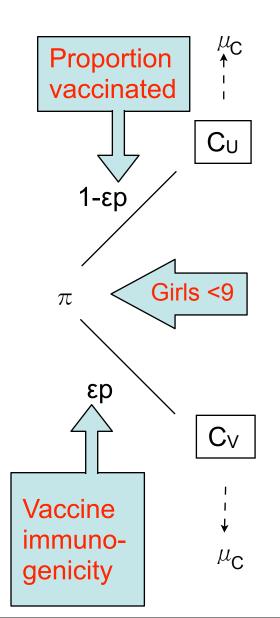
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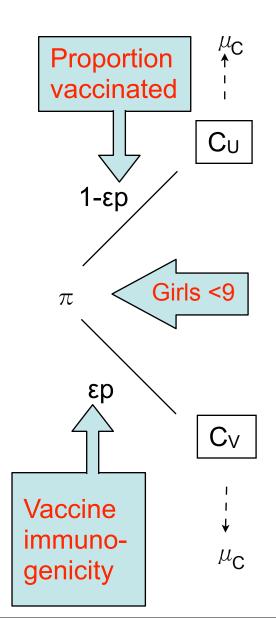




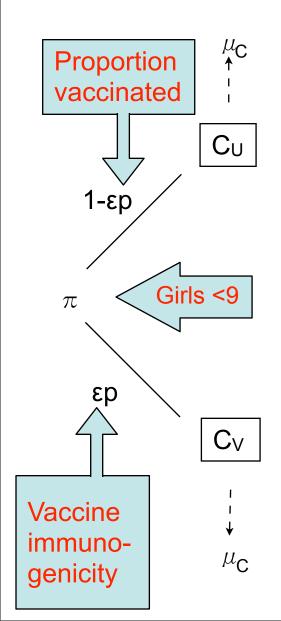






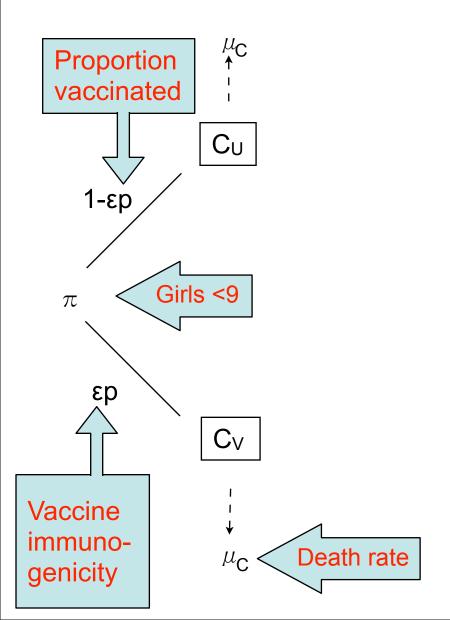


UNVACCINATED

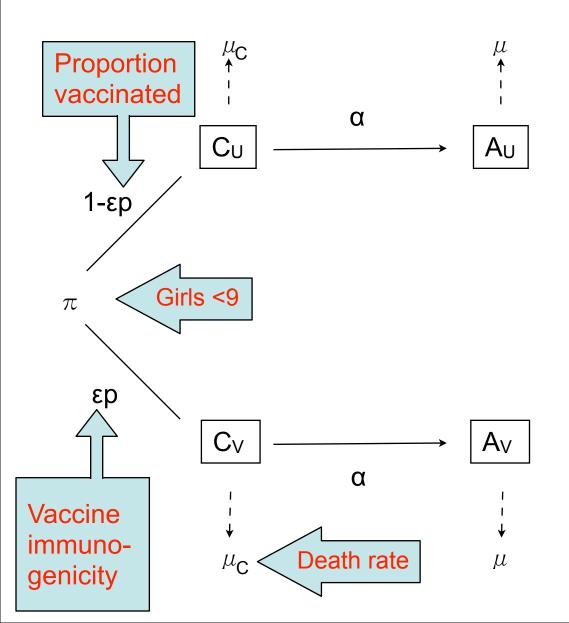


UNVACCINATED

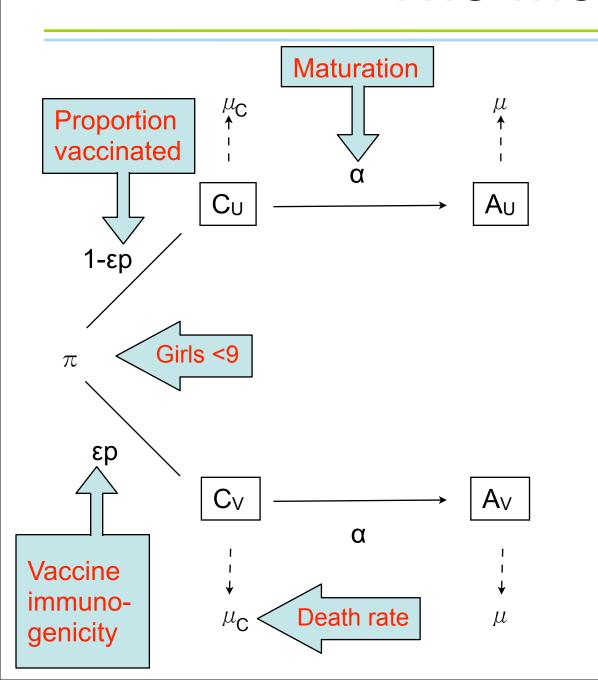
VACCINATED



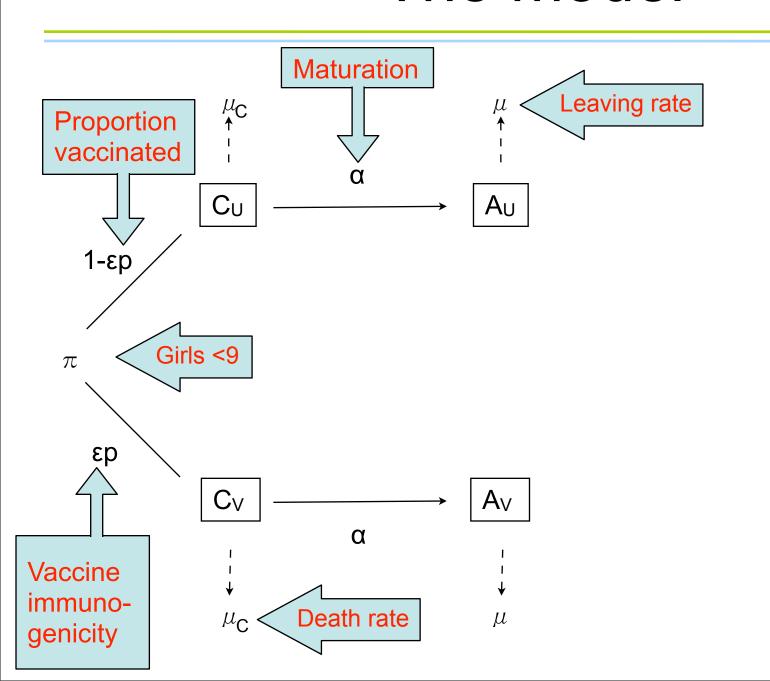
UNVACCINATED



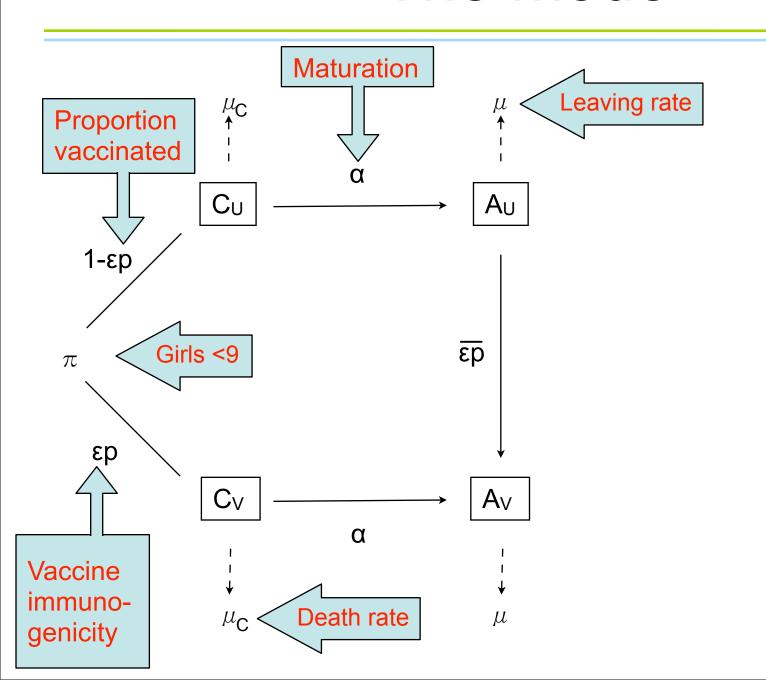
UNVACCINATED



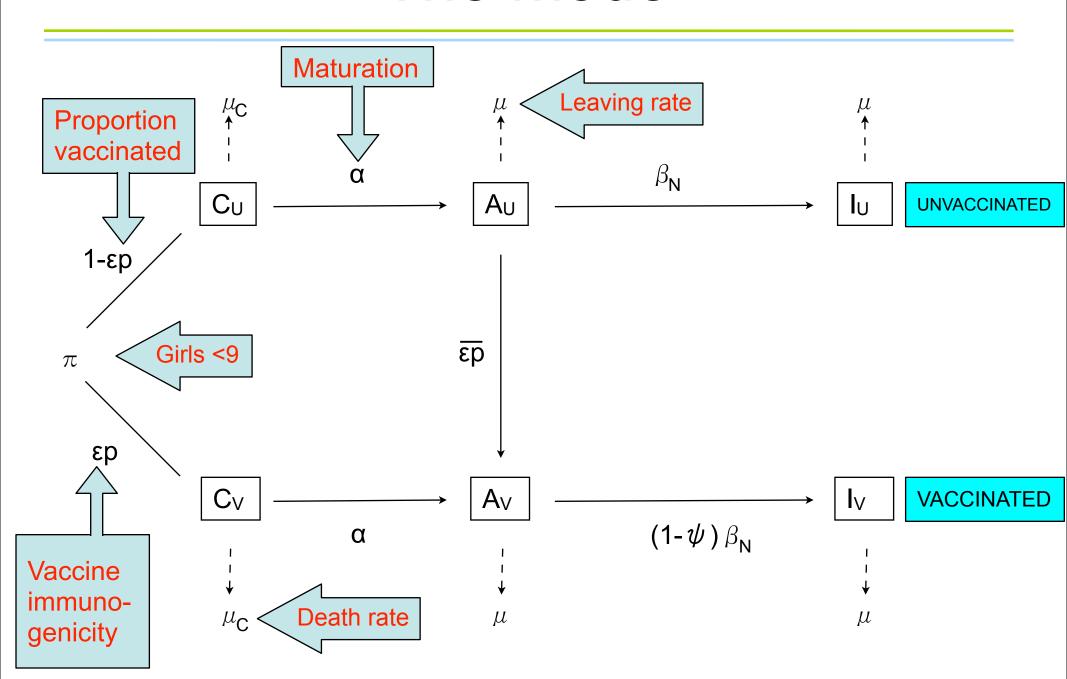
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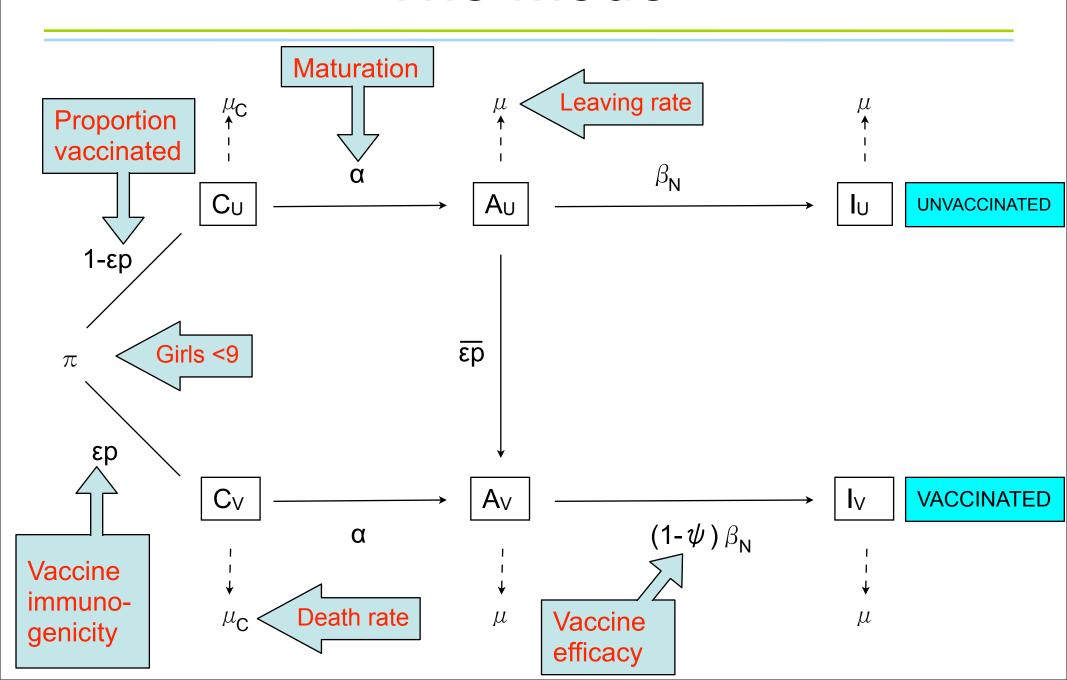


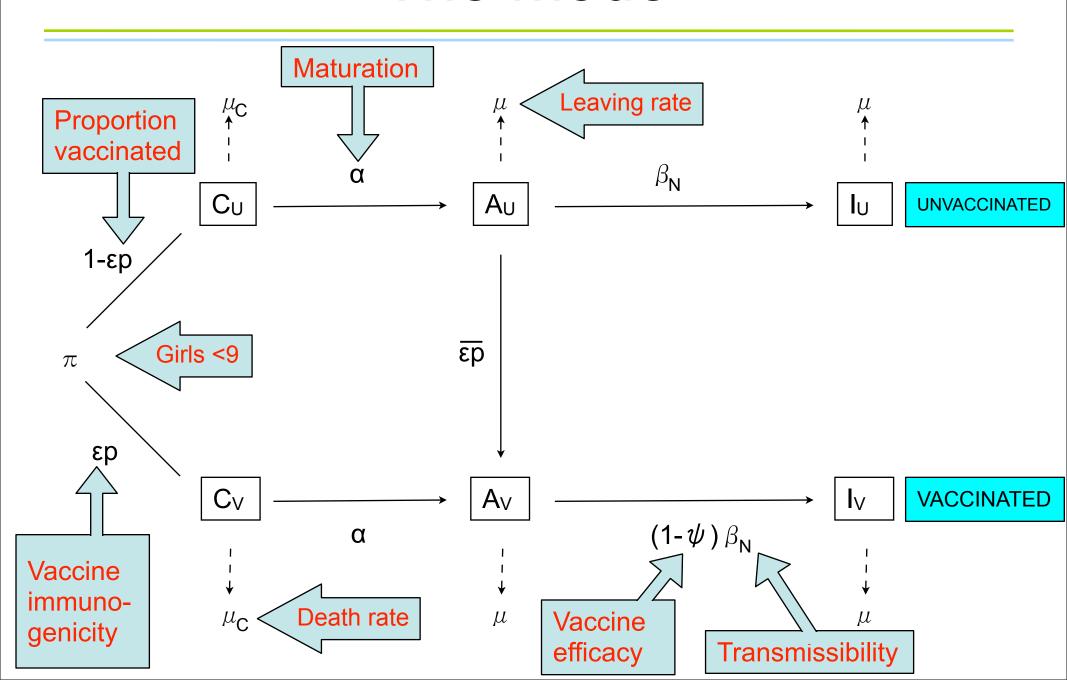
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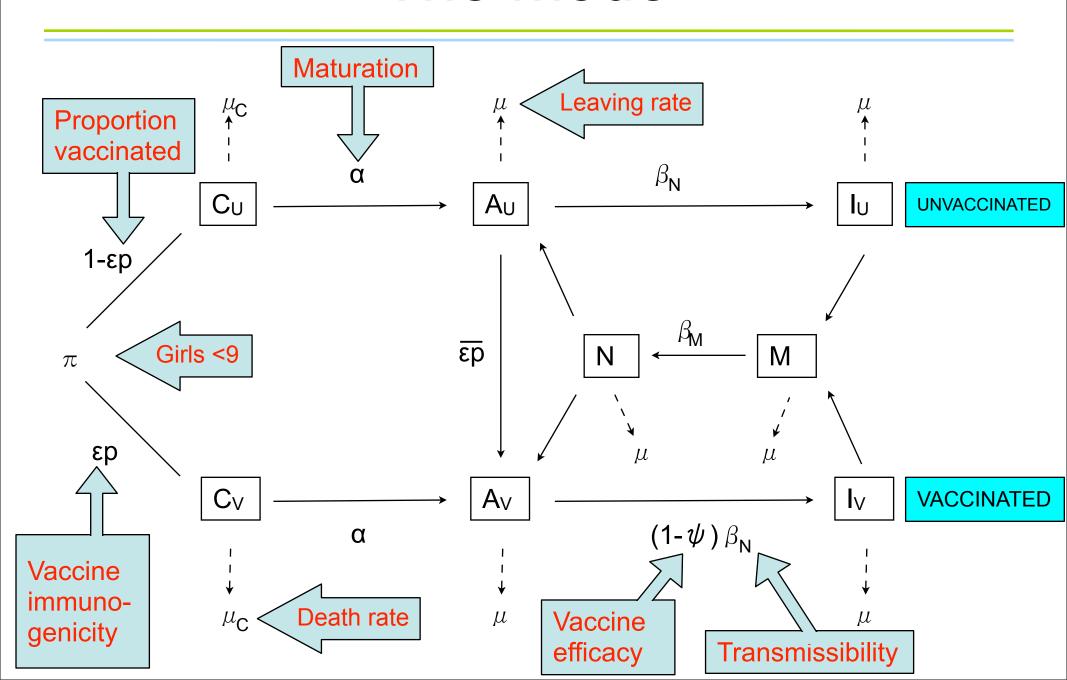


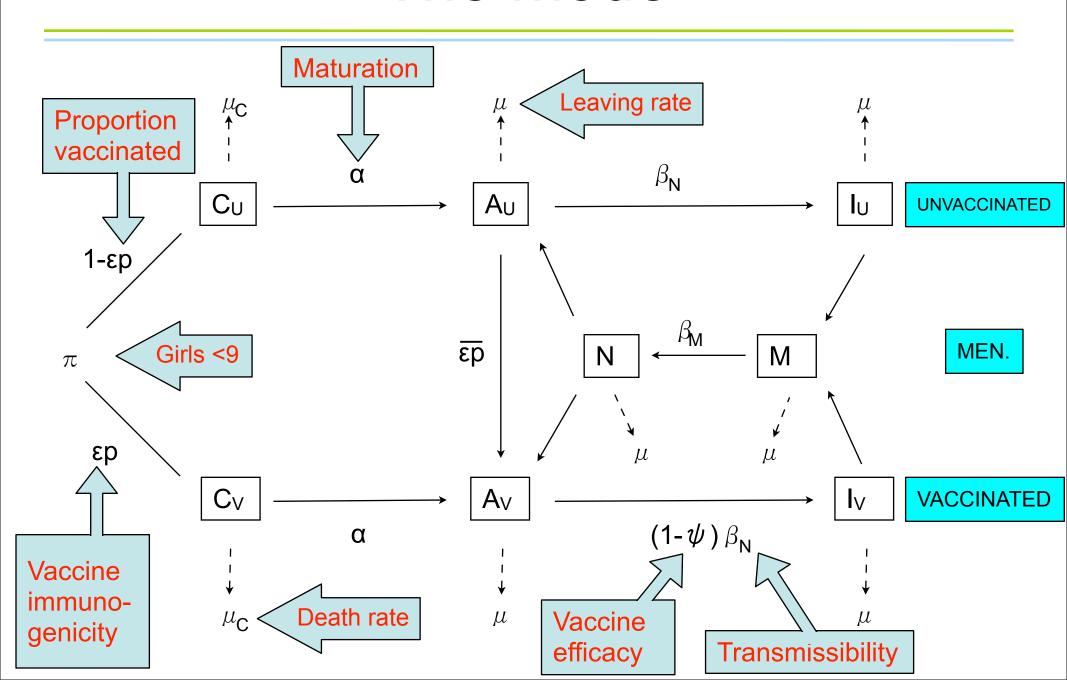
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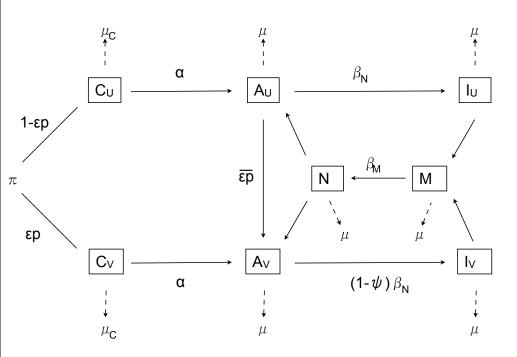




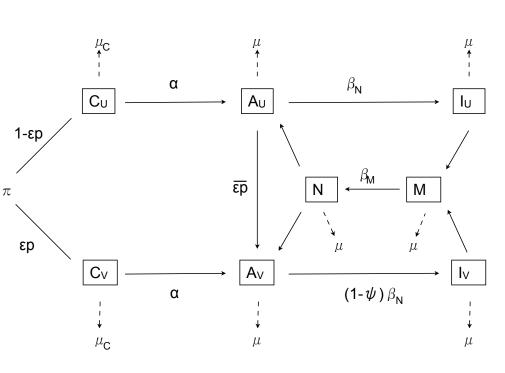




The ODEs



The ODEs



$$\frac{dC_U}{dt} = \pi_W (1 - \epsilon p) - \alpha C_U - \mu_C C_U$$

$$\frac{dC_V}{dt} = \pi_W \epsilon p - \alpha C_V - \mu_C C_V$$

$$\frac{dA_U}{dt} = \alpha C_U - f(\bar{\epsilon}\bar{p})A_U - \mu A_U - \beta_N A_U N$$

$$\frac{dA_V}{dt} = \alpha C_V + f(\bar{\epsilon}\bar{p})A_U - \mu A_V - (1 - \psi)\beta_N A_V N$$

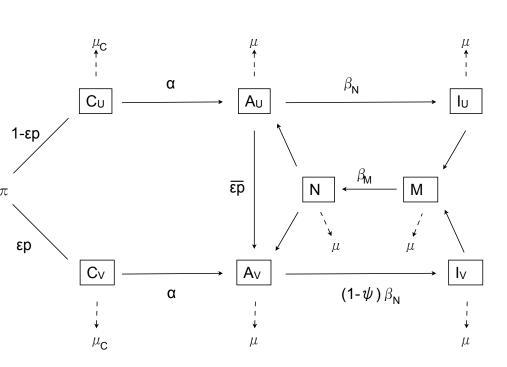
$$\frac{dI_U}{dt} = \beta_N A_U N - \mu I_U$$

$$\frac{dI_V}{dt} = (1 - \psi)\beta_N A_V N - \mu I_V$$

$$\frac{dM}{dt} = \pi_M - \beta_M I_U M - \mu M - \beta_M I_V M$$

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The ODEs



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Adult vaccination rate

The rate of vaccination of adults is

$$f(\bar{\epsilon}\bar{p}) = \frac{c\bar{\epsilon}\bar{p}}{1 - \bar{\epsilon}\bar{p} + \gamma}$$

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where c/γ is the maximum possible rate of vaccination, assuming perfect efficacy and immunogenicity

 This rate is zero if nobody is vaccinated and high (but not infinite) if everybody is.

Men do not get vaccinated

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- Children progress to the sexually active pool after 3 years

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- Children progress to the sexually active pool after 3 years
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- The vaccine may not confer 100% protection
- Overall prevalence matched the Canadian average (24%).

Disease-free equilibrium

The disease-free equilibrium is

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 C_j =children A_j =uninfected women I_j =infected adults M=uninfected men N=infected men π_M =boys π_W =girls ϵ =immunogenicity p=coverage α =maturation rate f=adult vaccination μ =leaving rate μ_C = childhood mortality

Disease-free equilibrium

The disease-free equilibrium is

$$\bar{C}_U = \frac{\pi_W(1-\epsilon p)}{\alpha+\mu_C} \qquad \bar{C}_V = \frac{\pi_W\epsilon p}{\alpha+\mu_C}$$

$$\bar{A}_U = \frac{\alpha C_U}{f+\mu} \qquad \bar{A}_V = \frac{\alpha C_V+fA_U}{\mu}$$

$$\bar{I}_U = 0 \qquad \bar{I}_V = 0$$

$$\bar{M} = \frac{\pi_M}{\mu} \qquad \bar{N} = 0$$

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Jacobian

The Jacobian at the disease-free equilibrium is

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$$J = \begin{bmatrix} -\mu_C - \alpha & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & -\mu_C - \alpha & 0 & 0 & 0 & 0 & 0 & 0 \\ \alpha & 0 & -f - \mu & 0 & 0 & 0 & 0 & -\beta_N A_U \\ 0 & \alpha & f & -\mu & 0 & 0 & 0 & -(1 - \psi)\beta_N A_V \\ 0 & 0 & 0 & 0 & -\mu & 0 & 0 & \beta_N A_U \\ 0 & 0 & 0 & 0 & 0 & -\mu & 0 & (1 - \psi)\beta_N A_V \\ 0 & 0 & 0 & 0 & -\beta_M M & -\beta_M M & -\mu & 0 \\ 0 & 0 & 0 & 0 & \beta_M M & \beta_M M & 0 & -\mu \end{bmatrix}$$

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Critical coverage threshold

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$$\epsilon p = \frac{1}{\psi \mu} \left[\mu + f(\bar{\epsilon}\bar{p})(1-\psi) - \frac{\mu^4(\mu + f(\bar{\epsilon}\bar{p}))(\alpha + \mu_C)}{\beta_M \beta_N \pi_M \pi_W \alpha} \right]$$

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Critical coverage threshold

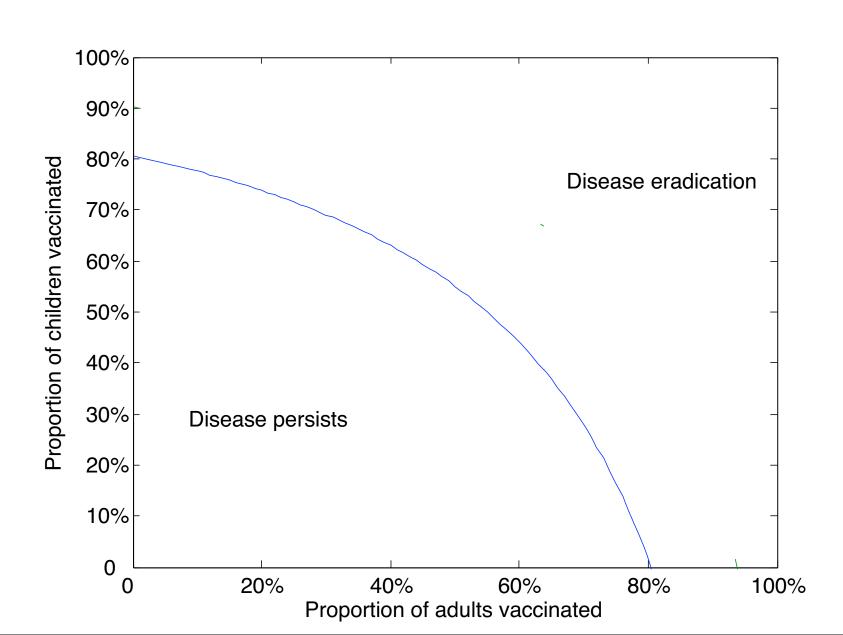
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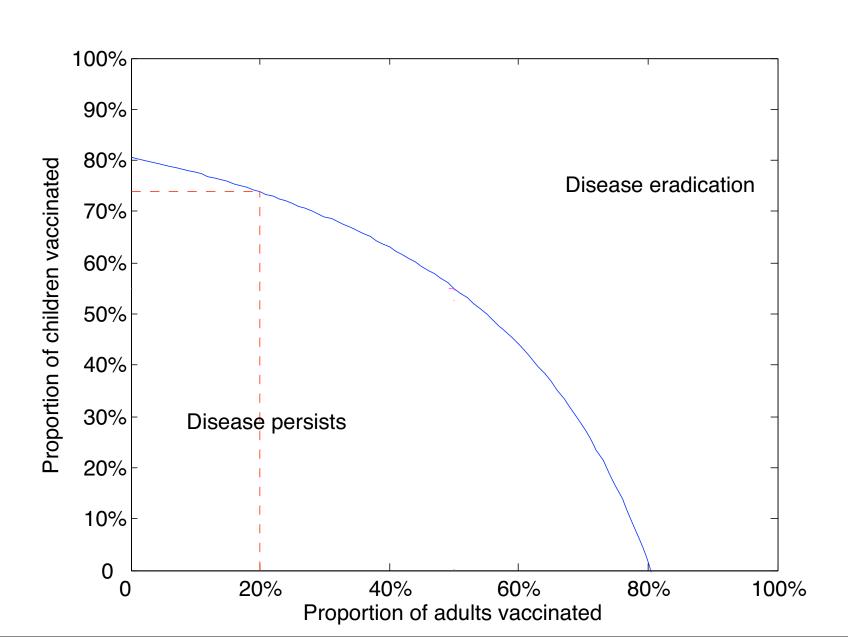
 If coverage exceeds this level, then we have eradication.

 π_M =boys π_W =girls ϵ =immunogenicity p=coverage β_j =transmission rate ψ =vaccine efficacy α =maturation rate f=adult vaccination μ =leaving rate μ_C = childhood mortality

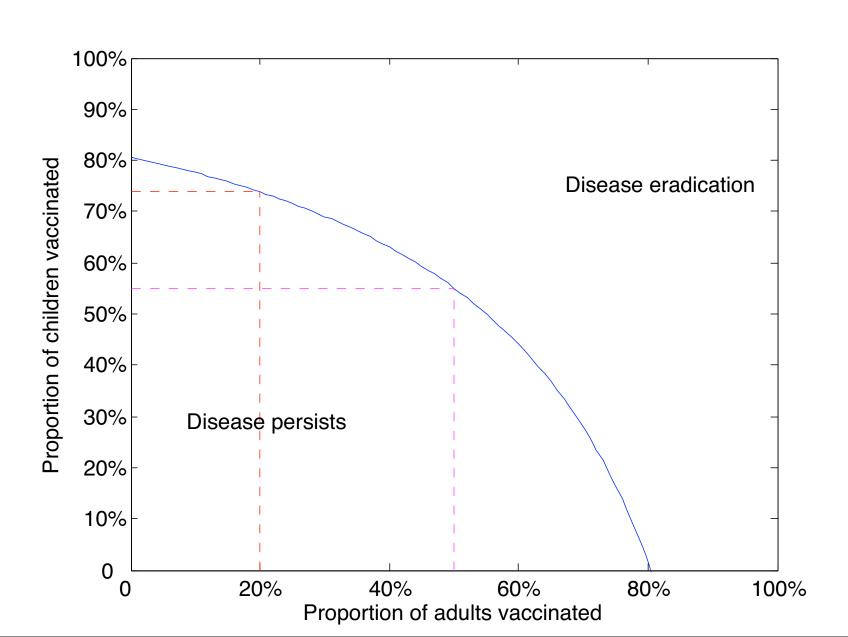
Results



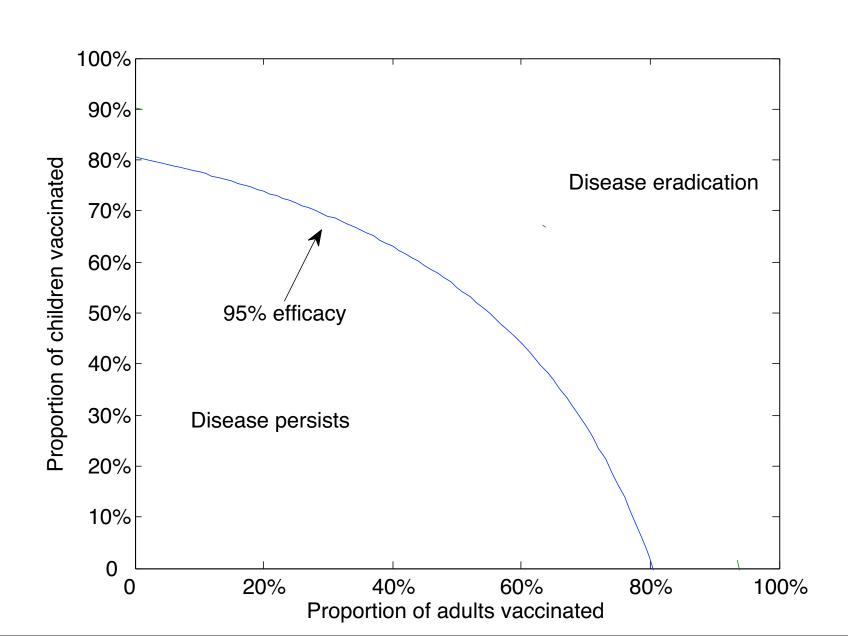
Results



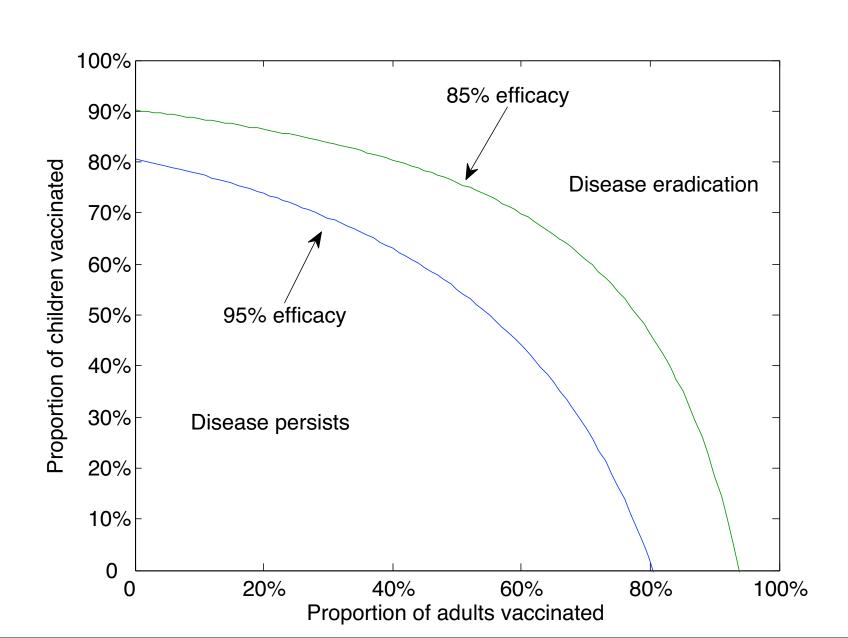
Results



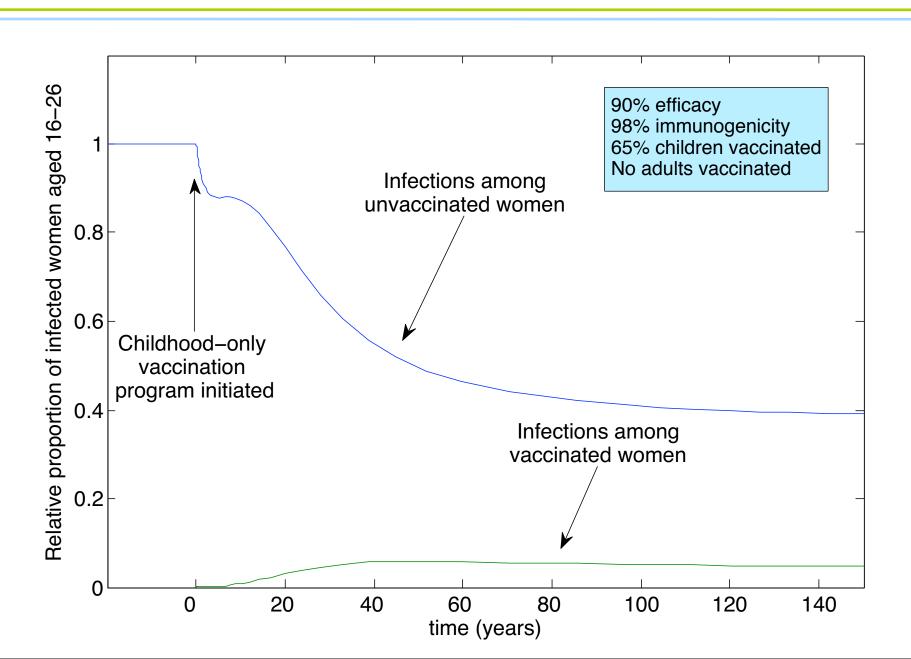
What happens as the efficacy decreases?



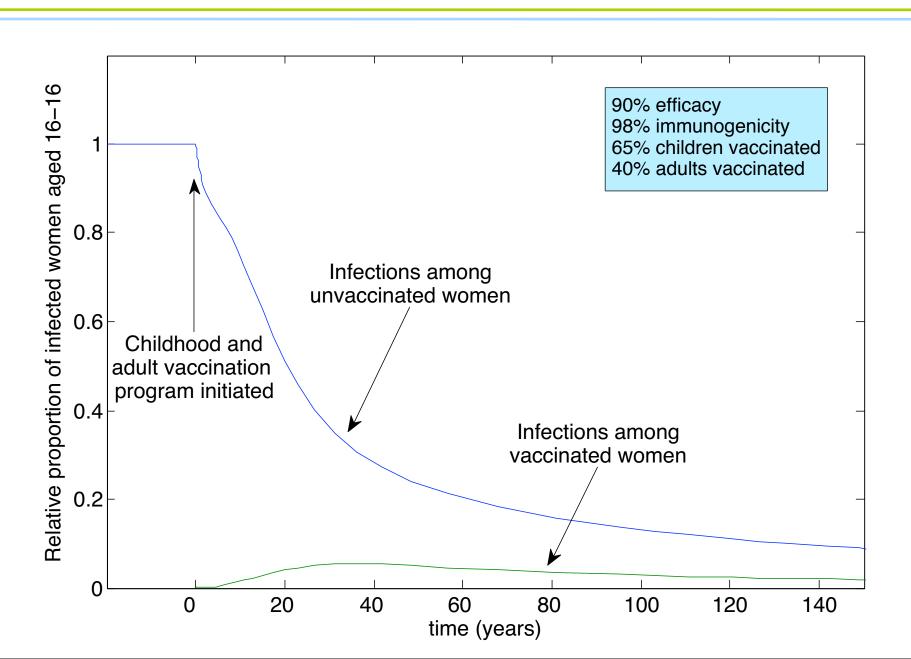
What happens as the efficacy decreases?



Vaccinating children vs both



Vaccinating children vs both



The vaccine efficacy might be suboptimal



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- The vaccine immunogenicity might be suboptimal

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(ie the vaccine might only create an antibody response a fraction of the time).

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$$\psi^* = 1 - \frac{\mu^4(\alpha + \mu_C)}{\beta_M \beta_N \pi_M \pi_W \alpha}$$

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 If the efficacy is lower than this critical value, then we can never have eradiation

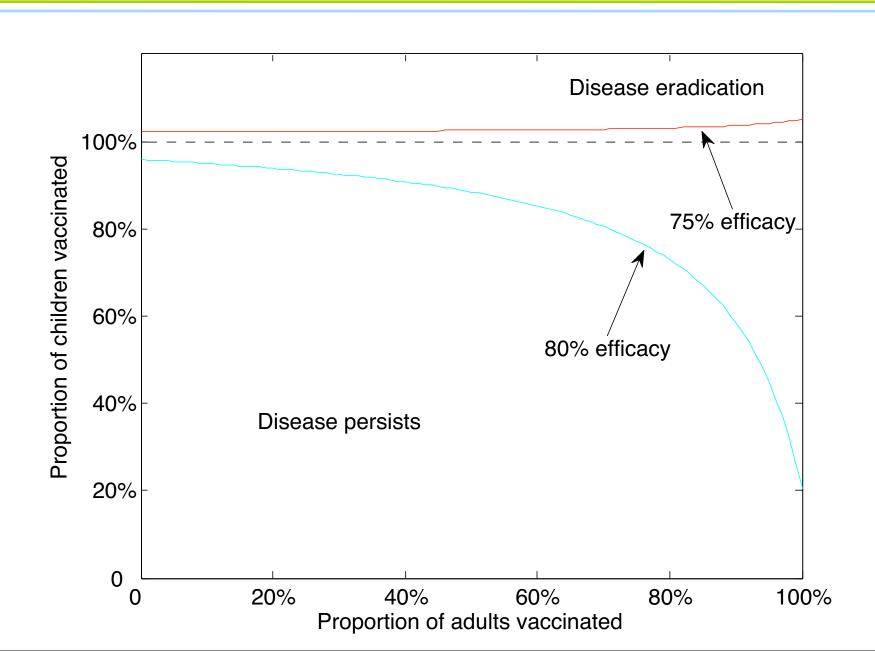
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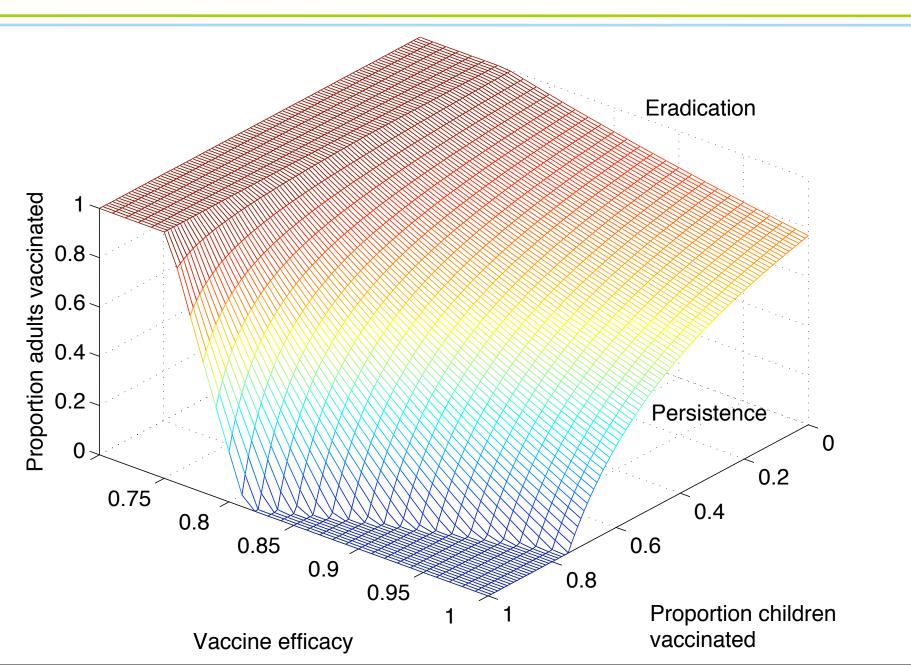
 If the efficacy is lower than this critical value, then we can never have eradiation (even if we had perfect coverage and the vaccine mounted a perfect immune response).

 π_{M} =boys π_{W} =girls ϵ =immunogenicity β_{j} =transmission rate ψ =vaccine efficacy α =maturation rate μ =leaving rate μ_{C} = childhood mortality

What if the vaccine has suboptimal efficacy?



Dependence on efficacy



Critical immunogenicity

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$$\epsilon^* = \frac{1}{\psi} \left[1 - \frac{\mu^4(\alpha + \mu_C)}{\beta_N \beta_M \pi_M \pi_W \alpha} \right]$$

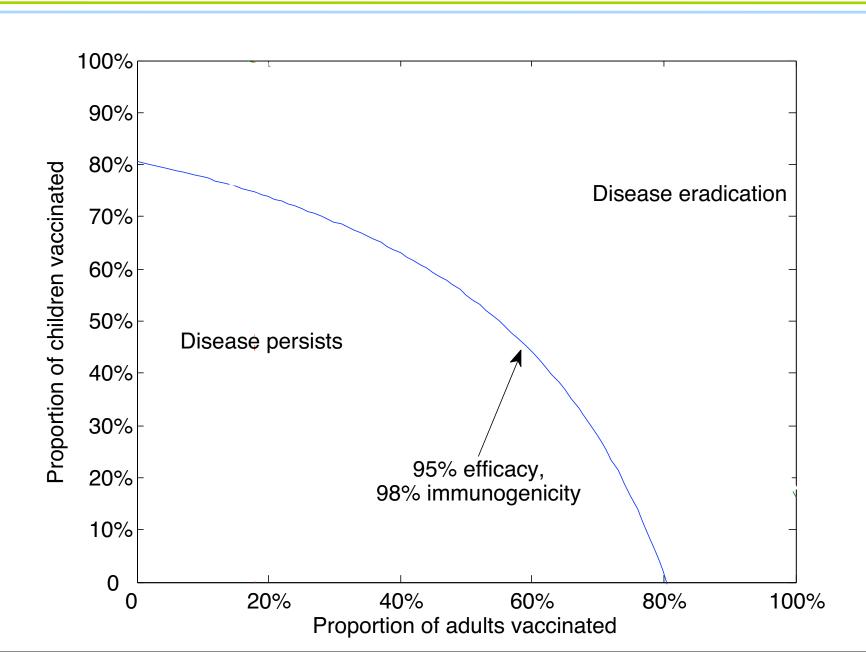
Critical immunogenicity

The critical immunogenicity is

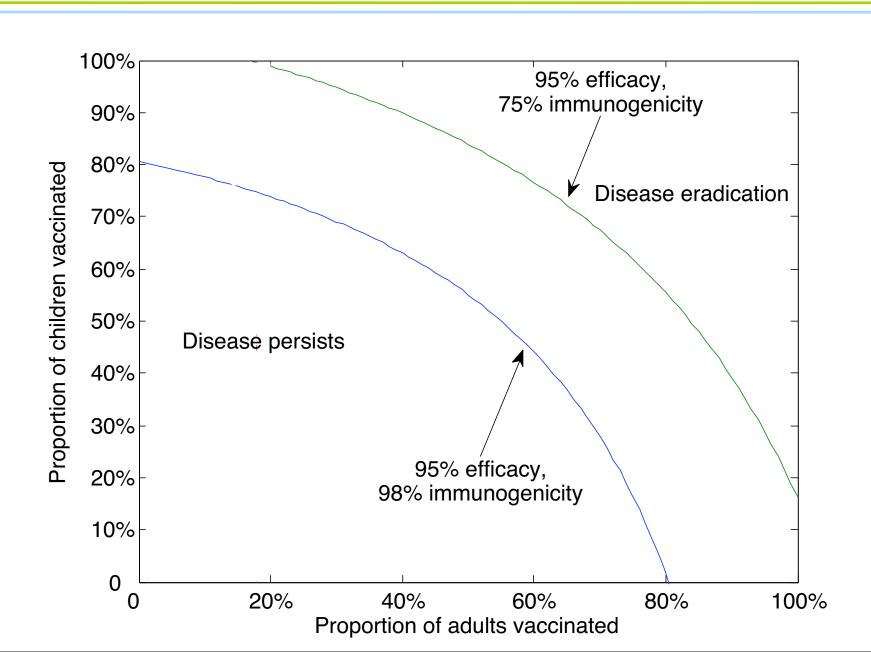
$$\epsilon^* = \frac{1}{\psi} \left[1 - \frac{\mu^4(\alpha + \mu_C)}{\beta_N \beta_M \pi_M \pi_W \alpha} \right]$$

 If the imunogenicity is less than this, then even 100% childhood vaccination will not lead to eradication.

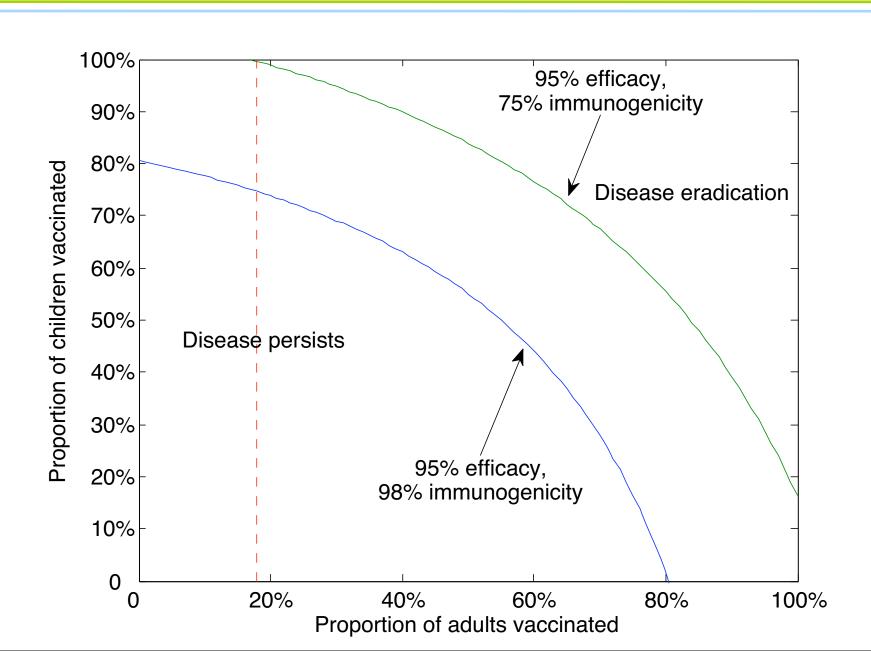
What if the vaccine has suboptimal immunogenicity?



What if the vaccine has suboptimal immunogenicity?



What if the vaccine has suboptimal immunogenicity?



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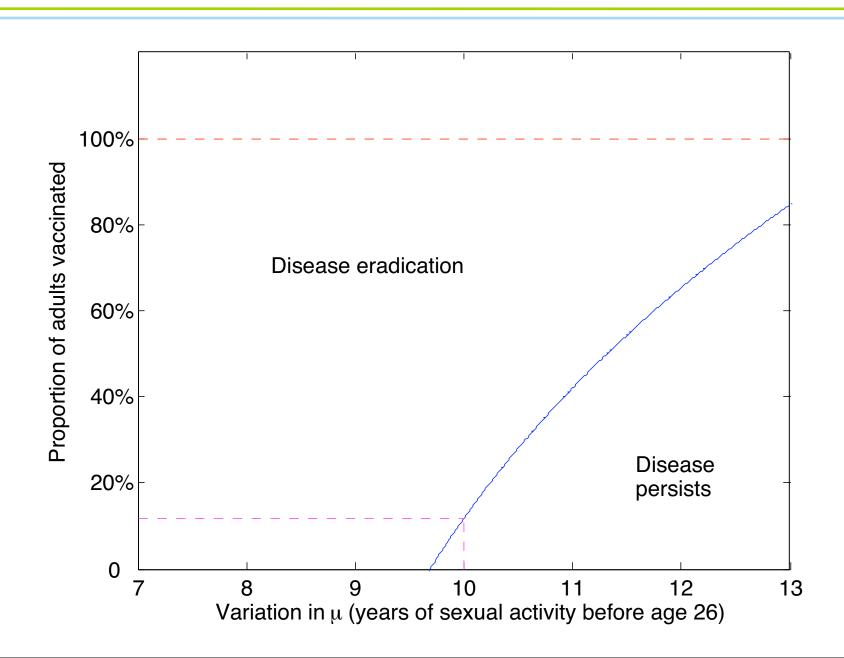
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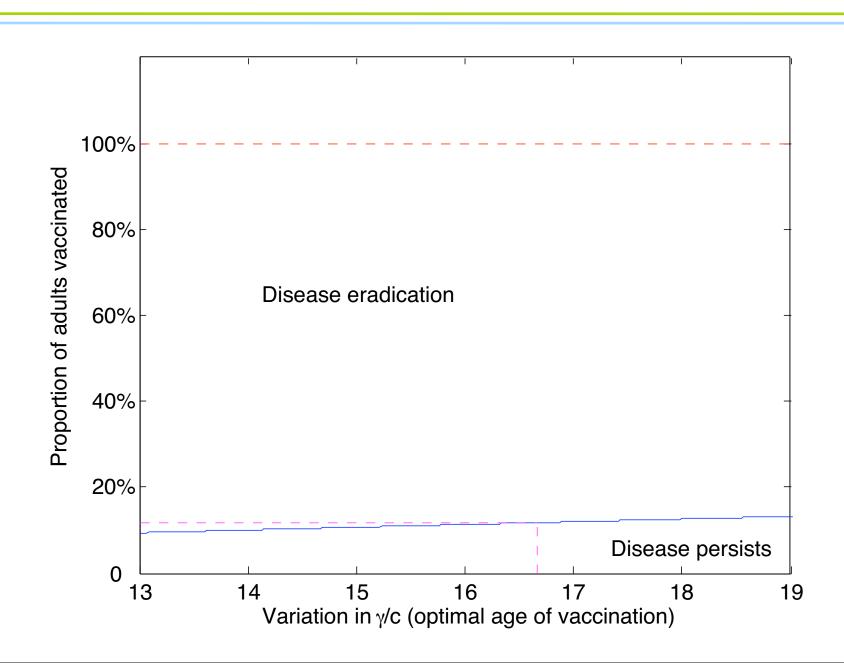
- How do the results depend on our other parameters?
- We varied the
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 - years of survival from childhood

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- We varied the
 - years of sexual activity before age 26
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 - years of survival from childhood
- Our output variable was the proportion of adults needing to be vaccinated, assuming 77% childhood vaccination.

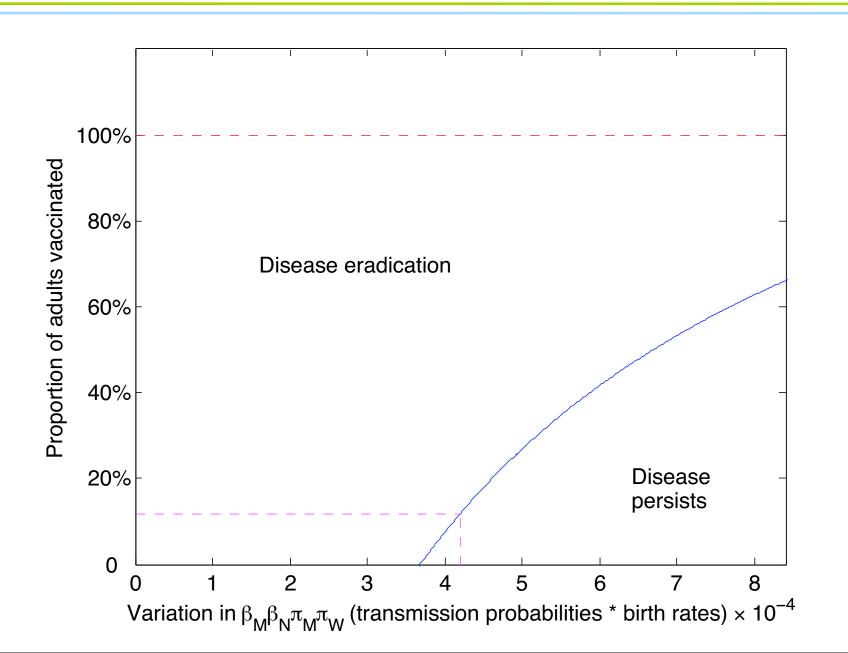
Dependence on years of sexual activity



Dependence on the optimal age of vaccination

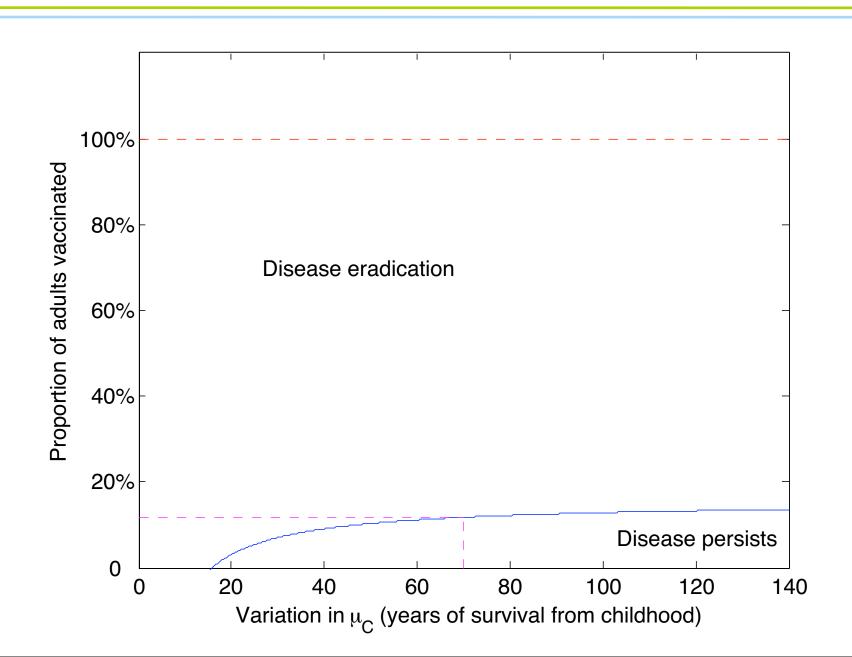


Dependence on the transmission and birth rates



Proportion of adults vaccinated

Dependence on years of survival since childhood





Using this model, we determined

A threshold for eradication of the disease



- A threshold for eradication of the disease
- The amount of vaccination for a childhoodonly program



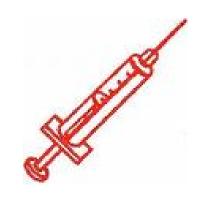
- A threshold for eradication of the disease
- The amount of vaccination for a childhoodonly program
- The amount by which childhood-only vaccination will be offset by adult vaccination



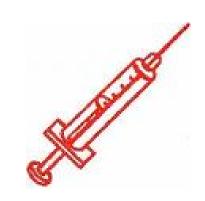
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- Dependence upon the

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- A threshold for eradication of the disease
- The amount of vaccination for a childhoodonly program
- The amount by which childhood-only vaccination will be offset by adult vaccination
- Dependence upon the
 - vaccine efficacy
 - vaccine immunogenicity
 - all other parameters.



Eradication of HPV is feasible

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- Childhood vaccination programs should be supplemented by adult vaccination
- There is a critical vaccine efficacy (77%) below which eradication is not possible
- There is a critical vaccine immunogenicity (80%) below which even 100% childhood vaccination cannot eradicate the epidemic.

Recommendation

 Recall that vaccination rates in Ontario are at 53%



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- This is less than required for eradication (>80%) if only children are to be vaccinated



Recommendation

- Recall that vaccination rates in Ontario are at 53%
- This is less than required for eradication (>80%) if only children are to be vaccinated
- Thus, voluntary adult vaccination should be covered by Canadian health care.



Key references

- M. Al-arydah and R.J. Smith? (2011) An age-structured model of human papillomavirus vaccination (Mathematics and Computersin Simulation 82:629-642)
- M. Llamazares and R.J. Smith? (2008) Evaluating human papillomavirus vaccination programs in Canada: should provincial healthcare pay for voluntary adult vaccination? (BMC Public Health 8:114).

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