

# Lizards and Lyme disease risk



- Diana Erazo
- Luisa Carrillo Rodriguez
- Marilia Palumbo Gaiarsa
- Paula Ribeiro Prist
- Rodrigo Mazzei Carvalho

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- [2. Lyme disease](#)
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- [Numerical integration in R](#)
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### Group 2

## Lizards and Lyme disease risk

Wiki site of the practical exercise of the [III Southern-Summer School on Mathematical Biology](#).

Here you will find the exercise assignment and the group's products.

If you are a group member login to edit this page, create new pages from it, and upload files.

### Group

- [Carvalho, Rodrigo Mazzei; Federal University of Bahia, Biology Institute, Brazil](#)
- [Castro, Danielle; University of São Paulo, School of Public Health, Brazil](#)
- [Erazo, Diana; BIOMAC, Universidad de los Andes, Colombia](#)
- [Gaiarsa, Marília Palumbo; University of São Paulo, Ecology Department, Brazil](#)
- [Prist, Paula Ribeiro; University of São Paulo, Ecology Department, Brazil](#)
- [Rodriguez Carrillo, Luisa Fernanda; National University of Colombia, Mathematics Dept., Colombia](#)

### Assistants

- [Bruno Pace](#)
- [Renato Coutinho](#)

2014:groups:g2:start

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- Castro, Danielle
- Eraza, Diana
- Gaiarsa, Marilia
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*Proc. R. Soc. B*  
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# Impact of the experimental removal of lizards on Lyme disease risk

Andrea Swei<sup>1,\*</sup>, Richard S. Ostfeld<sup>2</sup>, Robert S. Lane<sup>3</sup>  
and Cheryl J. Briggs<sup>4</sup>

<sup>1</sup>*Department of Integrative Biology, University of California, 3060 Valley Life Sciences Building, Berkeley, CA 94720-3140, USA*

<sup>2</sup>*Cary Institute of Ecosystem Studies, Millbrook, NY 12545-0129, USA*

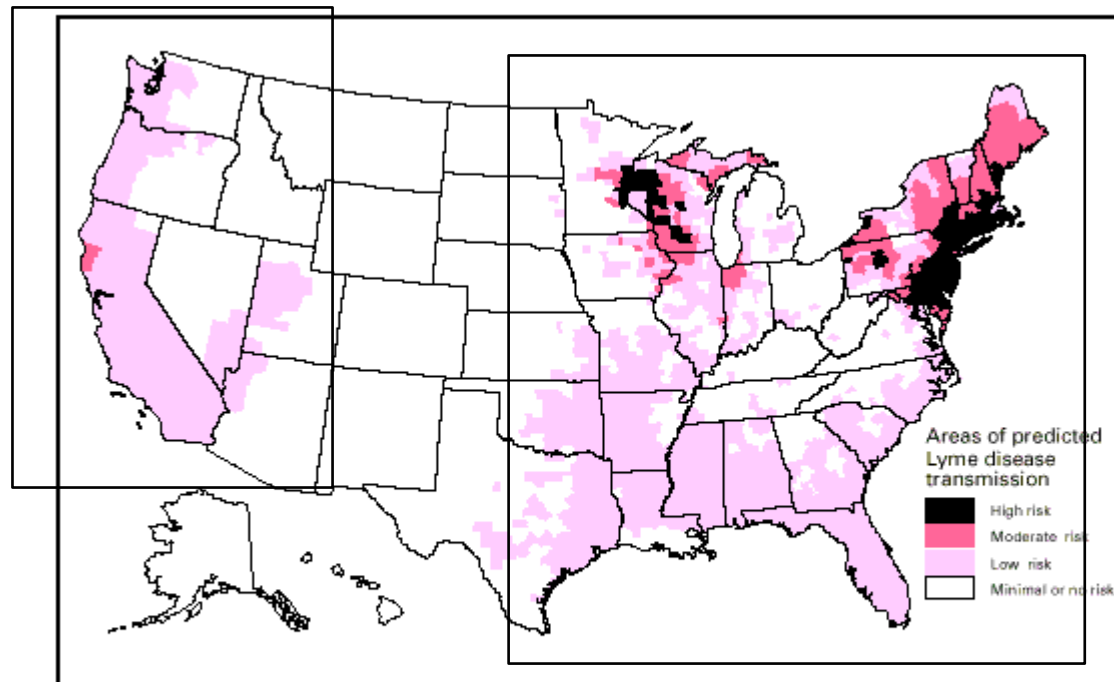
<sup>3</sup>*Department of Environmental Science, Policy and Management, University of California, Berkeley, CA 94720, USA*

<sup>4</sup>*Department of Ecology, Evolution, and Marine Biology, University of California, Santa Barbara, CA 93106-9610, USA*



# Introduction

It is an important public health issue in the US, where it is the most common vector-borne disease

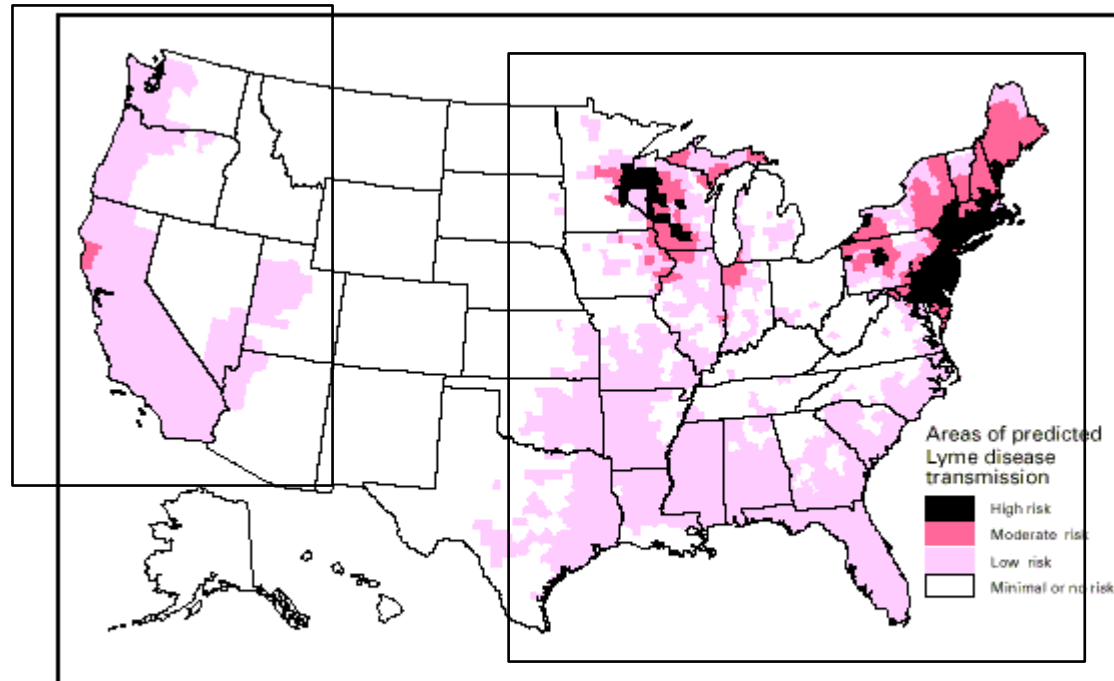


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Western black-legged tick (*Ixodes pacificus*)



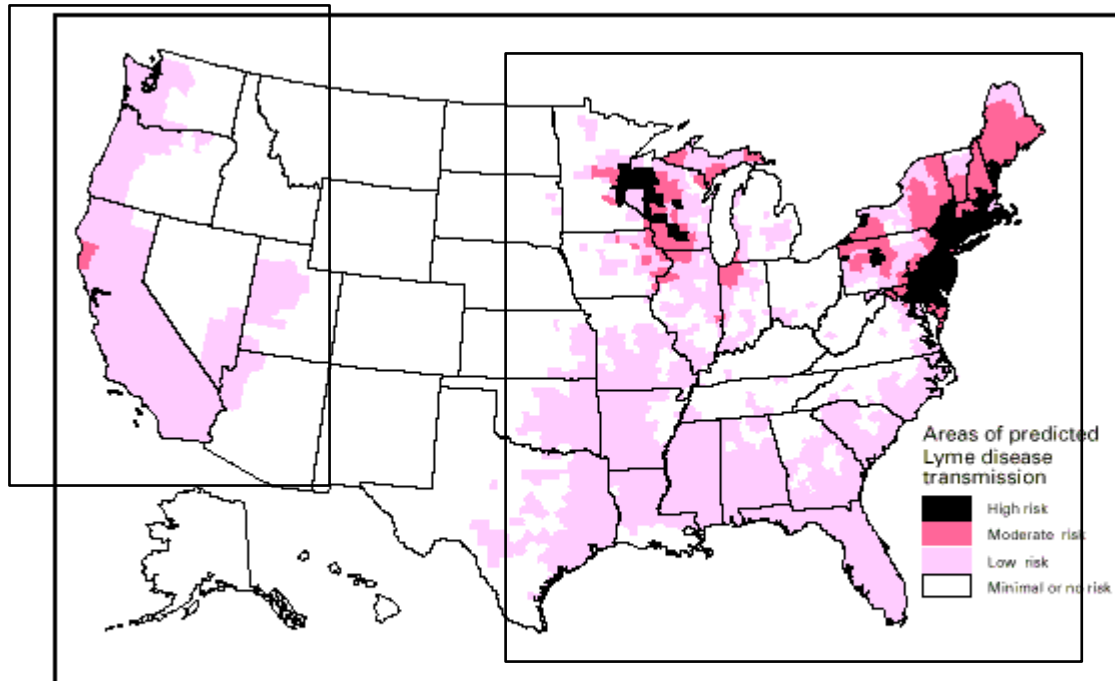
Black-legged tick (*Ixodes scapularis*)

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It's transmitted to humans through ticks' bites



Black-legged tick (*Ixodes scapularis*)

# Introduction

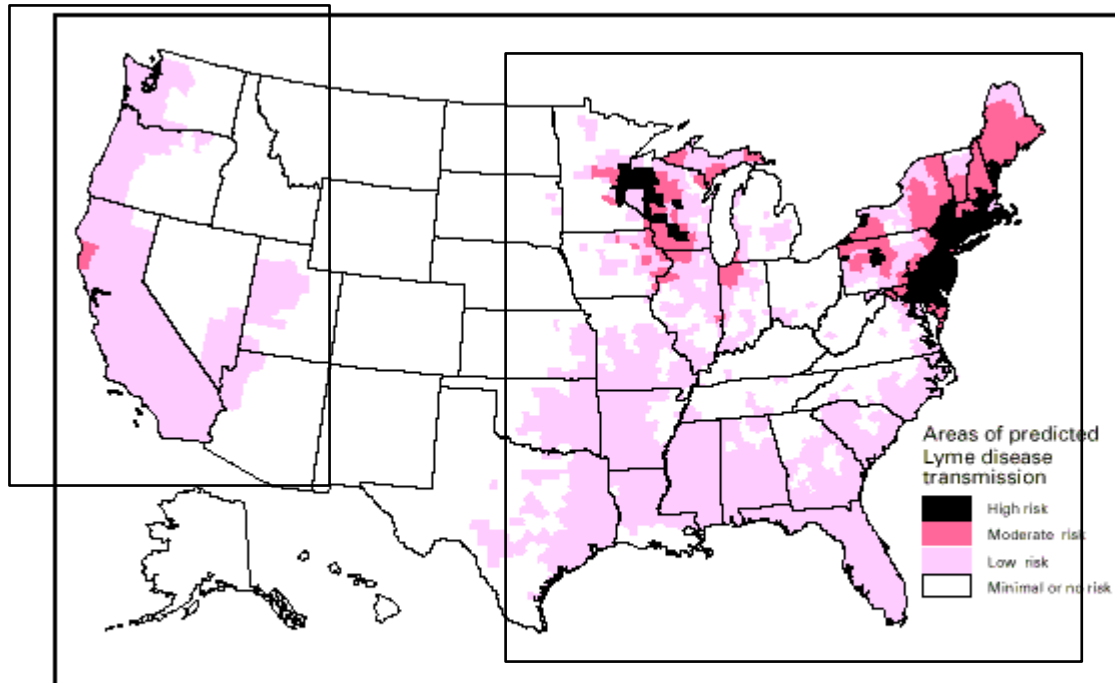
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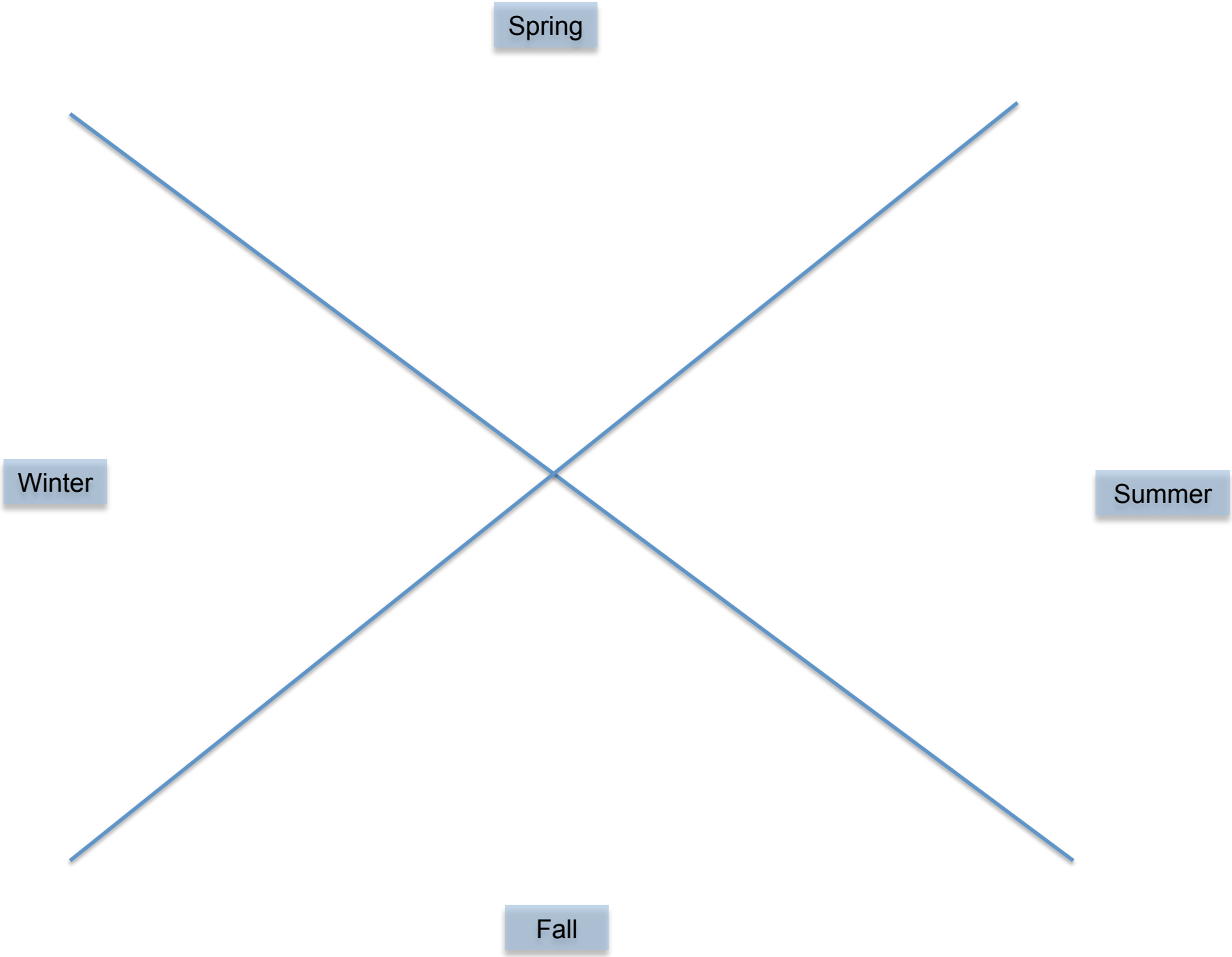
*Borrelia burgdorferi*



It's transmitted to humans through ticks' bites



Black-legged tick (*Ixodes scapularis*)





Spring



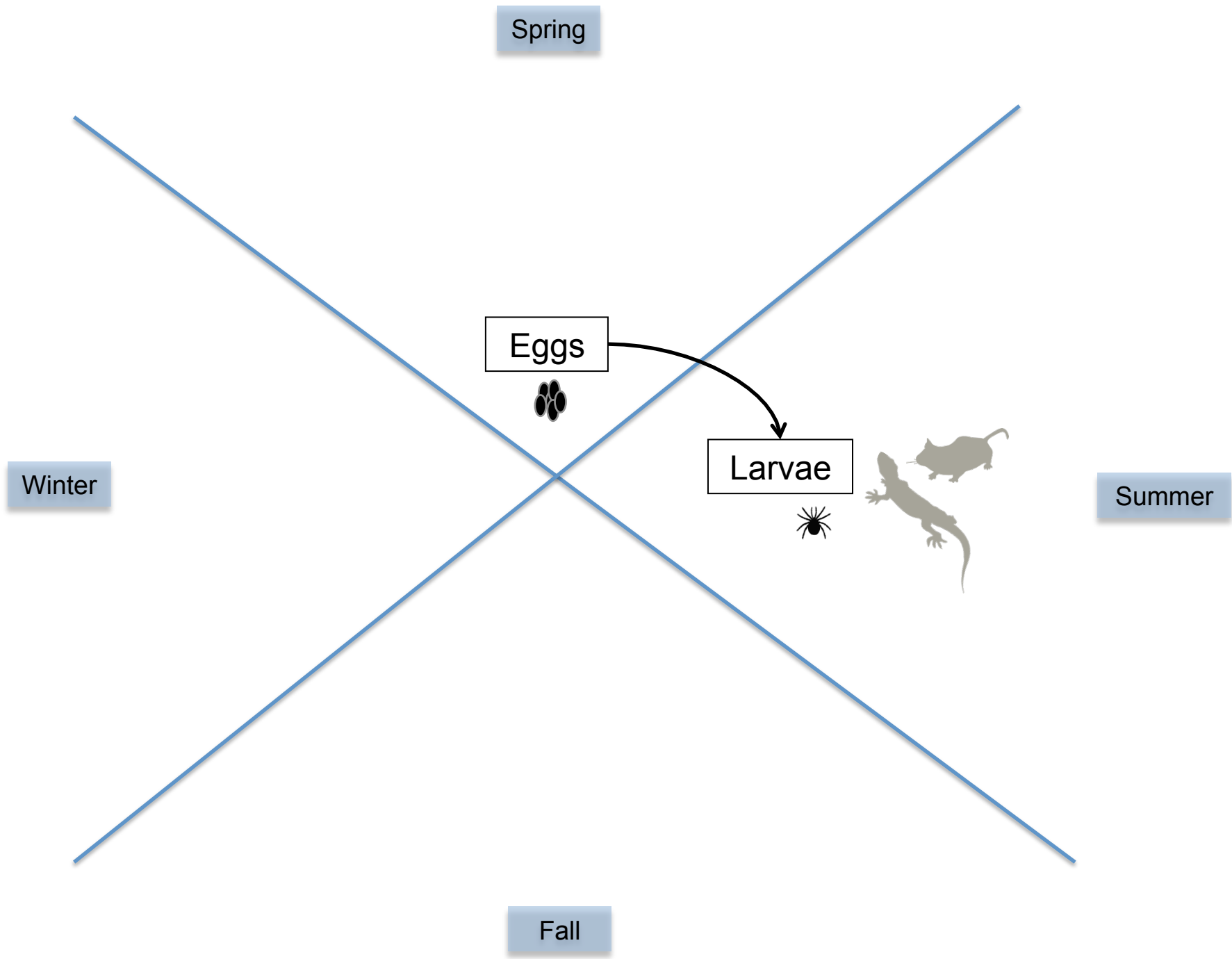
Eggs

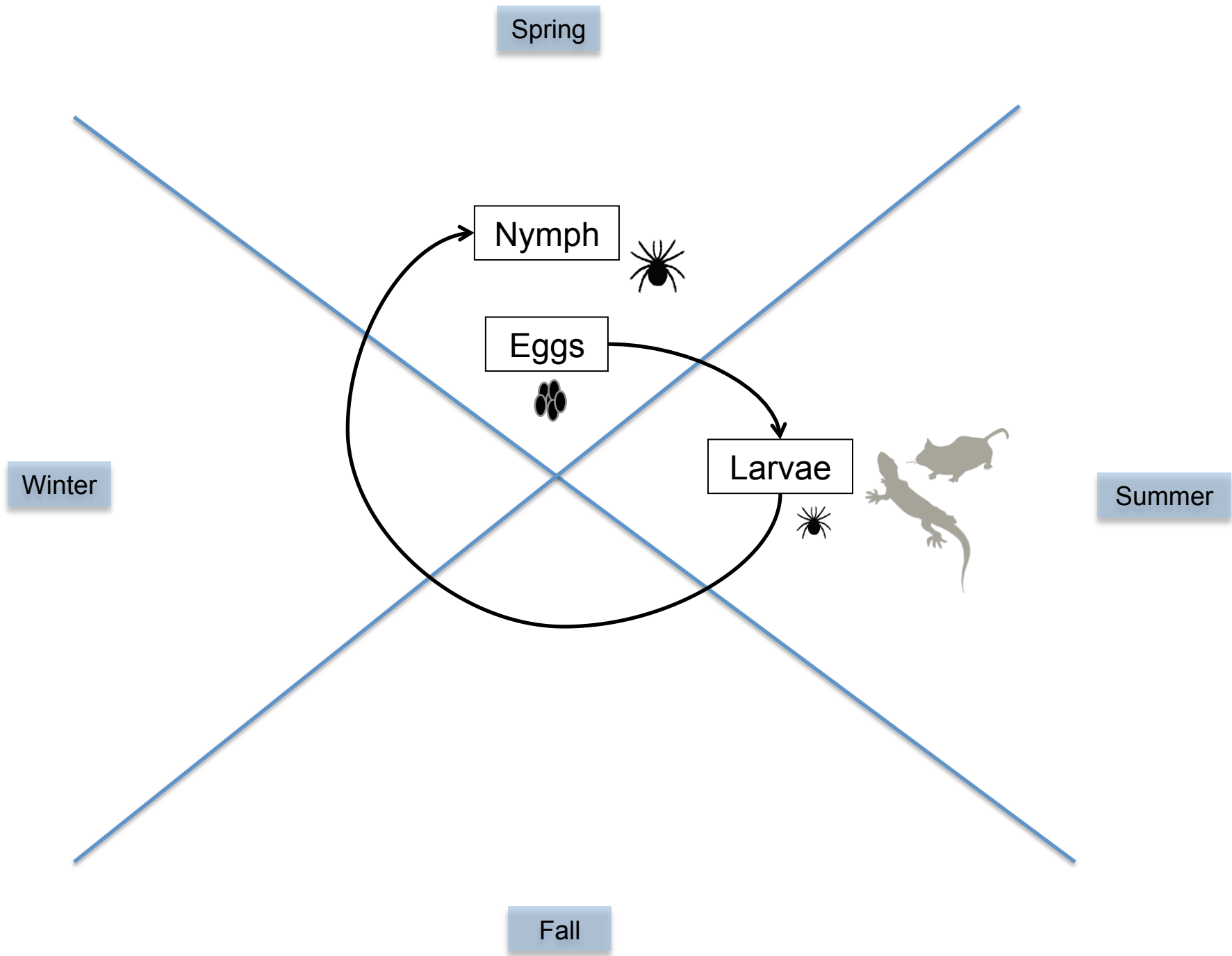


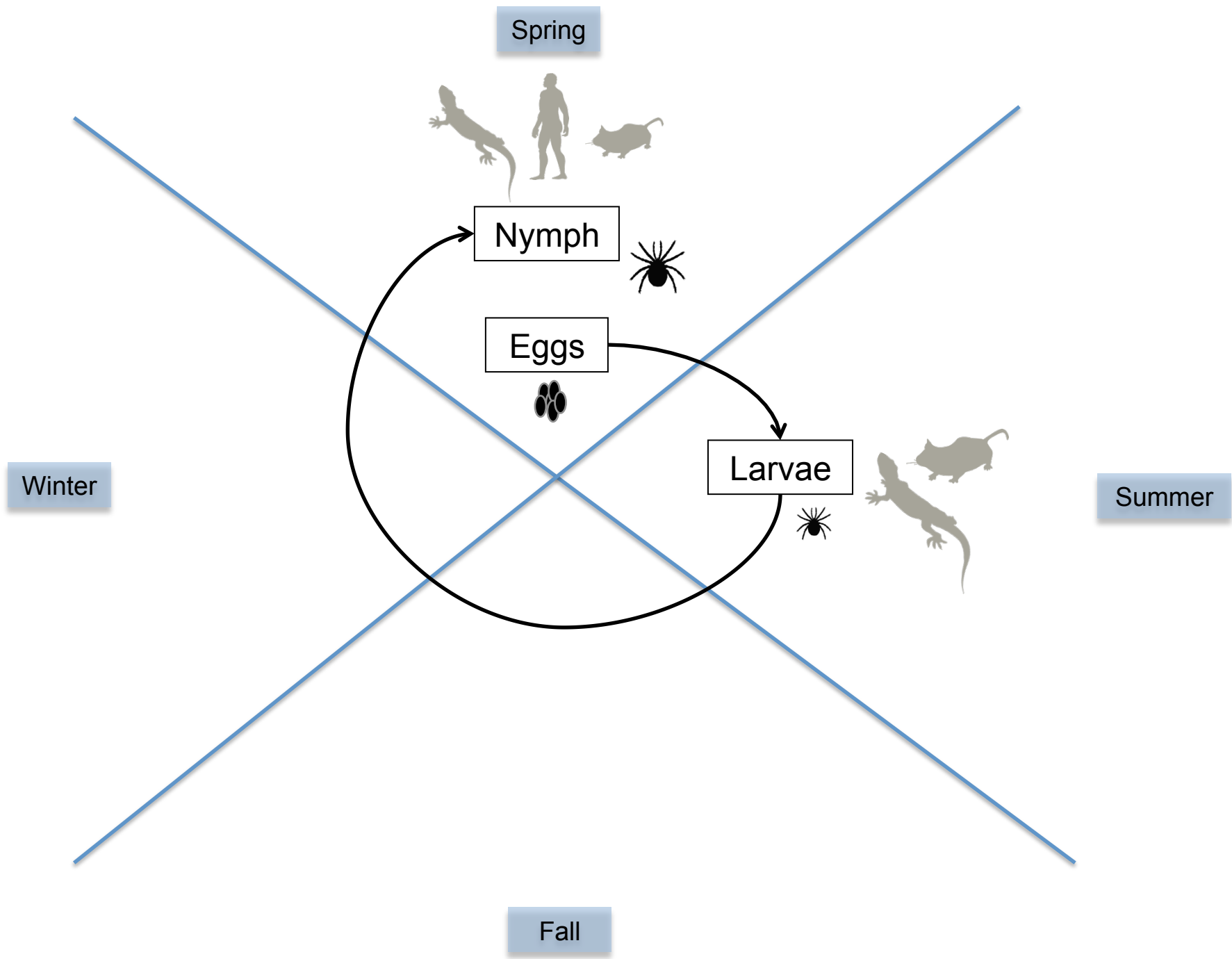
Winter

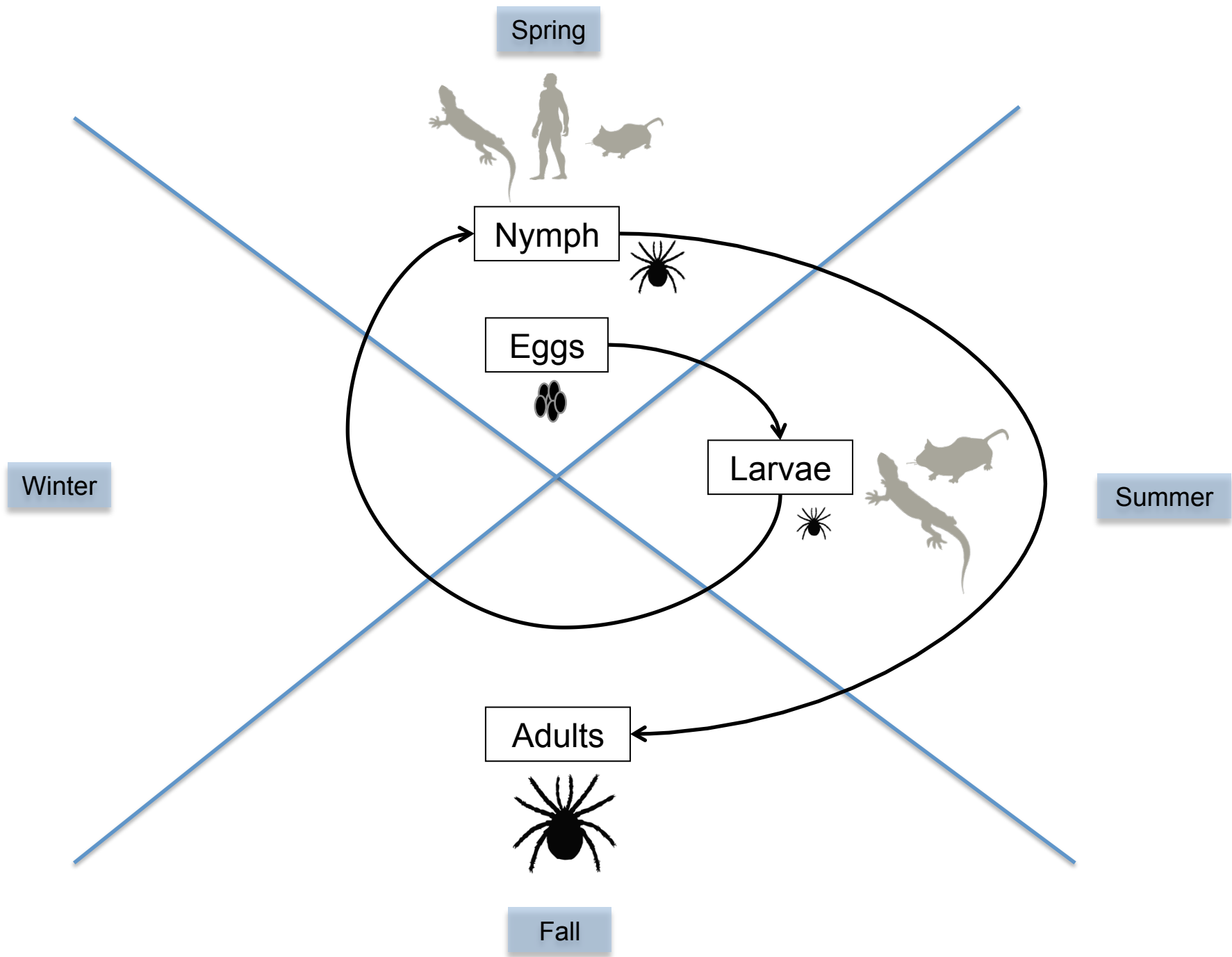
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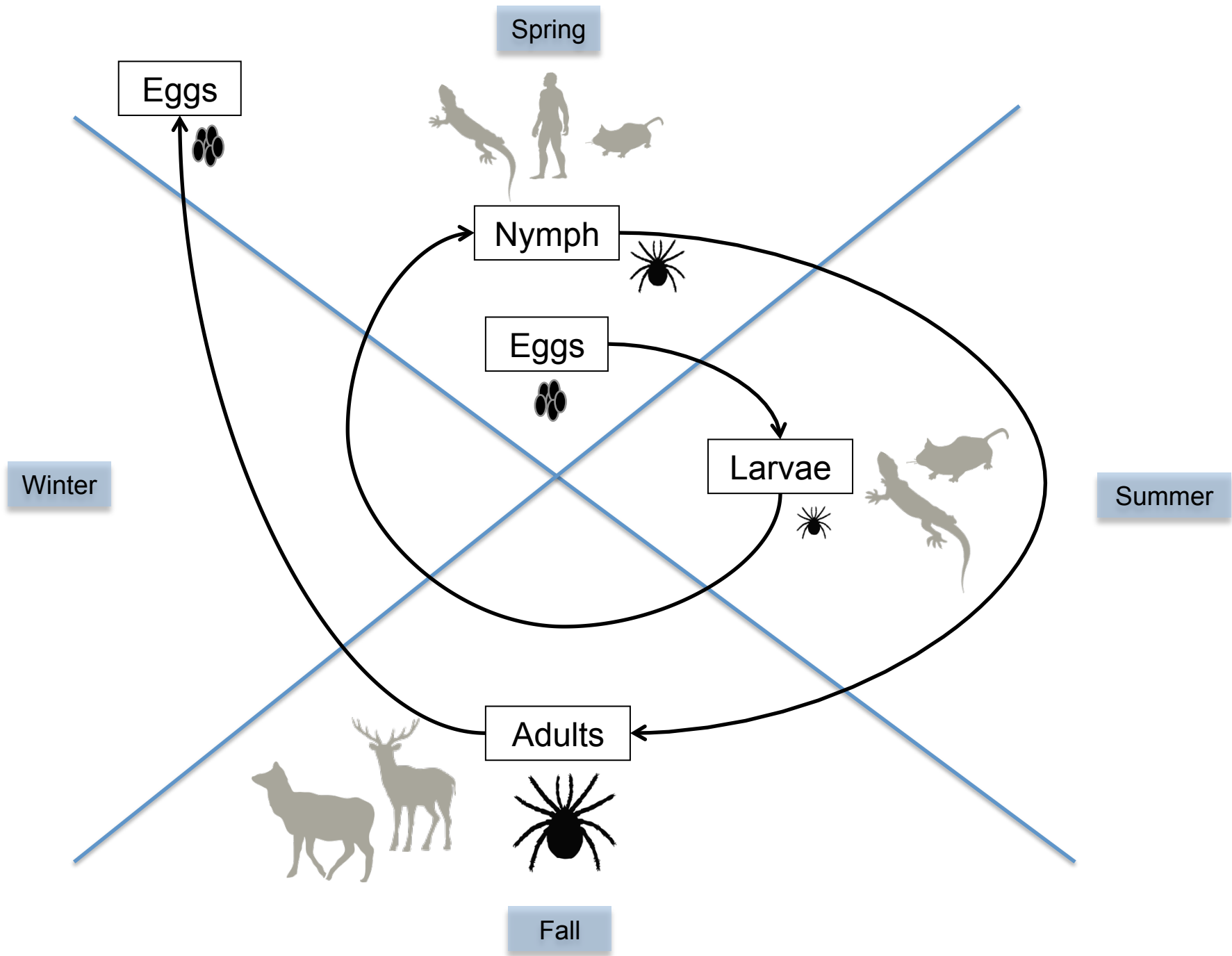
Fall

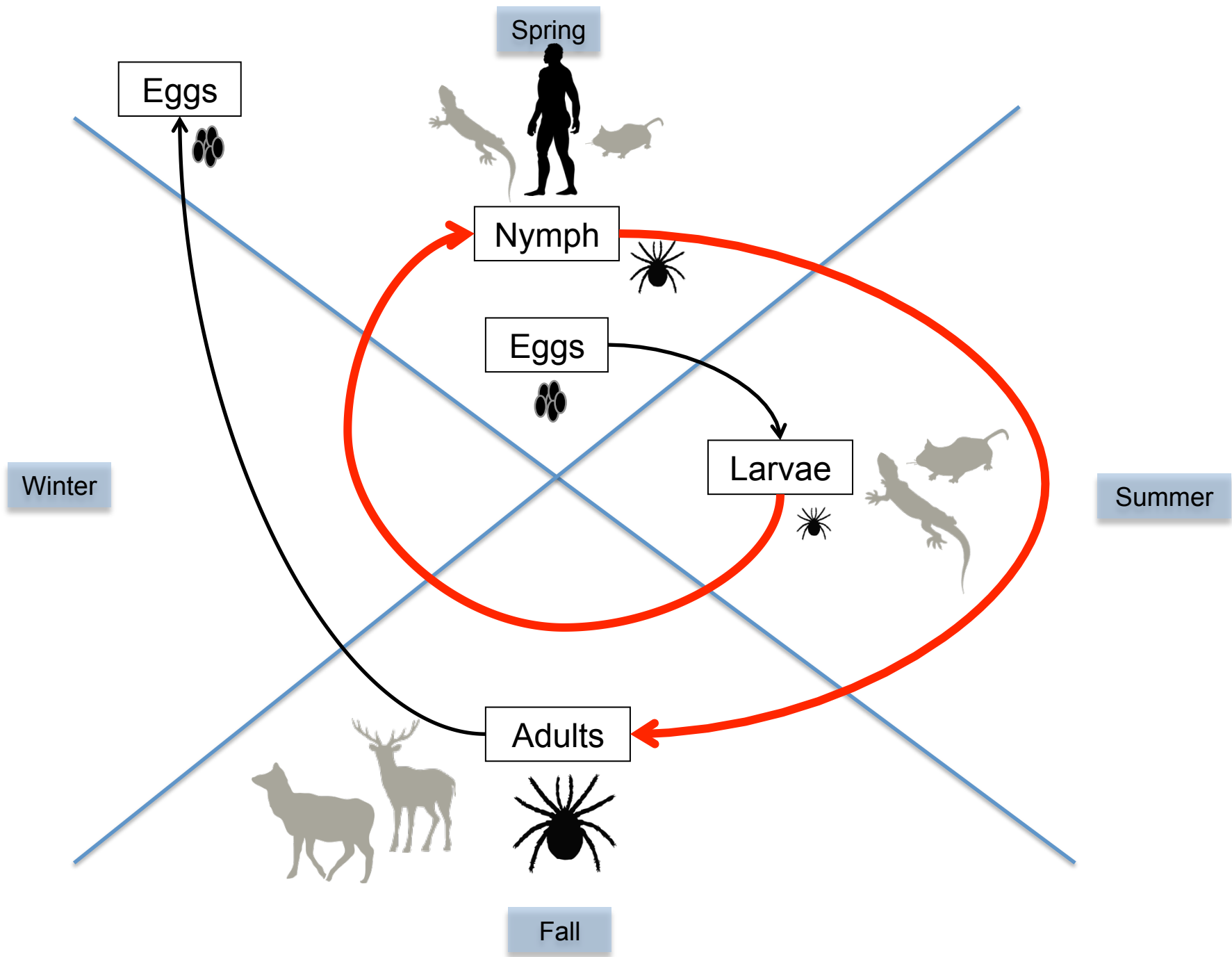










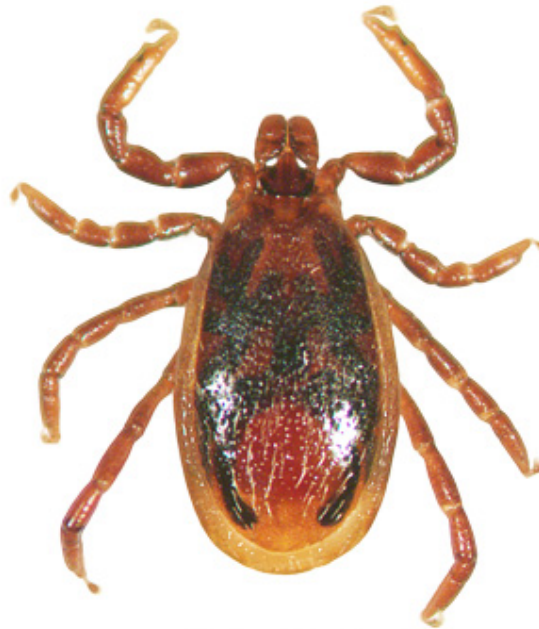




Larva



Nymph



Adult Male



Adult Female





# Hosts

*Sceloporus occidentalis*



## Hosts

Dusky-footed Woodrat  
(*Neotoma fuscipes*)



Deer Mouse  
(*Peromyscus maniculatus*)

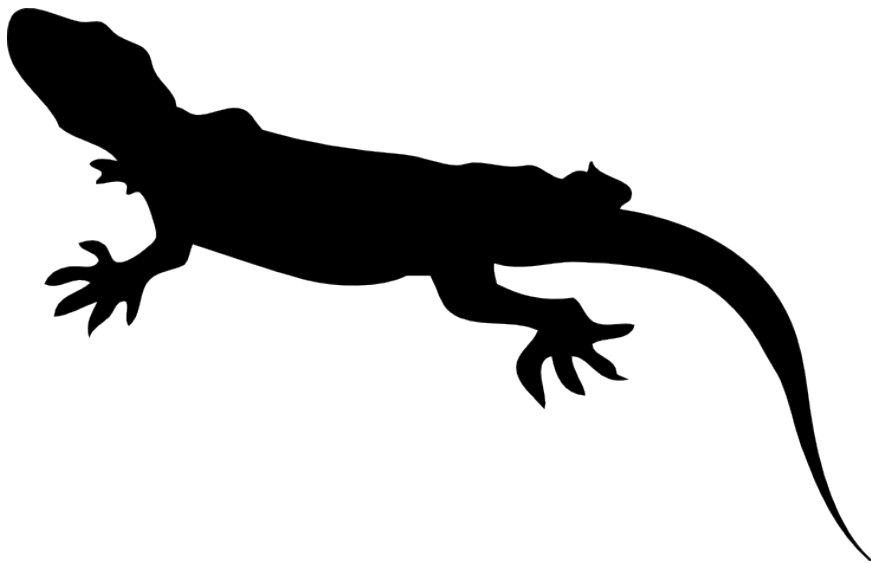


California Kangaroo Rat  
(*Dipodomys californicus*)

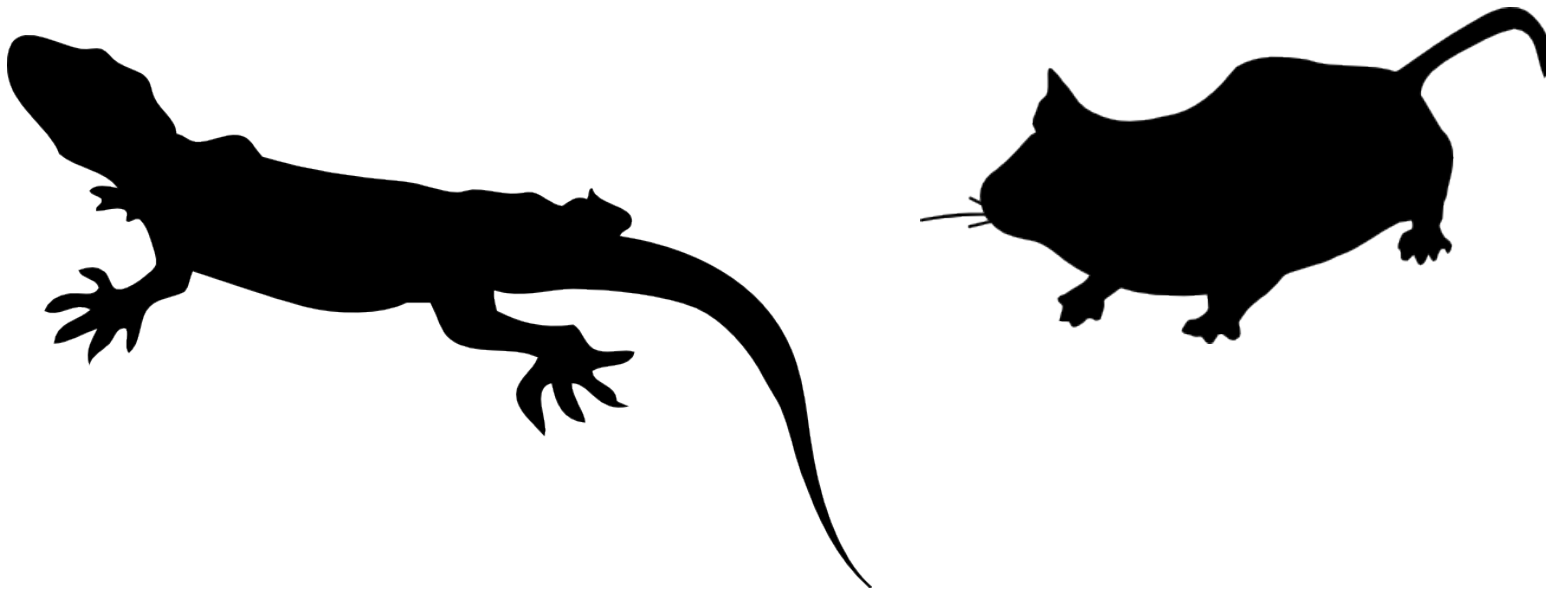


Western Grey Squirrel  
(*Sciurus griseus*)





**Host competence:** ability to sustain the tick population.



**Host competence:** ability to sustain the tick population.

**Reservoir competence:** ability of an infected host to infect a tick.



## Host competence



## Host competence



## Host competence



Lizards hold up to 90 % of the ticks



## Reservoir competence



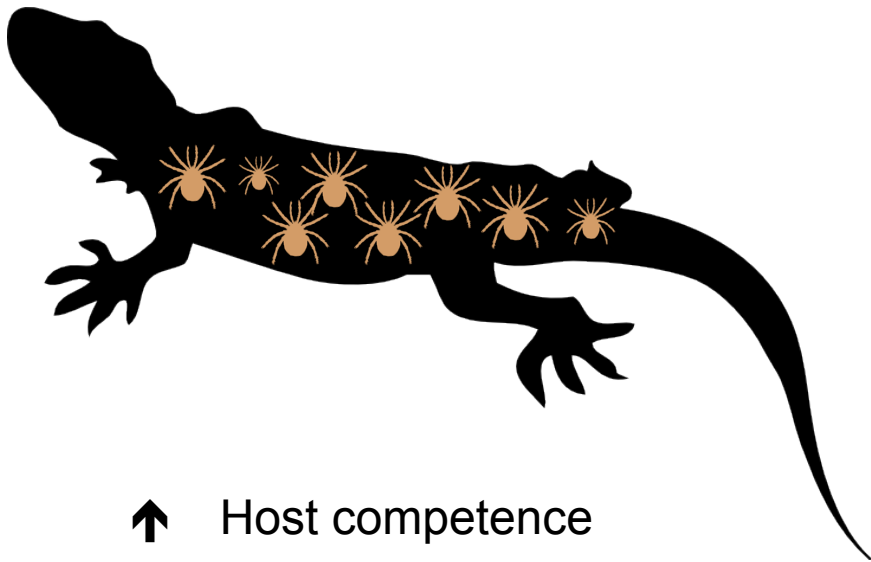
## Reservoir competence



Susceptible tick

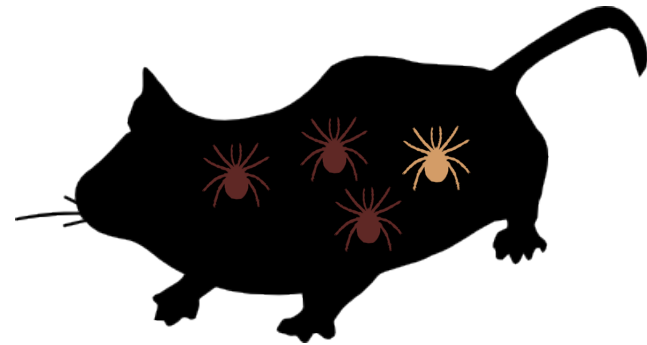


Infected tick



↑ Host competence

↓ Reservoir competence



↓ Host competence

↑ Reservoir competence

# Objectives

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## **Impact of the experimental removal of lizards on Lyme disease risk**

**Andrea Swei<sup>1,\*</sup>, Richard S. Ostfeld<sup>2</sup>, Robert S. Lane<sup>3</sup>  
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# Objectives

To assess the impacts of experimentally reduced western fence lizard density on abundance and infection prevalence of *Ixodes pacificus* and on tick distributions on the remaining hosts

*Sceloporus occidentalis*



*Ixodes pacificus*



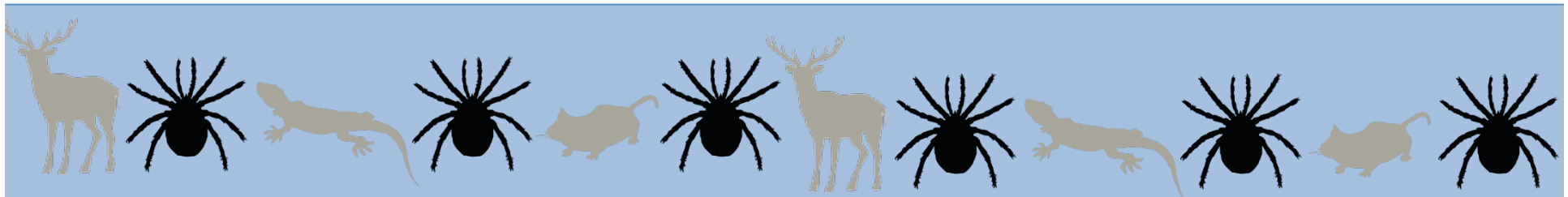
- ✓ Abundance
- ✓ Infection prevalence

Other hosts



# Hypothesis

The presence of lizards may act as a barrier for the transmission of lyme disease, due to its high host competence and lower reservoir competence

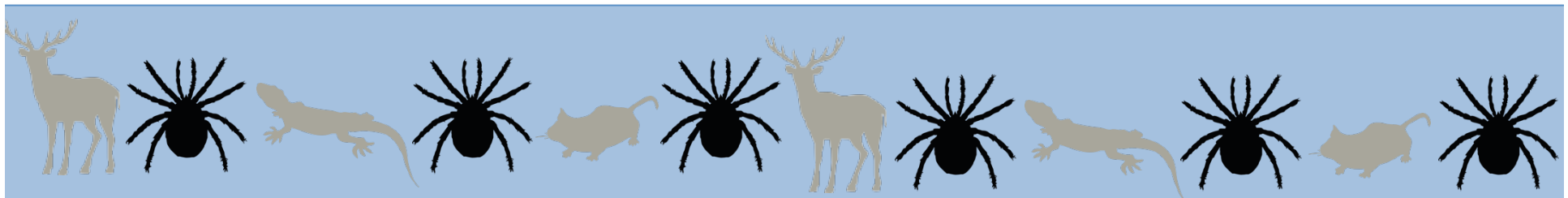


# Hypothesis

The presence of lizards may act as a barrier for the transmission of lyme disease, due to its high host competence and lower reservoir competence

## Predictions

1) If ticks switch to other hosts when lizards are scarce, and feed with equal success, then tick abundance might not decline and infection prevalence would increase.



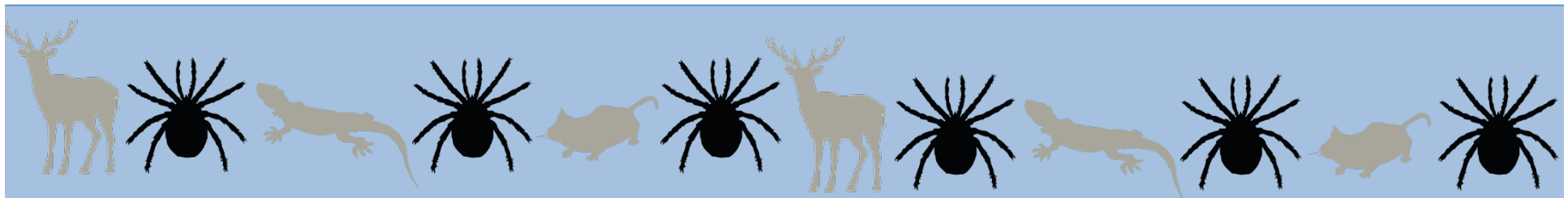
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2) Alternatively, reduced lizard abundance might lower tick abundance if ticks generally fail to find alternative, high-quality hosts





# Hypothesis

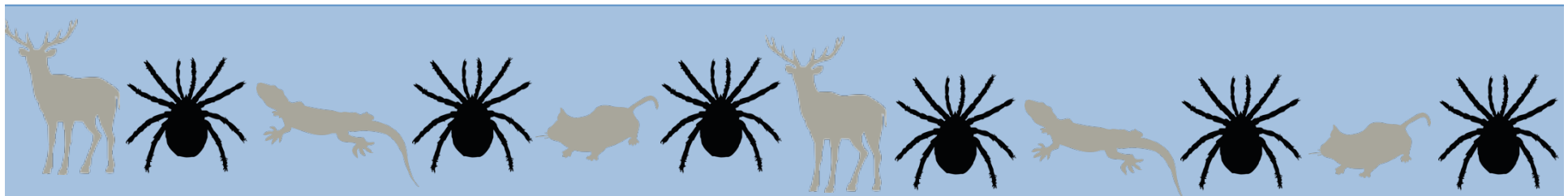
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2) Alternatively, reduced lizard abundance might lower tick abundance if ticks generally fail to find alternative, high-quality hosts

If there is a strong preference for lizards – no switch to an alternate host

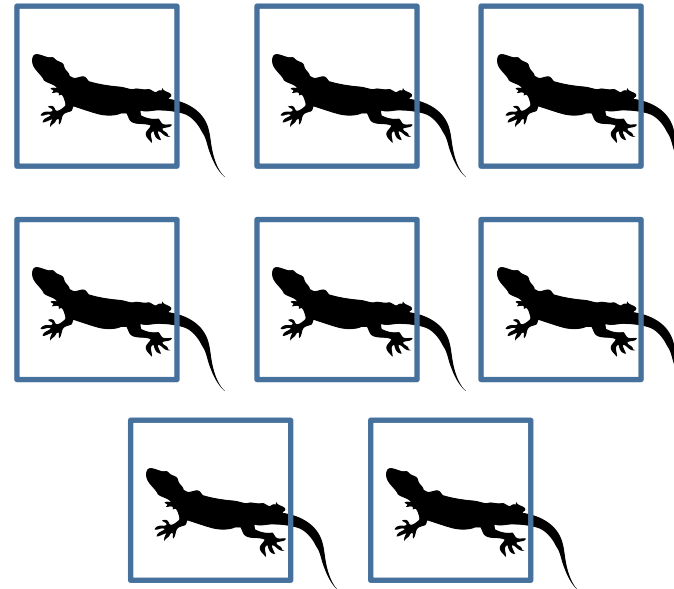
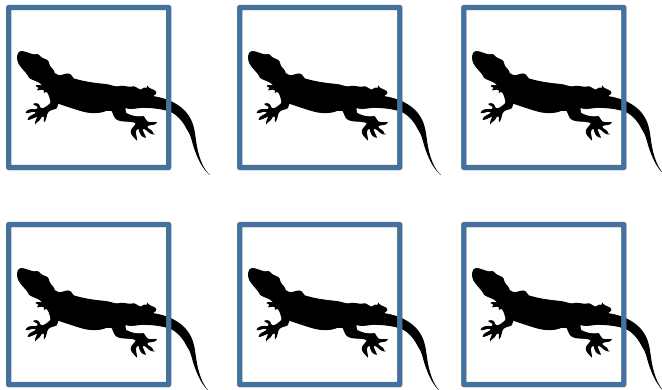


# Methods

Marin County, CA, north of San Francisco



14 long-term 1 ha plots

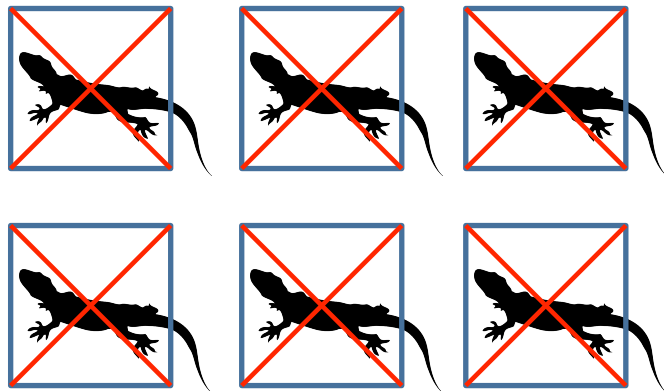


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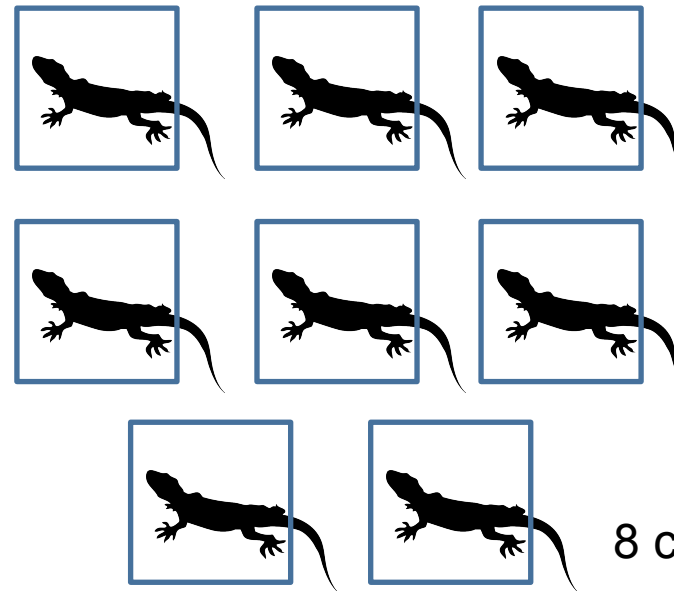
Marin County, CA, north of San Francisco



14 long-term 1 ha plots



6 experimental removal plots

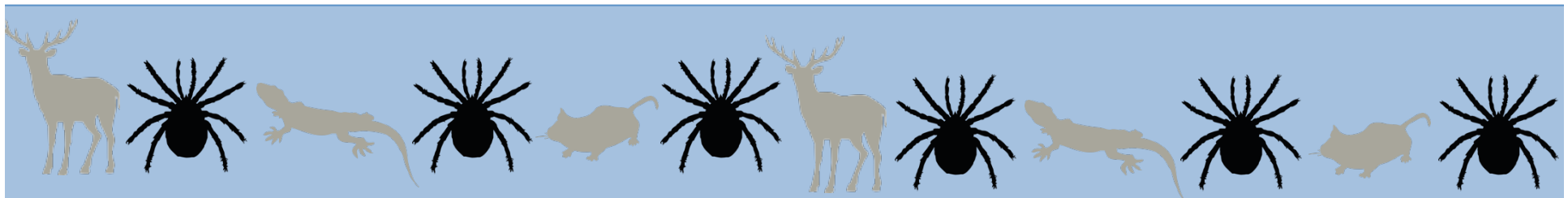


8 control plots

# Results

The effect of lizard removals on the density and infection prevalence of questing ticks was evaluated:

- ✓ Sampling larval ticks in the year of removals (time  $t$ )
- ✓ Nymphal ticks the year after the experimental manipulation



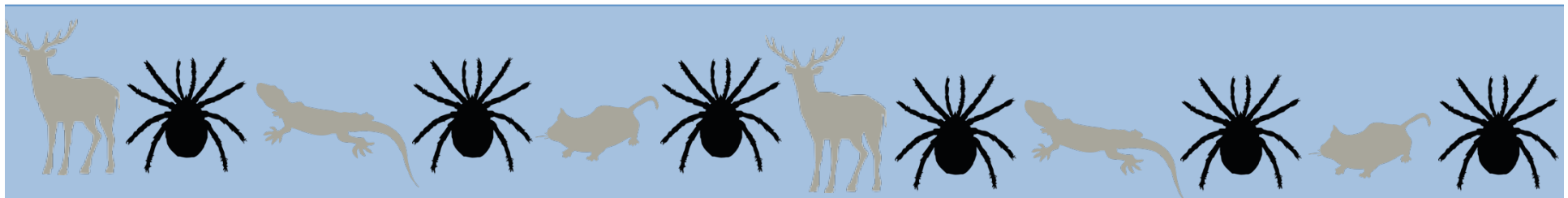
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Time t:

↑ Larvae ticks → were not able to immediately find an alternate blood meal host



# Results

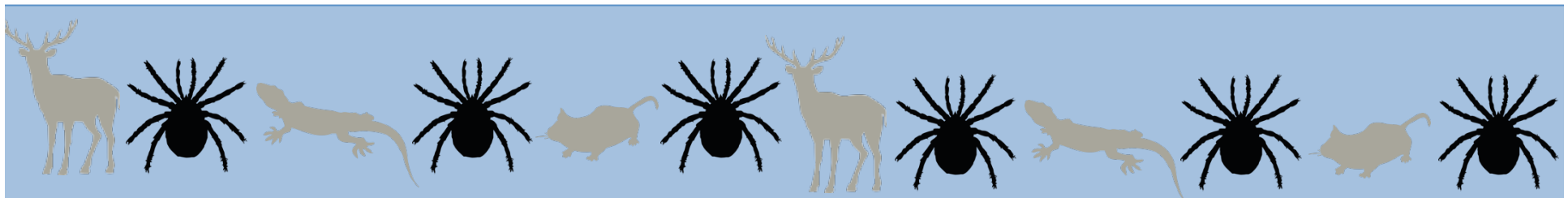
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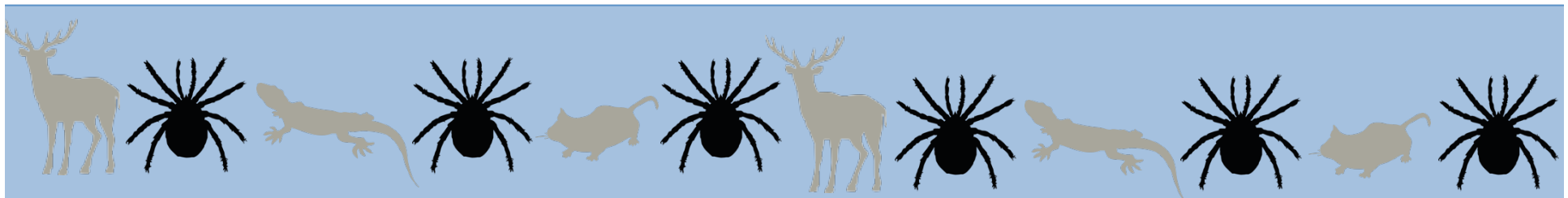
↑ Larvae ticks → were not able to immediately find an alternate blood meal host

↑ Larval burdens on female *N. fuscipes* → lizard removal elevated larval tick burden on female woodrats



# Results

The year following lizard removal:



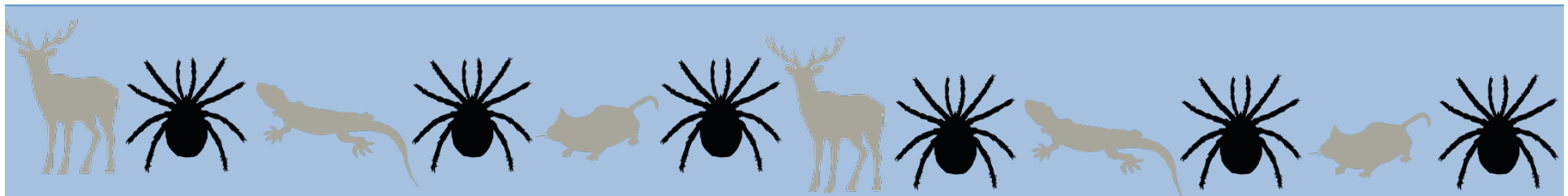
# Results

The year following lizard removal:

↓ Nymphal ticks



✓5.19% of larval *I. pacificus* did switch to a competent reservoir host (*N. fuscipes*)





# Results

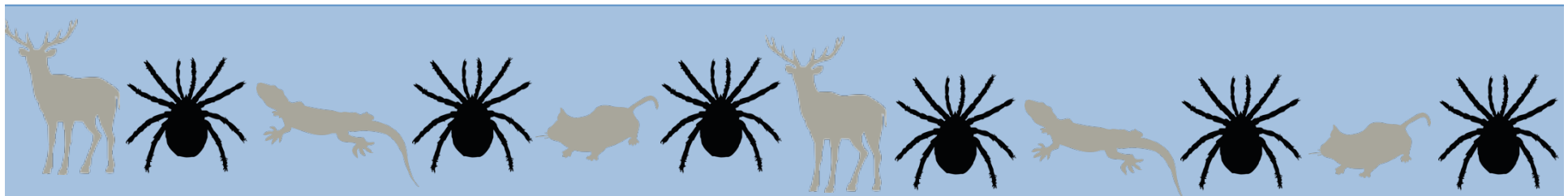
The year following lizard removal:

↓ Nymphal ticks



✓5.19% of larval *I. pacificus* did switch to a competent reservoir host (*N. fuscipes*)

✓The increased larval burden on *N. fuscipes* was not enough to absorb 94.81% of larvae that would have fed on lizards



# Results

The year following lizard removal:

↓ Nymphal ticks



✓ 5.19% of larval *I. pacificus* did switch to a competent reservoir host (*N. fuscipes*)

✓ The increased larval burden on *N. fuscipes* was not enough to absorb 94.81% of larvae that would have fed on lizards

Results indicate that an incompetent reservoir for a pathogen may, in fact, increase disease risk through the maintenance of higher vector density and therefore, higher density of infected vectors

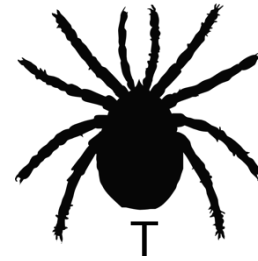
Larvae



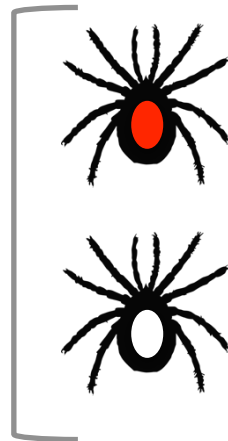
Nymph



Tick

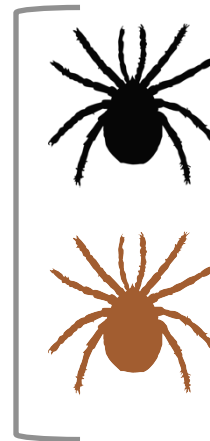


L = Larvae  
N = Nymph  
T = Tick  
  
f = hungry  
a = fed  
  
i = infected  
s = susceptible



fed

hungry



susceptible

infected



L<sup>f</sup>



L<sup>ai</sup>

L<sup>as</sup>



N<sup>fi</sup>

N<sup>fs</sup>



N<sup>ai</sup>

N<sup>as</sup>



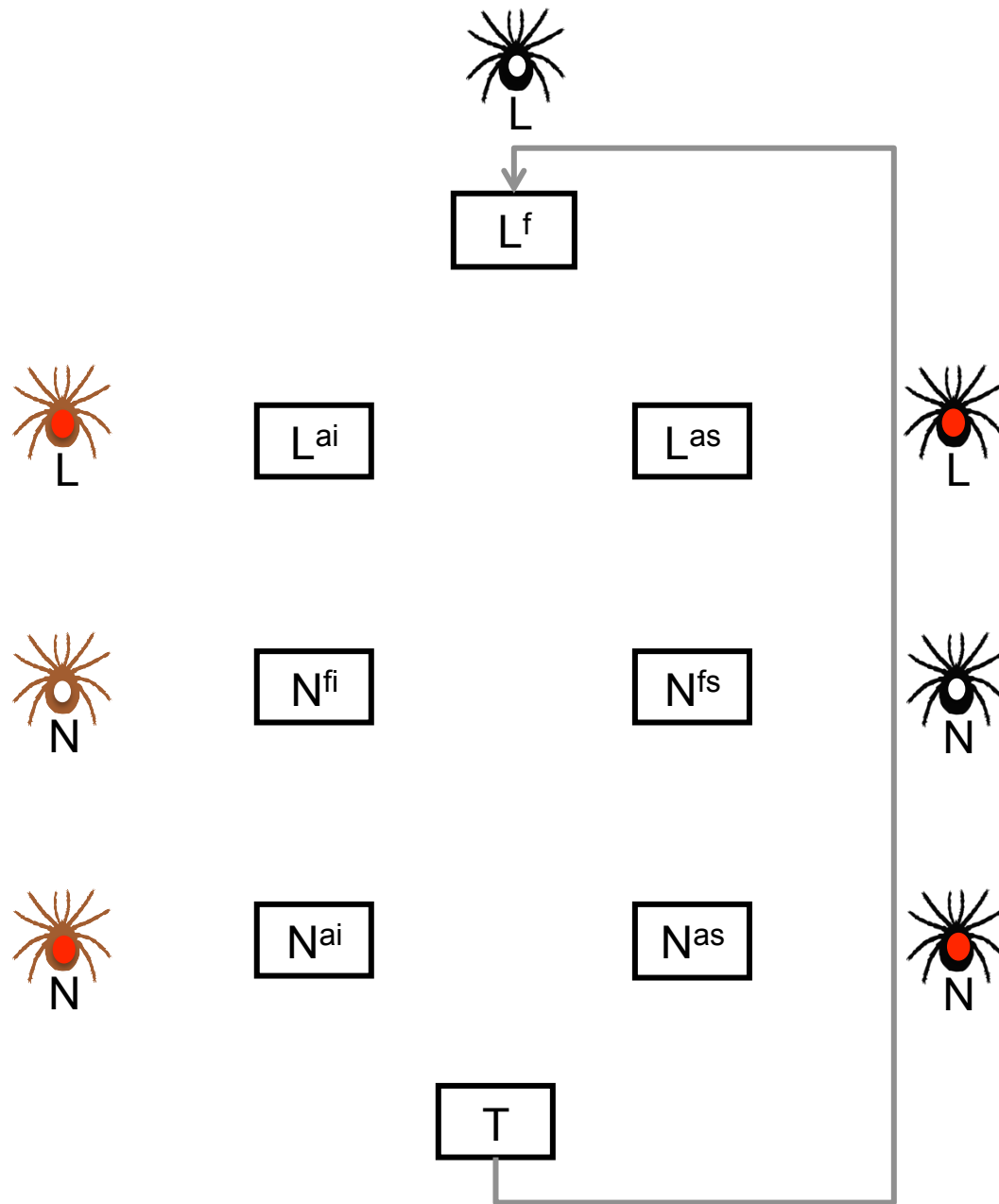
T



L= Larvae  
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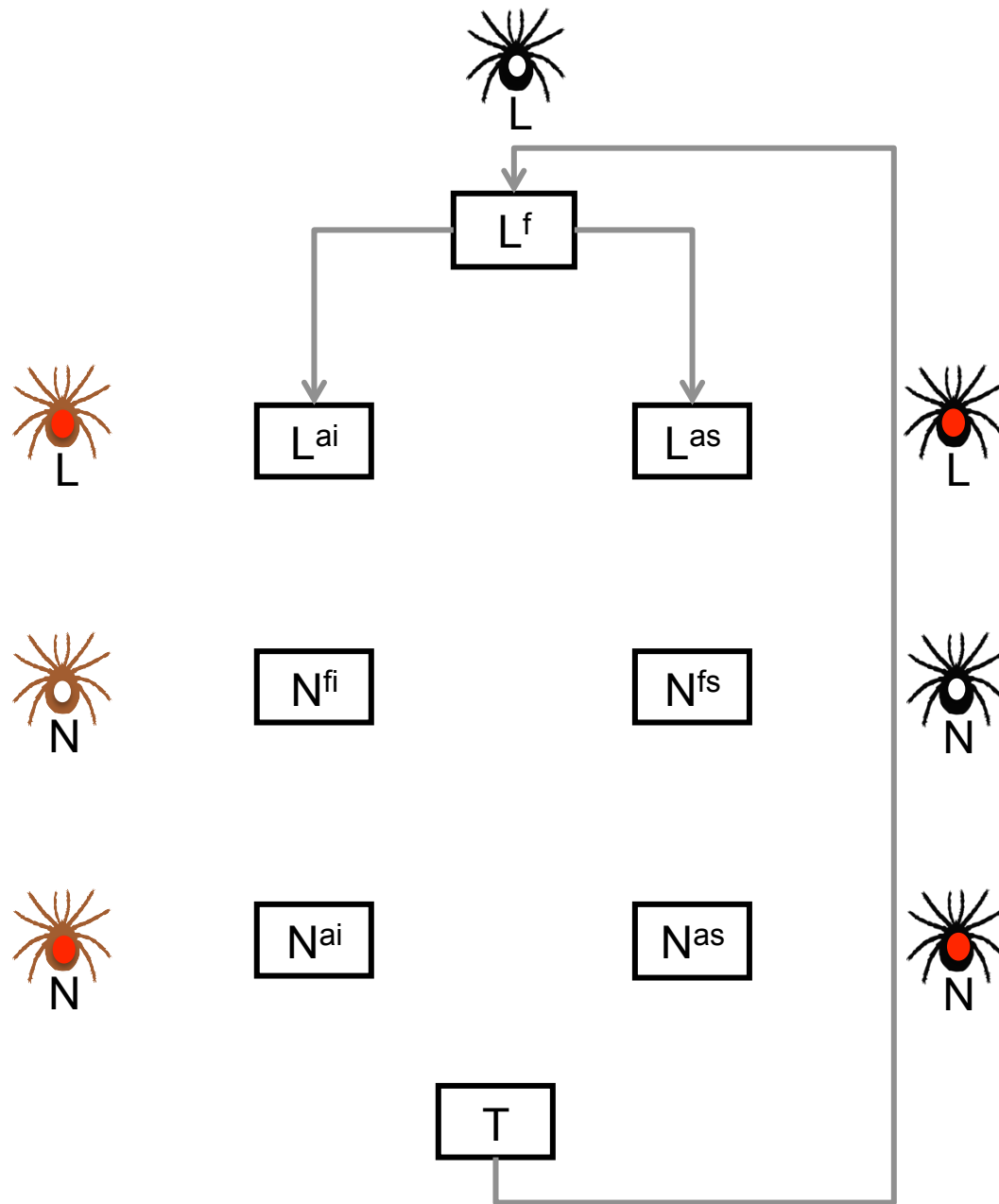
i = infected  
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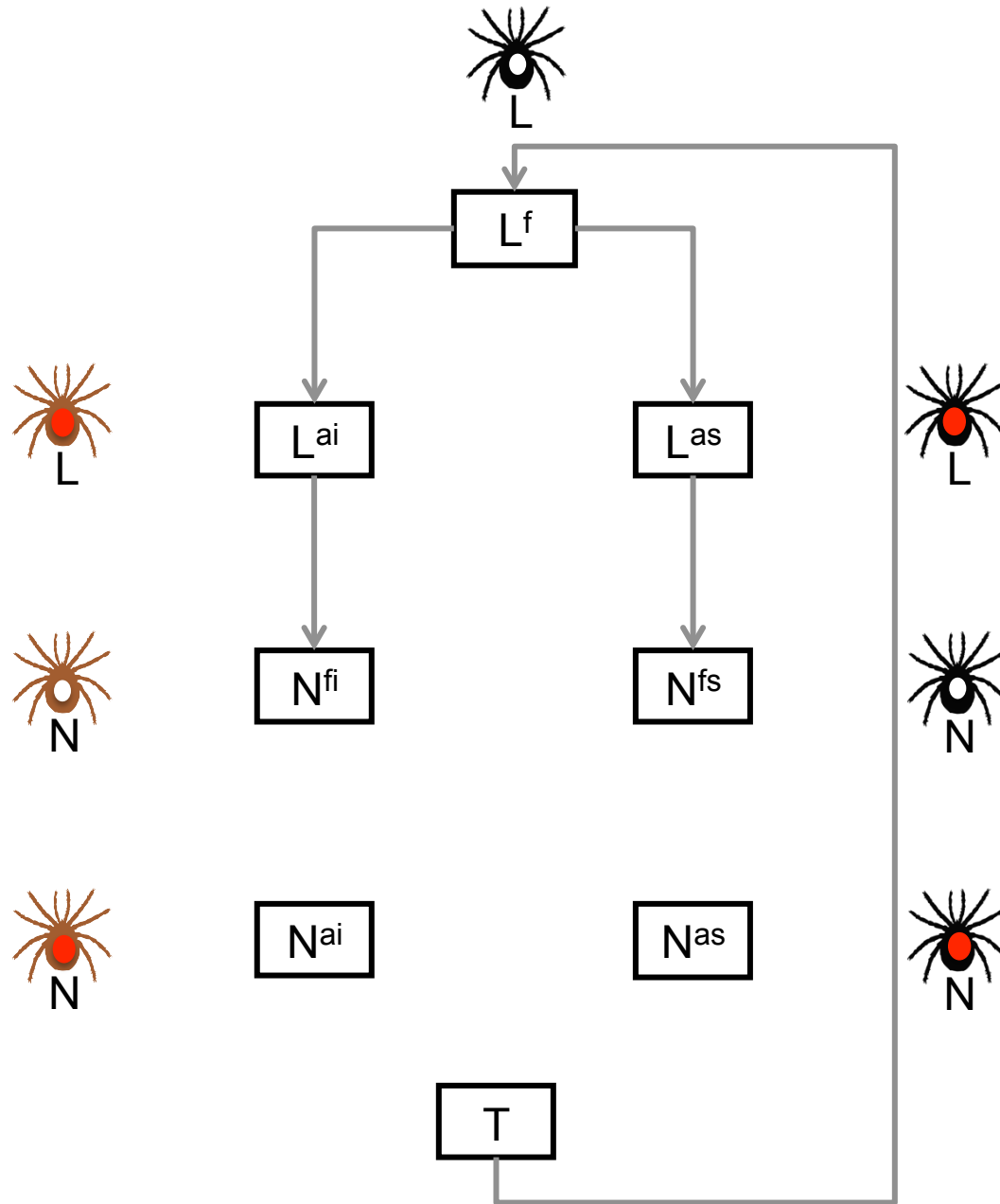
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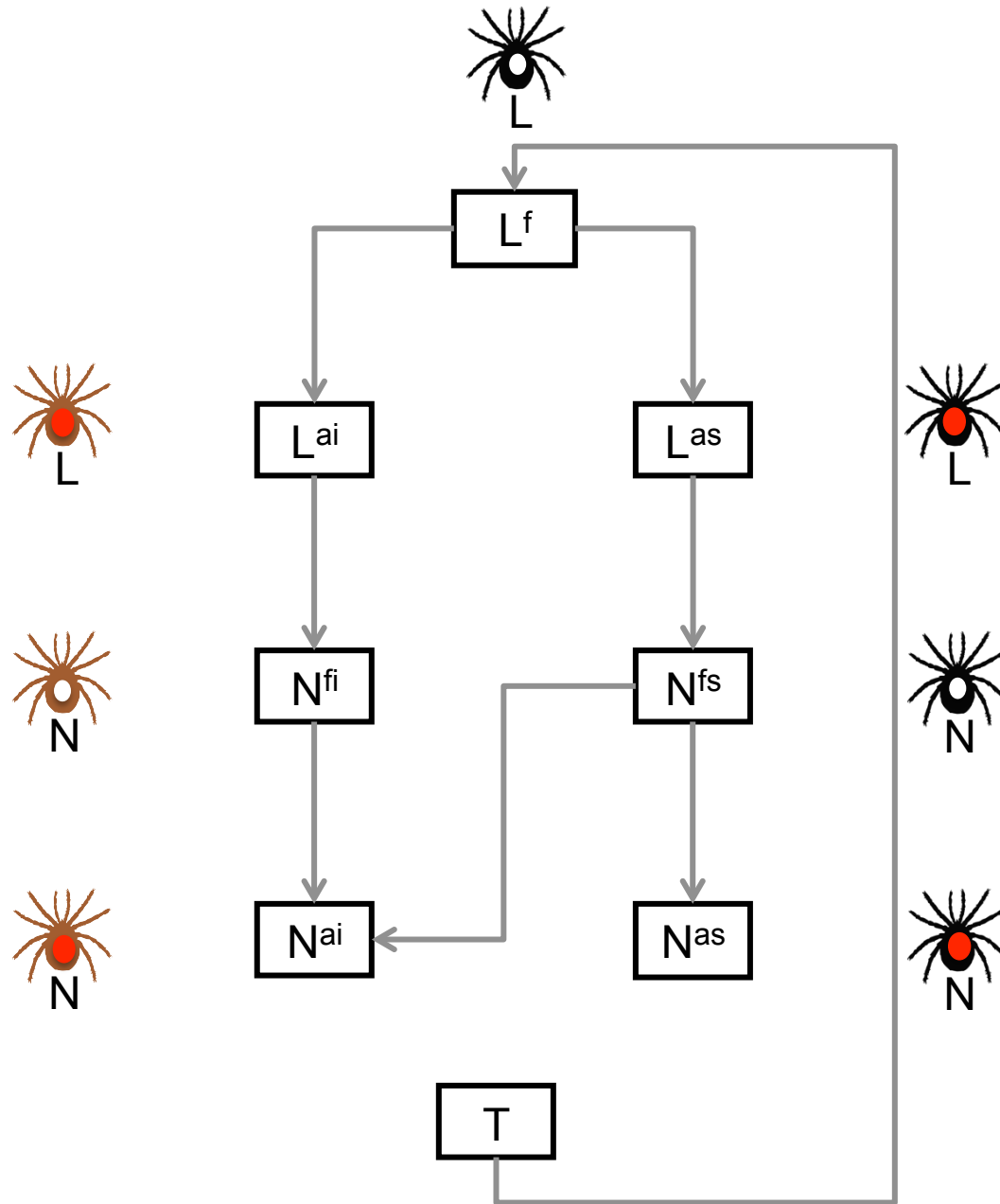
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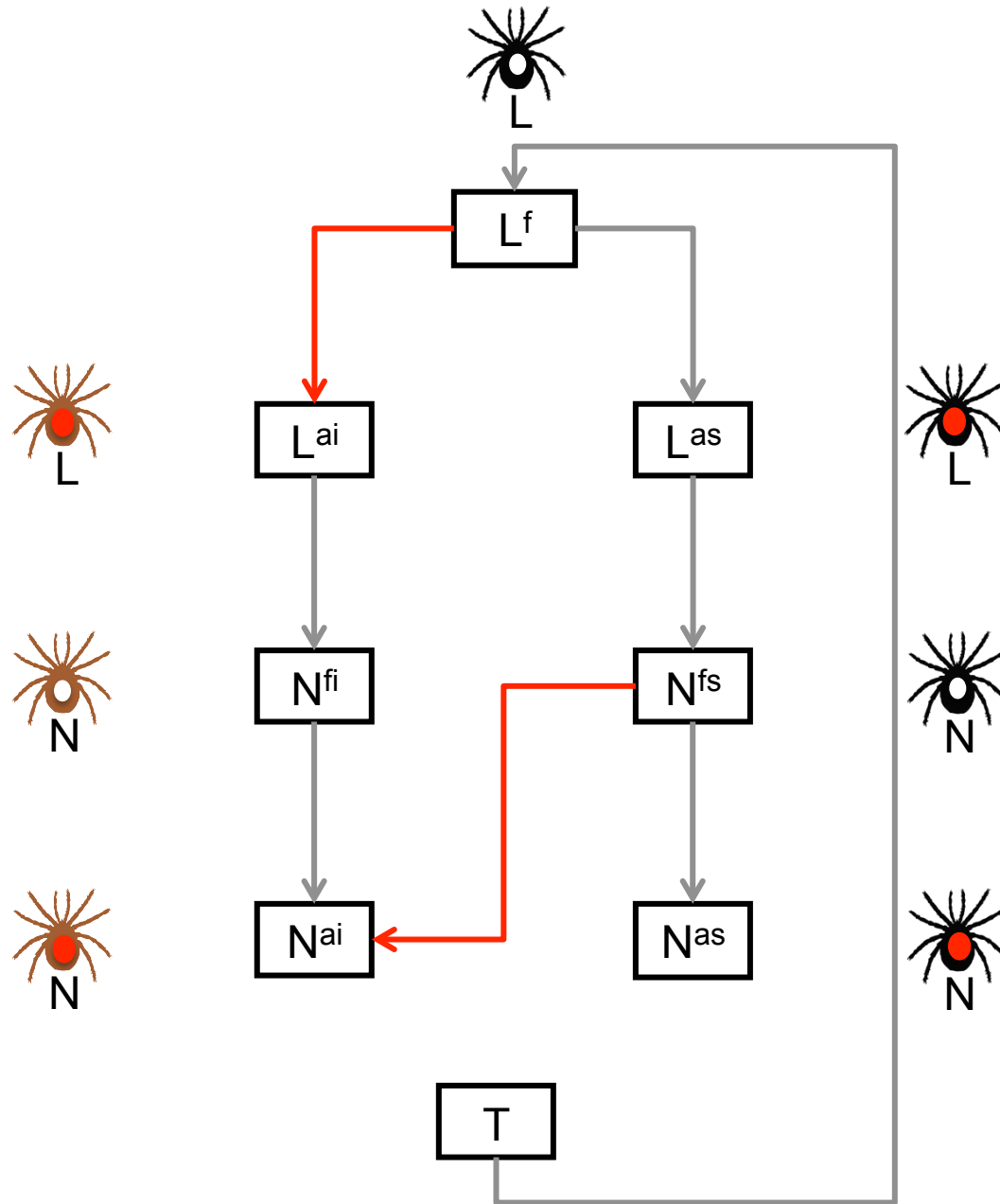


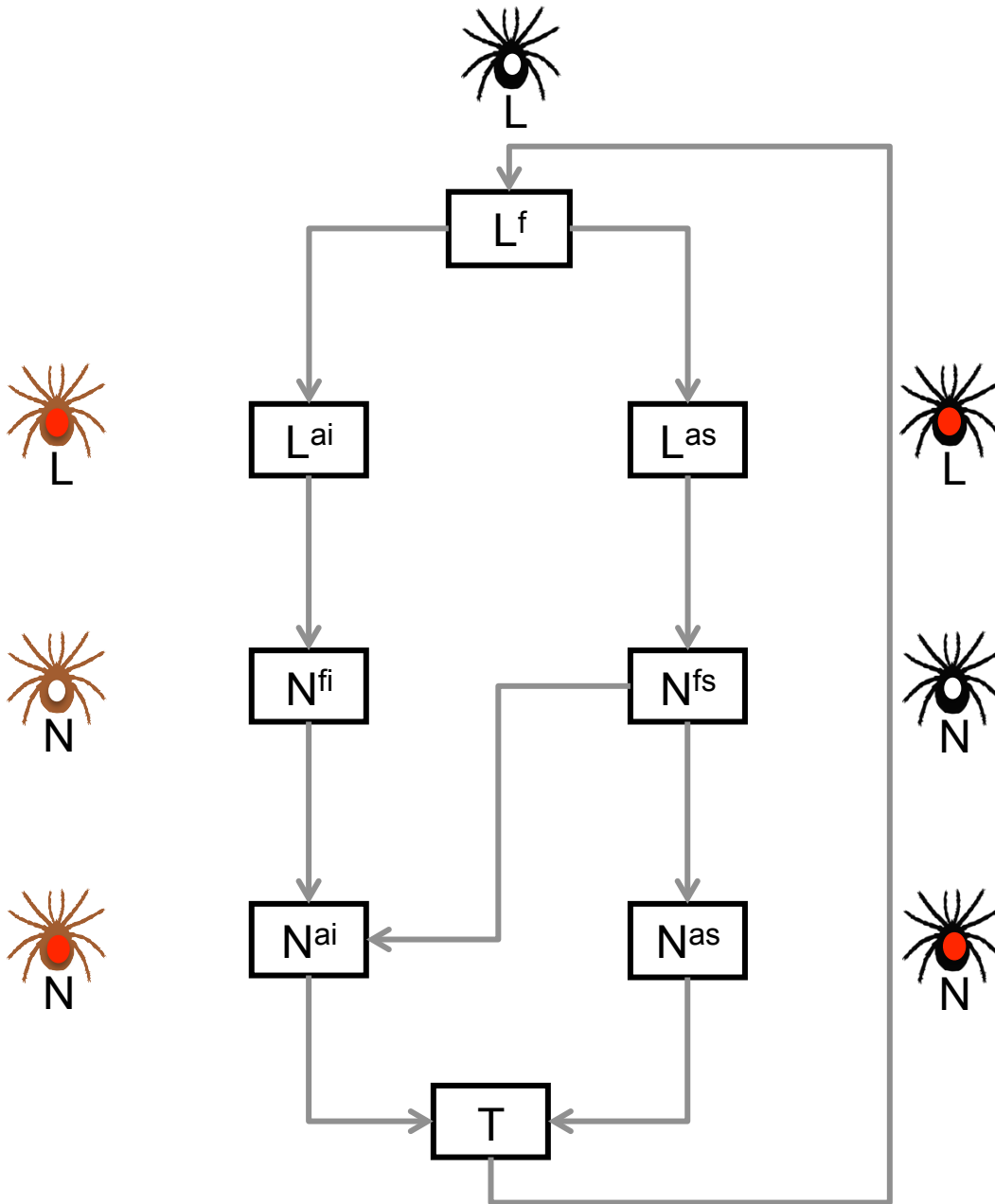
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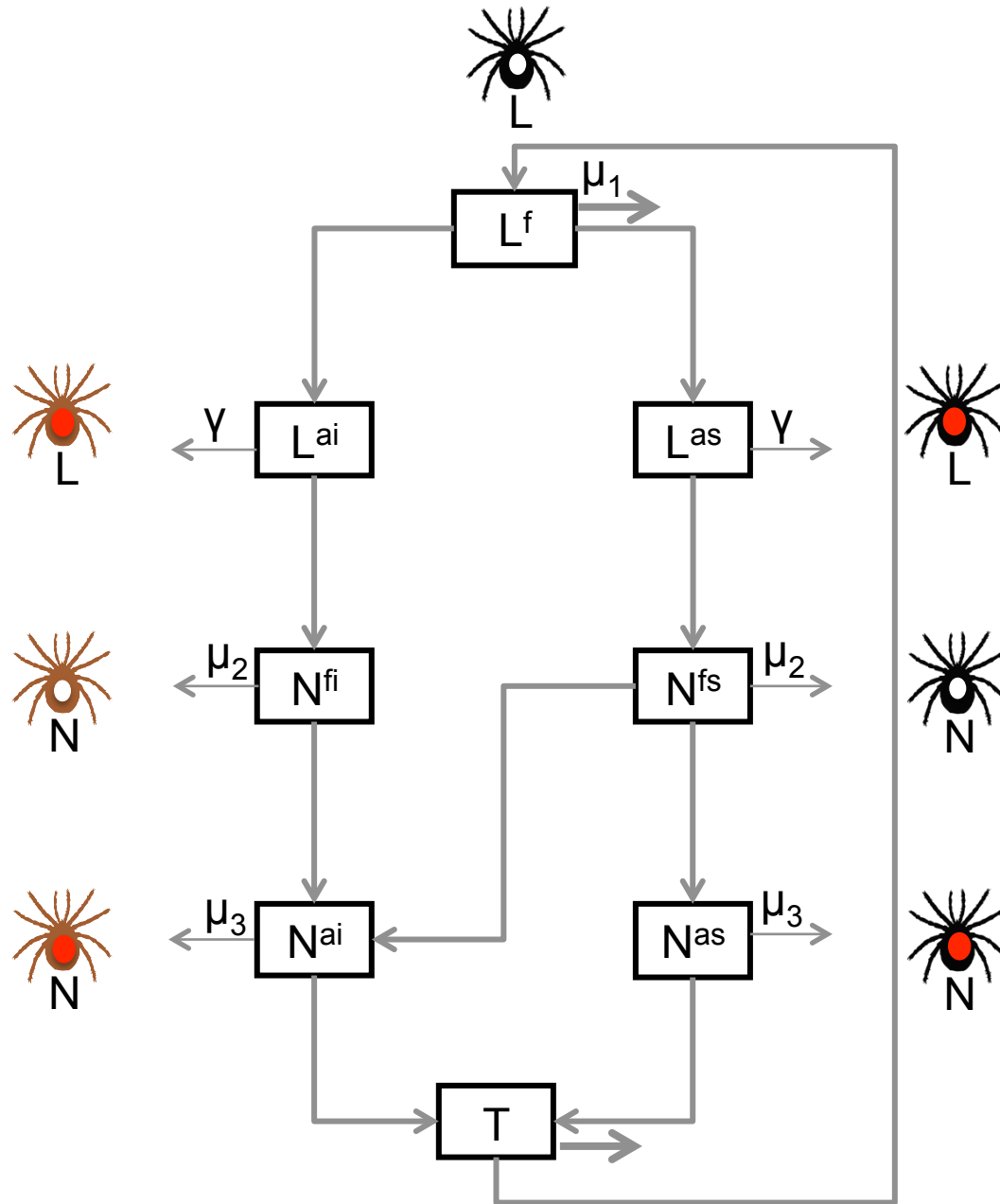




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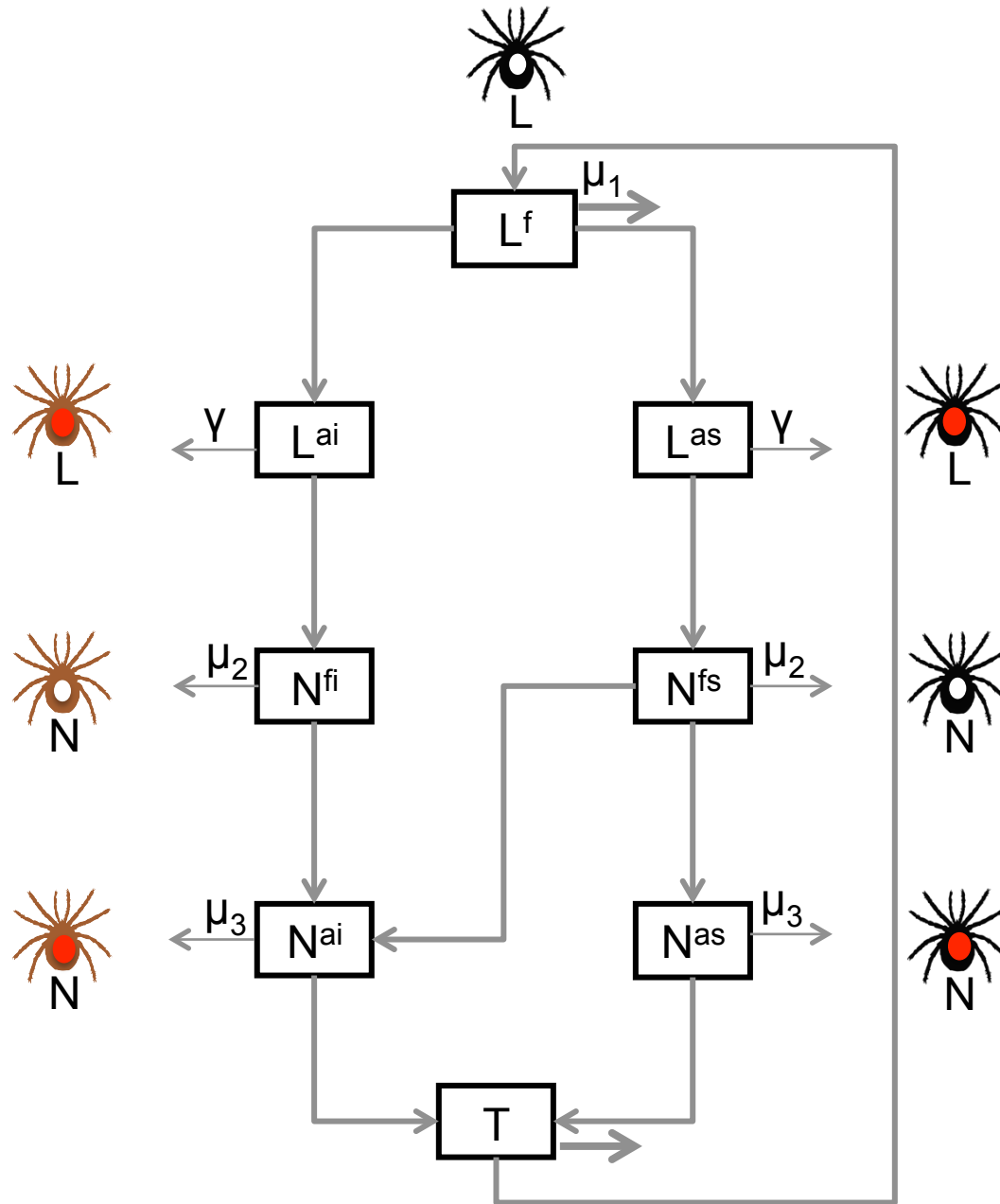
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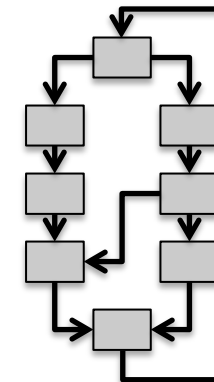
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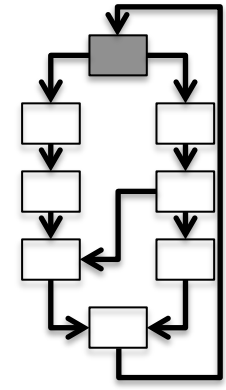
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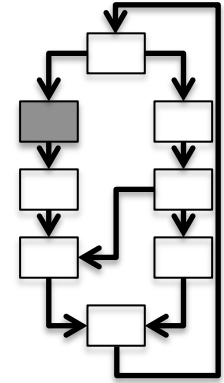
Larvae 

$$L_{t+1}^f = eE_t \quad \text{spider icon}$$




Larvae 

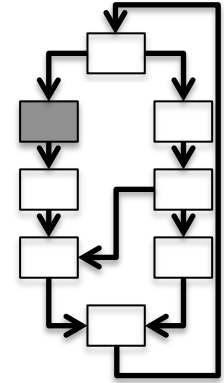
$$L_{t+1}^f = eE_t \quad \text{🕷}$$




$$L_{t+1}^{ai} = \left( \frac{V_A H_A A_t^i}{(A_t^i + A_t^s) H_A + R H_R + 1} \right) L_t^f (1 - \mu_1) \quad \text{🕷}$$

Larvae 

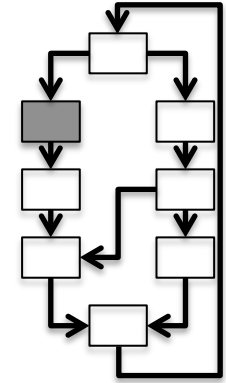
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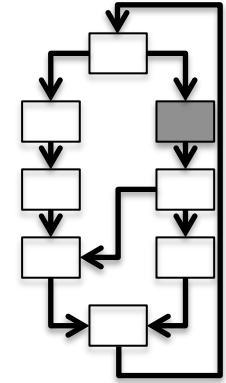
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Larvae 

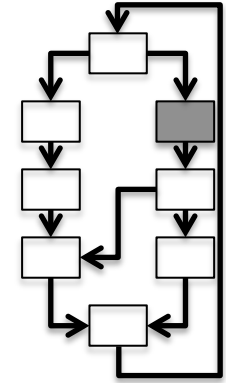


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$$L_{t+1}^{as} = \left( \frac{H_A A_t^s + (1 - V_A) H_A A_t^i + R H_{R+1}}{(A_t^i + A_t^s) H_A + R H_{R+1}} \right) L_t^f (1 - \mu_1) \quad \text{🕷}$$


Larvae 

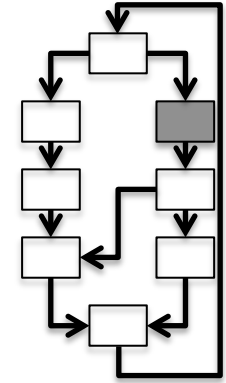


$$L_{t+1}^f = eE_t \quad \text{🕷}$$

$$L_{t+1}^{ai} = \left( \frac{V_A H_A A_t^i}{(A_t^i + A_t^s) H_A + R H_{R+1}} \right) L_t^f (1 - \mu_1) \quad \text{🕷}$$

$$L_{t+1}^{as} = \left( \frac{H_A A_t^s + (1 - V_A) H_A A_t^i + R H_{R+1}}{(A_t^i + A_t^s) H_A + R H_{R+1}} \right) L_t^f (1 - \mu_1) \quad \text{🕷}$$

Larvae 



$$L_{t+1}^f = eE_t \quad \text{🕷}$$

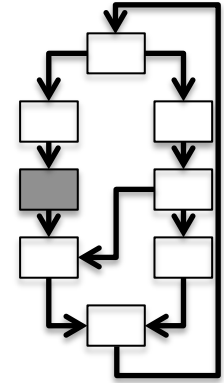
$$L_{t+1}^{ai} = \left( \frac{V_A H_A A_t^i}{(A_t^i + A_t^s) H_A + R H_{R+1}} \right) L_t^f (1 - \mu_1) \quad \text{🕷}$$

$$L_{t+1}^{as} = \left( \frac{H_A A_t^s + (1 - V_A) H_A A_t^i + R H_{R+1}}{(A_t^i + A_t^s) H_A + R H_{R+1}} \right) \boxed{L_t^f (1 - \mu_1)} \quad \text{🕷}$$

Nymph



$$N_{t+1}^{fi} = (1 - \gamma)L_t^{ai}$$



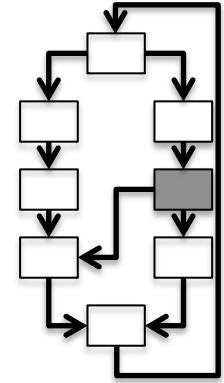
Nymph



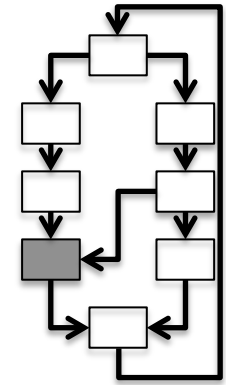
$$N_{t+1}^{fi} = (1 - \gamma)L_t^{ai}$$



$$N_{t+1}^{fs} = (1 - \gamma)L_t^{as}$$



Nymph

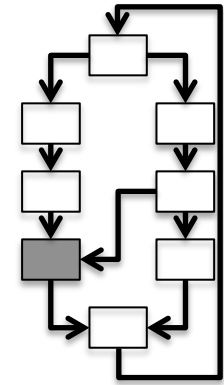


$$N_{t+1}^{fi} = (1 - \gamma) L_t^{ai} \quad \text{🕷️}$$

$$N_{t+1}^{fs} = (1 - \gamma) L_t^{as} \quad \text{🕷️}$$

$$N_{t+1}^{ai} = \left( \frac{V_A H_A A_t^i}{(A_t^i + A_t^s) H_A + R H_R + 1} \right) N_t^{fs} (1 - \mu_2) + N_t^{fi} (1 - \mu_2) \quad \text{🕷️}$$

Nymph

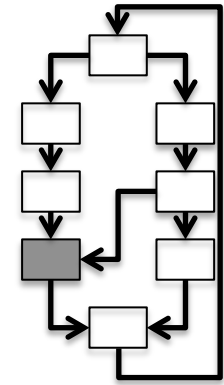


$$N_{t+1}^{fi} = (1 - \gamma) L_t^{ai} \quad \text{🕷️}$$

$$N_{t+1}^{fs} = (1 - \gamma) L_t^{as} \quad \text{🕷️}$$

$$N_{t+1}^{ai} = \left( \frac{V_A H_A A_t^i}{(A_t^i + A_t^s) H_A + R H_R + 1} \right) N_t^{fs} (1 - \mu_2) + N_t^{fi} (1 - \mu_2) \quad \text{🕷️}$$

Nymph



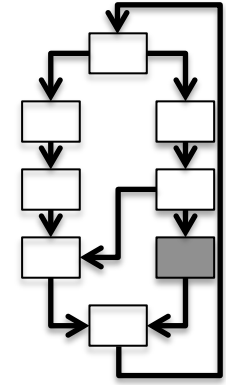
$$N_{t+1}^{fi} = (1 - \gamma)L_t^{ai} \quad \text{🕷️}$$

$$N_{t+1}^{fs} = (1 - \gamma)L_t^{as} \quad \text{🕷️}$$

$$N_{t+1}^{ai} = \left( \frac{V_A H_A A_t^i}{(A_t^i + A_t^s) H_A + R H_R + 1} \right) N_t^{fs} (1 - \mu_2) + N_t^{fi} (1 - \mu_2) \quad \text{🕷️}$$



Nymph



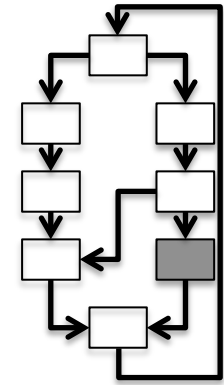
$$N_{t+1}^{fi} = (1 - \gamma) L_t^{ai} \quad \text{🕷️}$$

$$N_{t+1}^{fs} = (1 - \gamma) L_t^{as} \quad \text{🕷️}$$

$$N_{t+1}^{ai} = \left( \frac{V_A H_A A_t^i}{(A_t^i + A_t^s) H_A + R H_{R+1}} \right) N_t^{fs} (1 - \mu_2) + N_t^{fi} (1 - \mu_2) \quad \text{🕷️}$$

$$N_{t+1}^{as} = \left( \frac{H_A A_t^s + (1 - V_A) H_A A_t^i + R H_{R+1}}{(A_t^i + A_t^s) H_A + R H_{R+1}} \right) N_t^{fs} (1 - \mu_2) \quad \text{🕷️}$$

Nymph



$$N_{t+1}^{fi} = (1 - \gamma) L_t^{ai} \quad \text{🕷️}$$

$$N_{t+1}^{fs} = (1 - \gamma) L_t^{as} \quad \text{🕷️}$$

$$N_{t+1}^{ai} = \left( \frac{V_A H_A A_t^i}{(A_t^i + A_t^s) H_A + R H_{R+1}} \right) N_t^{fs} (1 - \mu_2) + N_t^{fi} (1 - \mu_2) \quad \text{🕷️}$$

$$N_{t+1}^{as} = \left( \frac{H_A A_t^s + (1 - V_A) H_A A_t^i + R H_{R+1}}{(A_t^i + A_t^s) H_A + R H_{R+1}} \right) N_t^{fs} (1 - \mu_2) \quad \text{🕷️}$$

Nymph



$$N_{t+1}^{fi} = (1 - \gamma) L_t^{ai}$$



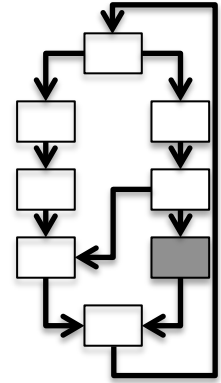
$$N_{t+1}^{fs} = (1 - \gamma) L_t^{as}$$



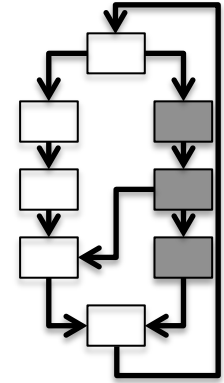
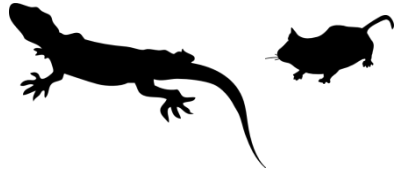
$$N_{t+1}^{ai} = \left( \frac{V_A H_A A_t^i}{(A_t^i + A_t^s) H_A + R H_{R+1}} \right) N_t^{fs} (1 - \mu_2) + N_t^{fi} (1 - \mu_2)$$



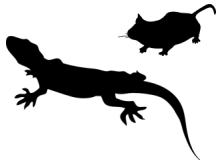
$$N_{t+1}^{as} = \left( \frac{H_A A_t^s + (1 - V_A) H_A A_t^i + R H_{R+1}}{(A_t^i + A_t^s) H_A + R H_{R+1}} \right) N_t^{fs} (1 - \mu_2)$$



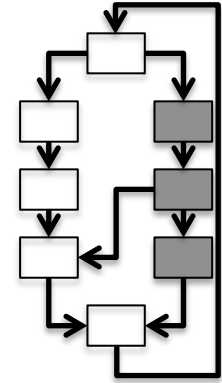
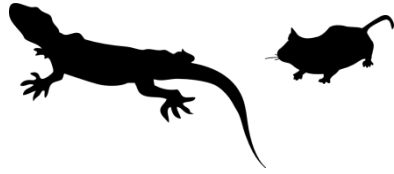
Hosts

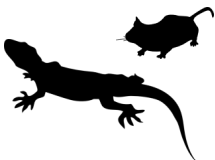


$$A_{t+1}^s = (1 - \gamma_A) A_t^s \rho_A + (1 - \gamma_A) A_t^i \rho_A + (1 - \gamma_A) A_t^s - \epsilon_A \mu_2 \frac{N_t^{fi}}{N_t^{fi} + N_t^{fs}} (1 - \gamma_A) A_t^s$$

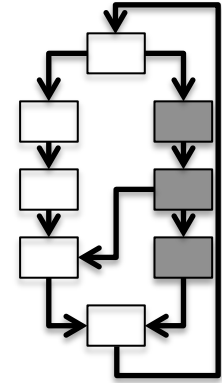
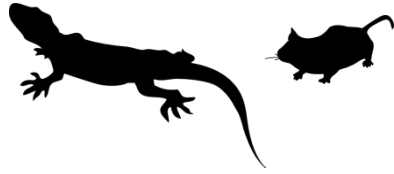


Hosts

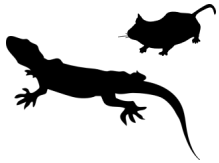


$$A_{t+1}^s = \boxed{(1 - \gamma_A) A_t^s \rho_A} + (1 - \gamma_A) A_t^i \rho_A$$

$$+ (1 - \gamma_A) A_t^s - \epsilon_A \mu_2 \frac{N_t^{fi}}{N_t^{fi} + N_t^{fs}} (1 - \gamma_A) A_t^s$$

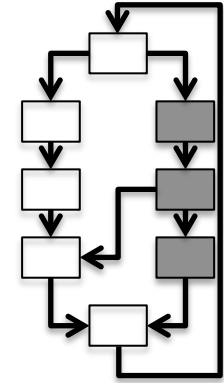
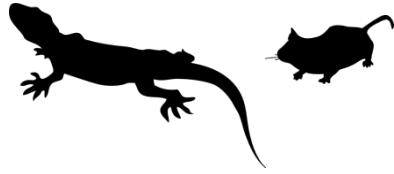
Hosts



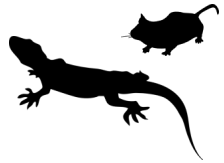
$$A_{t+1}^s = (1 - \gamma_A)A_t^s \rho_A + (1 - \gamma_A)A_t^i \rho_A + (1 - \gamma_A)A_t^s - \epsilon_A \mu_2 \frac{N_t^{fi}}{N_t^{fi} + N_t^{fs}} (1 - \gamma_A)A_t^s$$



Hosts

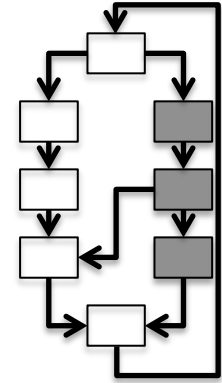
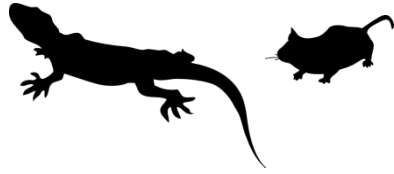


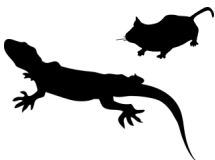
$$A_{t+1}^s = (1 - \gamma_A) A_t^s \rho_A + (1 - \gamma_A) A_t^i \rho_A$$



$$+ (1 - \gamma_A) A_t^s - \epsilon_A \mu_2 \frac{N_t^{fi}}{N_t^{fi} + N_t^{fs}} (1 - \gamma_A) A_t^s$$

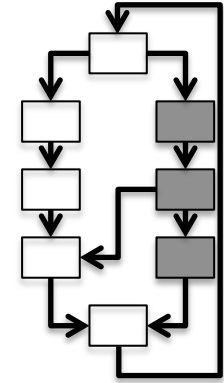
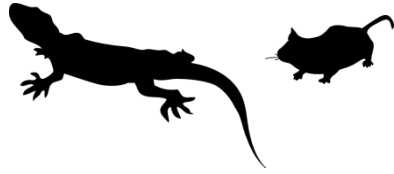
Hosts



$$A_{t+1}^s = (1 - \gamma_A) A_t^s \rho_A + (1 - \gamma_A) A_t^i \rho_A + (1 - \gamma_A) A_t^s \left[ -\epsilon_A \mu_2 \frac{N_t^{fi}}{N_t^{fi} + N_t^{fs}} \right] (1 - \gamma_A) A_t^s$$




Hosts

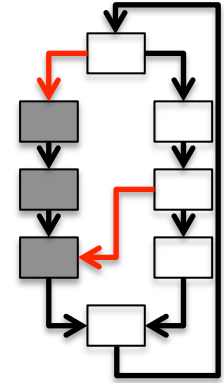
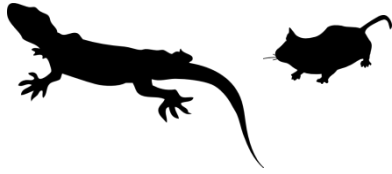


$$A_{t+1}^s = (1 - \gamma_A) A_t^s \rho_A + (1 - \gamma_A) A_t^i \rho_A$$

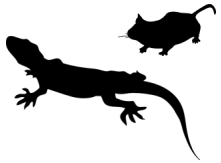


$$+ (1 - \gamma_A) A_t^s - \epsilon_A \mu_2 \frac{N_t^{fi}}{N_t^{fi} + N_t^{fs}} (1 - \gamma_A) A_t^s$$

Hosts



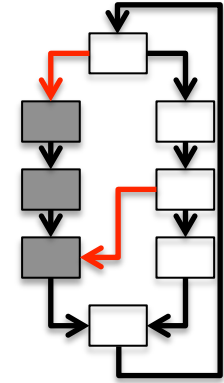
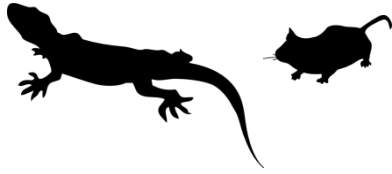
$$A_{t+1}^s = (1 - \gamma_A) A_t^s \rho_A + (1 - \gamma_A) A_t^i \rho_A + (1 - \gamma_A) A_t^s - \epsilon_A \mu_2 \frac{N_t^{fi}}{N_t^{fi} + N_t^{fs}} (1 - \gamma_A) A_t^s$$



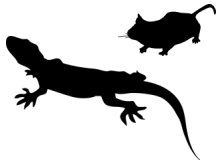
$$A_{t+1}^i = (1 - \gamma_A) A_t^i + \epsilon_A (1 - \gamma_A) \mu_2 \frac{N_t^{fi}}{N_t^{fi} + N_t^{fs}} A_t^s$$



Hosts



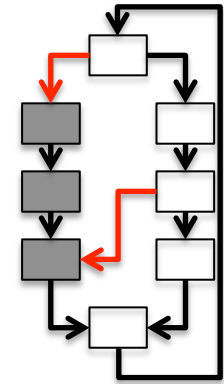
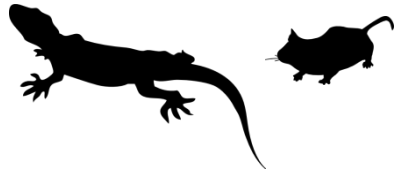
$$A_{t+1}^s = (1 - \gamma_A) A_t^s \rho_A + (1 - \gamma_A) A_t^i \rho_A + (1 - \gamma_A) A_t^s - \epsilon_A \mu_2 \frac{N_t^{fi}}{N_t^{fi} + N_t^{fs}} (1 - \gamma_A) A_t^s$$



$$A_{t+1}^i = \boxed{(1 - \gamma_A) A_t^i} + \epsilon_A (1 - \gamma_A) \mu_2 \frac{N_t^{fi}}{N_t^{fi} + N_t^{fs}} A_t^s$$



Hosts



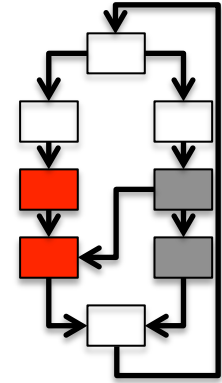
$$A_{t+1}^s = (1 - \gamma_A) A_t^s \rho_A + (1 - \gamma_A) A_t^i \rho_A + (1 - \gamma_A) A_t^s - \epsilon_A \mu_2 \frac{N_t^{fi}}{N_t^{fi} + N_t^{fs}} (1 - \gamma_A) A_t^s$$



$$A_{t+1}^i = (1 - \gamma_A) A_t^i + \epsilon_A (1 - \gamma_A) \mu_2 \frac{N_t^{fi}}{N_t^{fi} + N_t^{fs}} A_t^s$$

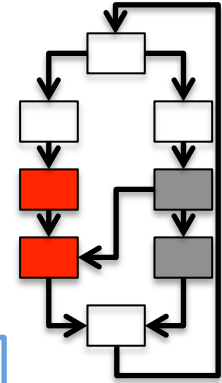


Humans



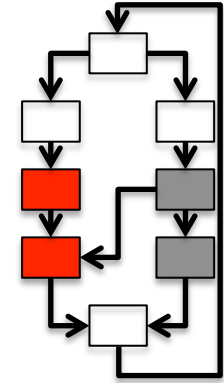
$$H_{t+1}^s = \boxed{\delta H_t^i + H_t^s} - \psi \epsilon \mu \frac{N_t^{fi}}{N_t^{fi} + N_t^{fs}} H_t^s$$

Humans



$$H_{t+1}^s = \delta H_t^i + H_t^s - \psi \epsilon \mu \frac{N_t^{fi}}{N_t^{fi} + N_t^{fs}} H_t^s$$

Humans



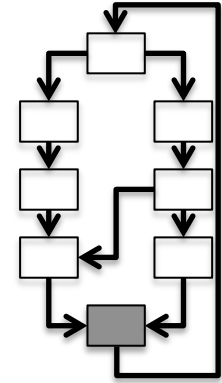
$$H_{t+1}^s = \delta H_t^i + H_t^s - \psi \epsilon \mu \frac{N_t^{fi}}{N_t^{fi} + N_t^{fs}} H_t^s$$



$$H_{t+1}^i = H_t^i - \delta H_t^i + \psi \epsilon \mu \frac{N_t^{fi}}{N_t^{fi} + N_t^{fs}} H_t^s$$

Ticks

$$T_{t+1} = (N_t^{ai} + N_t^{as})(1 - \mu_3)$$



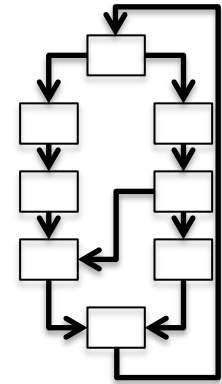


Ticks

$$T_{t+1} = (N_t^{ai} + N_t^{as})(1 - \mu_3)$$

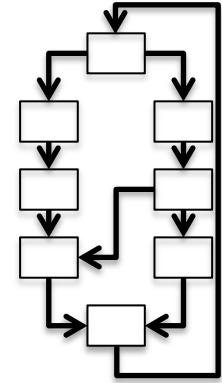
Saturation term

$$\mu = \exp^{-\sigma \frac{AH_A + RH_R}{N_t^{fi} + N_t^{fs}}}$$



Ticks

$$T_{t+1} = (N_t^{ai} + N_t^{as})(1 - \mu_3)$$



Saturation term

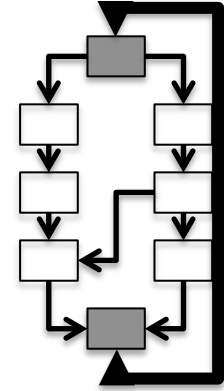
$$\mu = \exp^{-\sigma \frac{AH_A + RH_R}{N_t^{fi} + N_t^{fs}}}$$

Maintenance term

$$\rho_A = \frac{\gamma_A}{1 - \gamma_A}$$

Ticks

$$T_{t+1} = (N_t^{ai} + N_t^{as})(1 - \mu_3)$$



Saturation term

$$\mu = \exp^{-\sigma \frac{AH_A + RH_R}{N_t^{fi} + N_t^{fs}}}$$

Maintenance term

$$\rho_A = \frac{\gamma_A}{1 - \gamma_A}$$

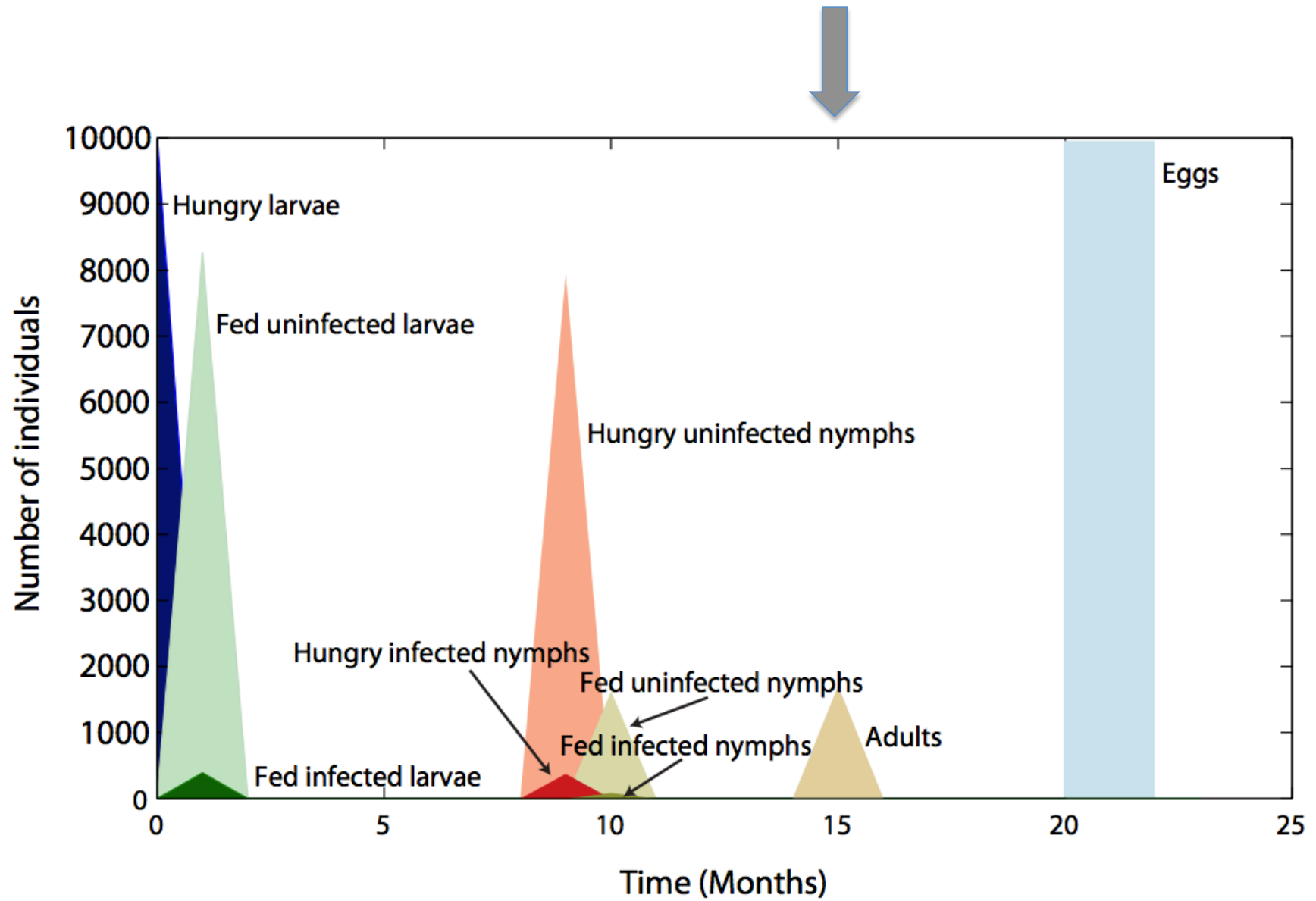
Eggs

$$E_{t+1} = N_e T_t$$



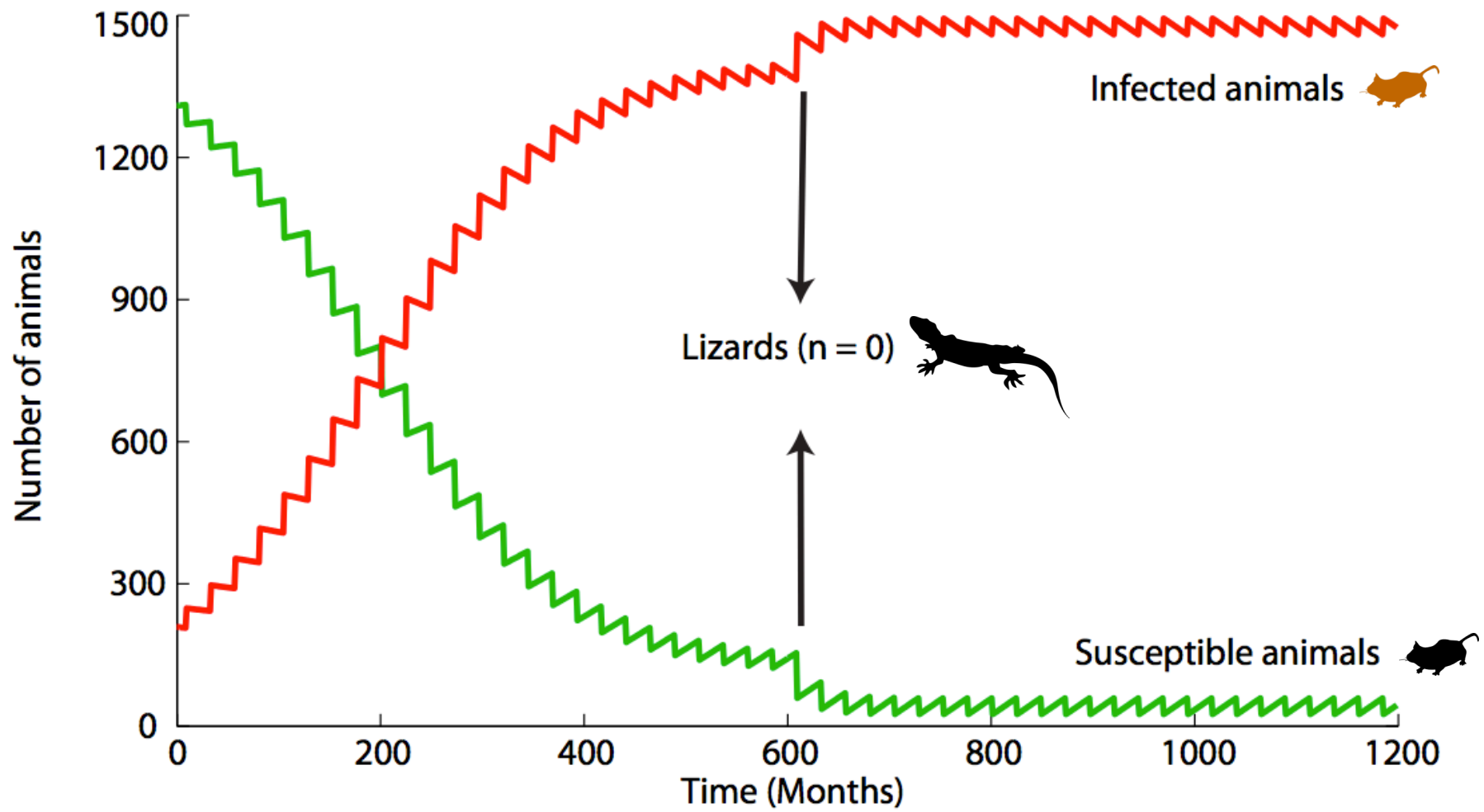


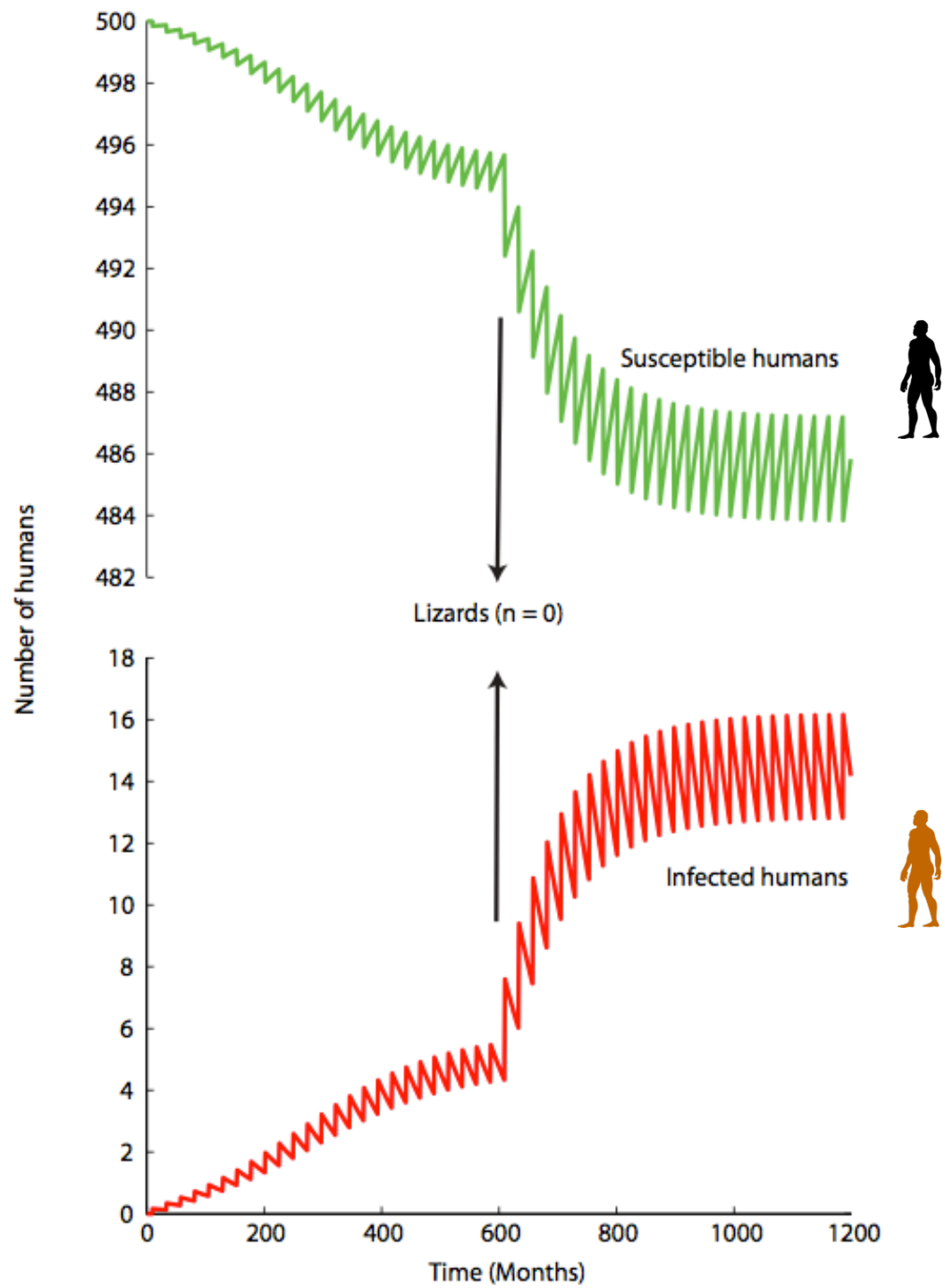












# Final Remarks

PROCEEDINGS  
OF  
THE ROYAL  
SOCIETY **B**

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**Impact of the experimental removal of lizards on Lyme disease risk**

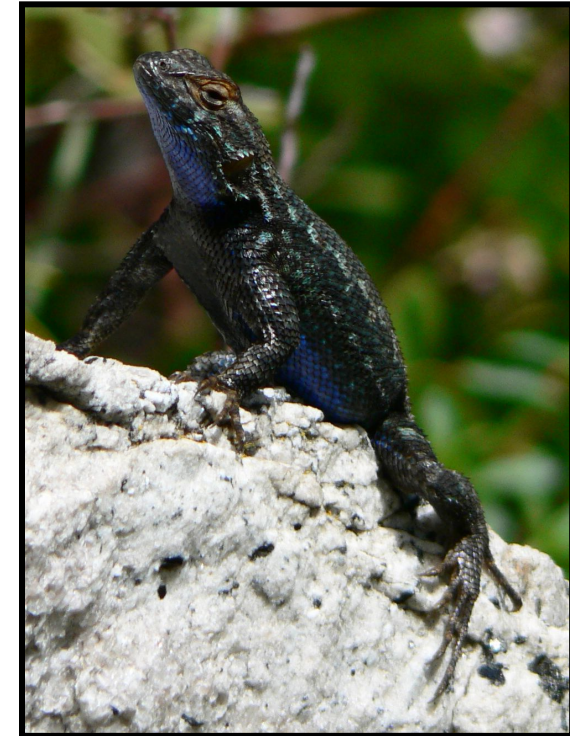
Andrea Swei<sup>1,\*</sup>, Richard S. Ostfeld<sup>2</sup>, Robert S. Lane<sup>3</sup>  
and Cheryl J. Briggs<sup>4</sup>

<sup>1</sup>Department of Integrative Biology, University of California, 3060 Valley Life Sciences Building, Berkeley, CA 94720-3140, USA

<sup>2</sup>Cary Institute of Ecosystem Studies, Millbrook, NY 12545-0129, USA

<sup>3</sup>Department of Environmental Science, Policy and Management, University of California, Berkeley, CA 94720, USA

<sup>4</sup>Department of Ecology, Evolution, and Marine Biology, University of California, Santa Barbara, CA 93106-9610, USA



- Transient state;
- Lizard = barrier

# Final Remarks

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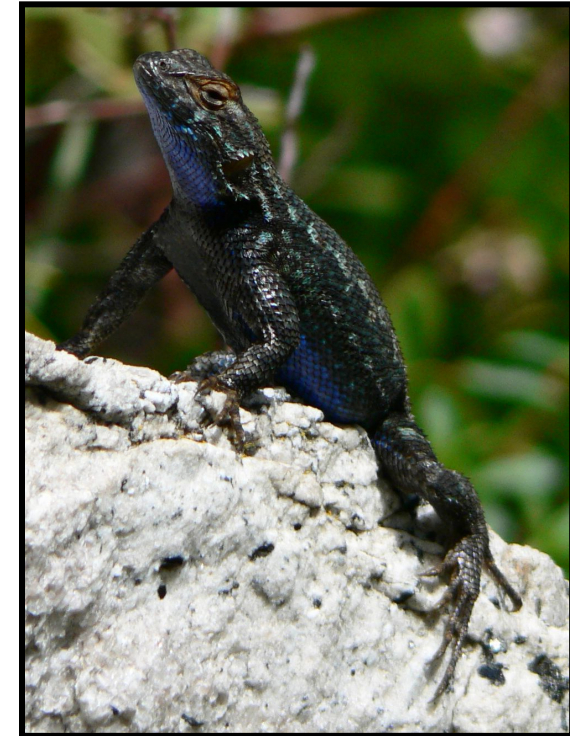
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- Transient state;
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## Questions

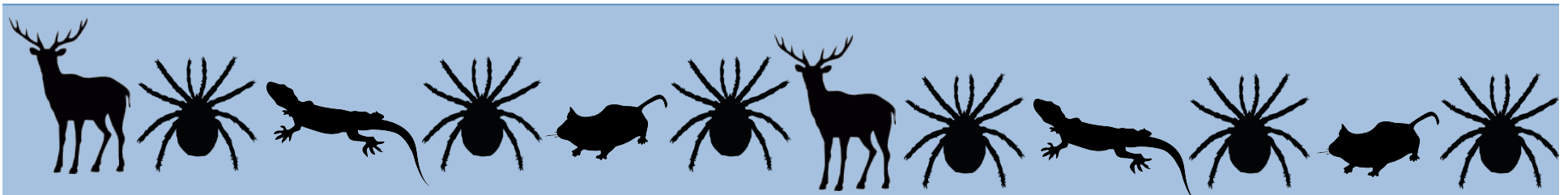
Can a mathematical model for Lyme disease transmission help understand the experimental result described above?

What else such a model can predict about:

- infection risk to humans?
- host assemblages and Lyme disease prevalence in humans and reservoirs?
- management of reservoir populations to decrease the risk of infection?

# THANKS!!!

- Organizers
- Professors
- T.As



Where

$e$  =: "Number of eggs that hatch"

$V_A$  =: "Reservoir competence on animals"

$H_A$  =: "Host competence of animals"

$R$  =: "Number of lizards"

$H_R$  =: "Host competence of lizards "

$H_H$  =: "Host competence of humans"

$\mu_1$  =: "Feeding success rate of larva"

$\mu_2$  =: "Feeding success rate of nymphs"

$\gamma$  =: "Larval death rate"

$\gamma_A$  =: "Animal death rate"

$\gamma_H$  =: "Humans death rate"

$\rho_A$  =: "New animals that born to mantain the equilibrium of the system"

$\epsilon$  =: "Efficiency of the bites on humans"

$\epsilon_A$  =: "Efficiency of the bites on animals"

$\delta$  =: "Human infection recovery rate"

$\lambda$  =: "Encounter rate of infected nymph and human"

$\psi$  =: "Death rate due to the disease"